

VALIDATION MANUAL
FE RESULTS VALIDATION

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PLATES/SHELLS STRUCTURES

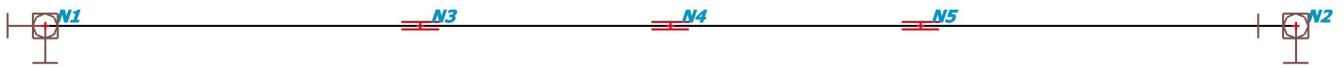
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1. TESTCASE DESCRIPTION

Uni-directional bending of an elastic (Euler) beam. Length: $L = 1,0$ m, fixed ends. Section: $I_z=1.7e-8$, $E=2.1e11$

2. MODEL

2.1. Analysis model



2.2. Nodes

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] | Member | Data |
|------|-------------|-------------|-------------|--------|----------|
| N1 | 0,000 | 0,000 | 0,000 | B1 | Sn1 |
| N2 | 1,000 | 0,000 | 0,000 | B1 | Sn2 |
| N3 | 0,300 | 0,000 | 0,000 | B1 | F1 M1 |

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] | Member | Data |
|------|-------------|-------------|-------------|--------|----------|
| N4 | 0,500 | 0,000 | 0,000 | B1 | |
| N5 | 0,700 | 0,000 | 0,000 | B1 | F2 F3 |

2.3. Members

| Name | Cross-section | Material | Length [m] | Beg. node | End node | Type |
|------|------------------------------------|----------|------------|-----------|----------|-----------|
| B1 | CS4 - Rectangulaire plein (21; 21) | S 235 | 1,000 | N1 | N2 | beam (80) |

2.4. Nodal supports

| Name | Node | System | Type | X | Y | Z | Rx | Ry | Rz |
|------|------|--------|----------|-------|-------|-------|-------|-------|-------|
| Sn1 | N1 | GCS | Standard | Rigid | Rigid | Rigid | Rigid | Rigid | Rigid |
| Sn2 | N2 | GCS | Standard | Rigid | Rigid | Rigid | Rigid | Rigid | Rigid |

2.5. Materials

Steel EC3

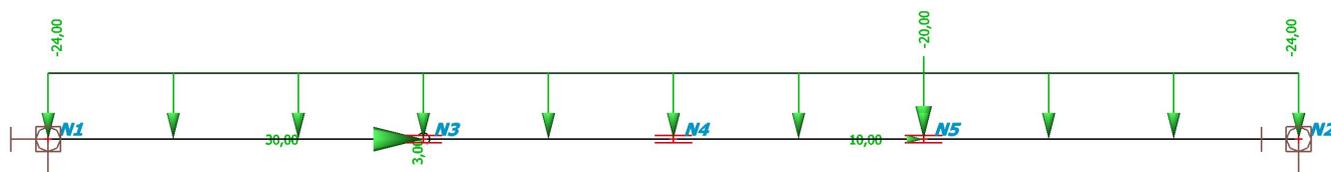
| Name | ρ [kg/m ³] | E_{mod} [MPa] | μ | Limit inférieure [mm] | Limite supérieure [mm] | F_y [MPa] | F_u [MPa] | Colour |
|-------|-----------------------------|-----------------|-----------------|-----------------------|------------------------|-------------|-------------|--------|
| | | G_{mod} [MPa] | α [m/mK] | | | | | |
| S 235 | 7850,00 | 2,1000e+05 | 0.3 | 0 | 40 | 235,0 | 360,0 | ■ |
| | | 8,0769e+04 | 0,01e-003 | 40 | 80 | 215,0 | 360,0 | |

2.6. Cross-sections

| CS4 | | |
|--|------------------------------|------------|
| Type | Rectangulaire plein | |
| Detailed | 21; 21 | |
| Formcode | 7 - Full rectangular section | |
| Item material | S 235 | |
| A [m ²] | 4,5166e-04 | |
| A _y [m ²], A _z [m ²] | 3,7639e-04 | 3,7639e-04 |
| A _L [m ² /m], A _D [m ² /m] | 8,5010e-02 | 8,5010e-02 |
| c _{y,ucs} [mm], c _{z,ucs} [mm] | 11 | 11 |
| α [deg] | 0,00 | |
| I _y [m ⁴], I _z [m ⁴] | 1,7000e-08 | 1,7000e-08 |
| i _y [mm], i _z [mm] | 6 | 6 |
| W _{el,y} [m ³], W _{el,z} [m ³] | 1,5998e-06 | 1,5998e-06 |
| W _{pl,y} [m ³], W _{pl,z} [m ³] | 2,3997e-06 | 2,3997e-06 |
| M _{pl,y,+} [Nm], M _{pl,y,-} [Nm] | 563,94 | 563,94 |
| M _{pl,z,+} [Nm], M _{pl,z,-} [Nm] | 563,94 | 563,94 |
| d _y [mm], d _z [mm] | 0 | |
| I _t [m ⁴], I _w [m ⁶] | 2,8709e-08 | 0,0000e+00 |
| β _y [mm], β _z [mm] | 0 | |
| Picture | | |

3. LOAD

3.1. LC1 / Tot. value



3.2. Point force in node

| Name | Node | Load case | System | Dir | Type | Value - F [kN] |
|------|------|-----------|--------|-----|-------|----------------|
| F1 | N3 | LC1 | GCS | X | Force | 30,00 |
| F2 | N5 | LC1 | GCS | X | Force | 10,00 |
| F3 | N5 | LC1 | GCS | Z | Force | -20,00 |

3.3. Line force

| Name | Member | Type | Dir | Value - P ₁ [kN/m] | Pos x ₁ | Coor | Orig | Ecc ey [m] |
|------|-----------|--------|--------------|-------------------------------|--------------------|--------|------------|------------|
| | Load case | System | Distribution | Value - P ₂ [kN/m] | Pos x ₂ | Loc | | Ecc ez [m] |
| LF1 | B1 | Force | Z | -24,00 | 0.000 | Rela | From start | 0,000 |
| | LC1 | LCS | Uniform | | 1.000 | Length | | 0,000 |

3.4. Moment in node

| Name | Node | Load case | System | Dir | Type | Value - M [kNm] |
|------|------|-----------|--------|-----|--------|-----------------|
| M1 | N3 | LC1 | GCS | My | Moment | 3,00 |

4. RESULTS

4.1. 1D internal forces; V_z

Valeur: V_z

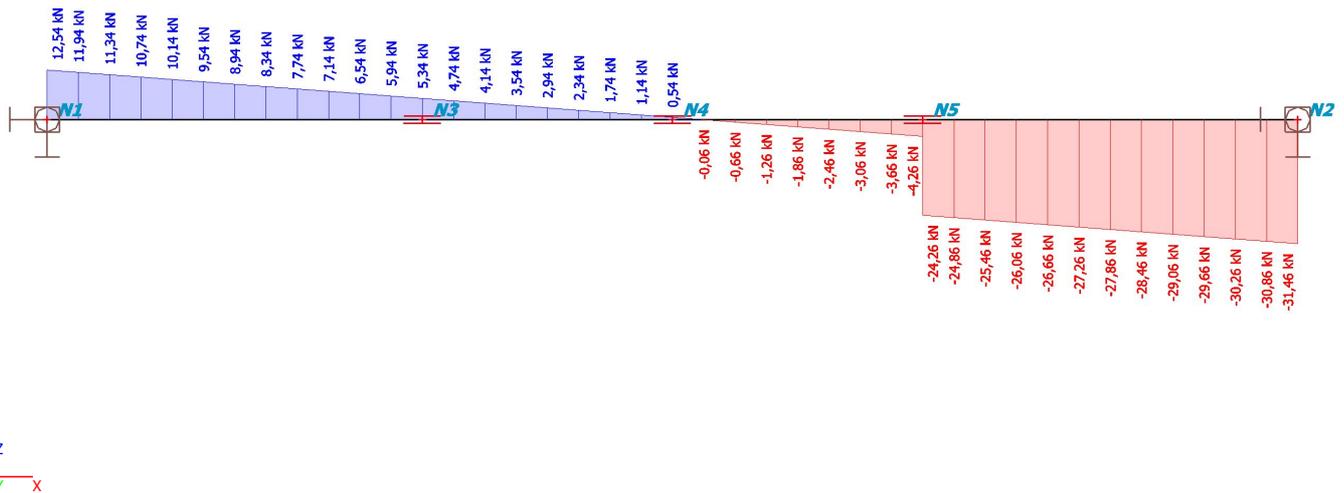
Calcul linéaire

Cas de charge: LC1

Système de coordonnées: Principal

Extrême 1D: Section

Sélection: Tout



4.2. 1D internal forces; M_y

Valeur: M_y

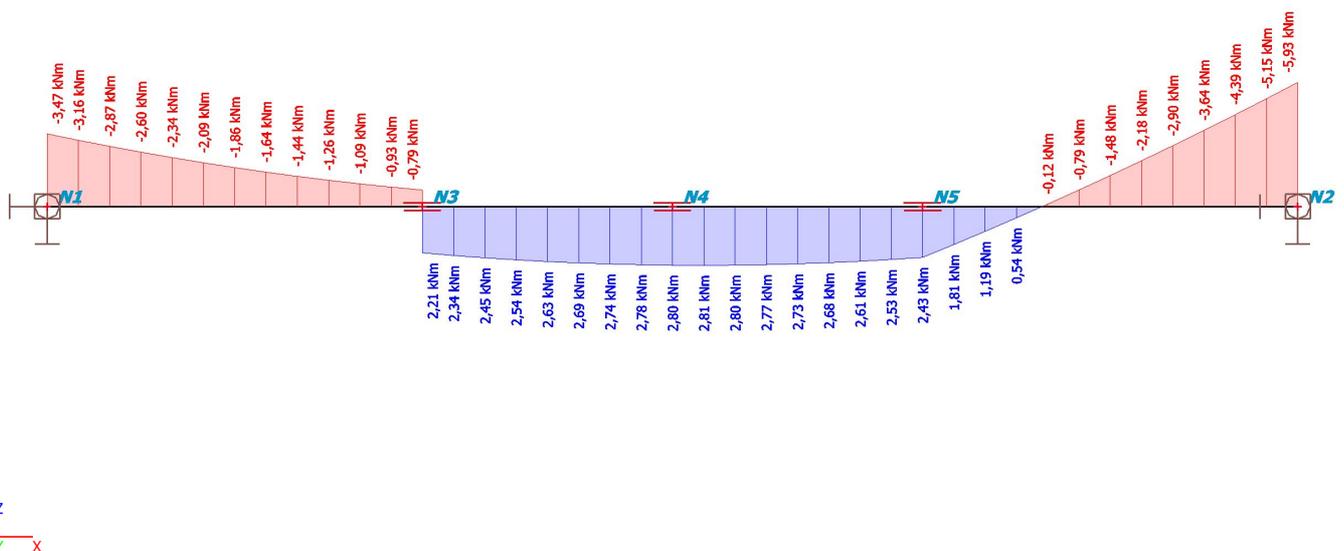
Calcul linéaire

Cas de charge: LC1

Système de coordonnées: Principal

Extrême 1D: Section

Sélection: Tout



4.3. 1D deformations; u_z

Valeur: u_z

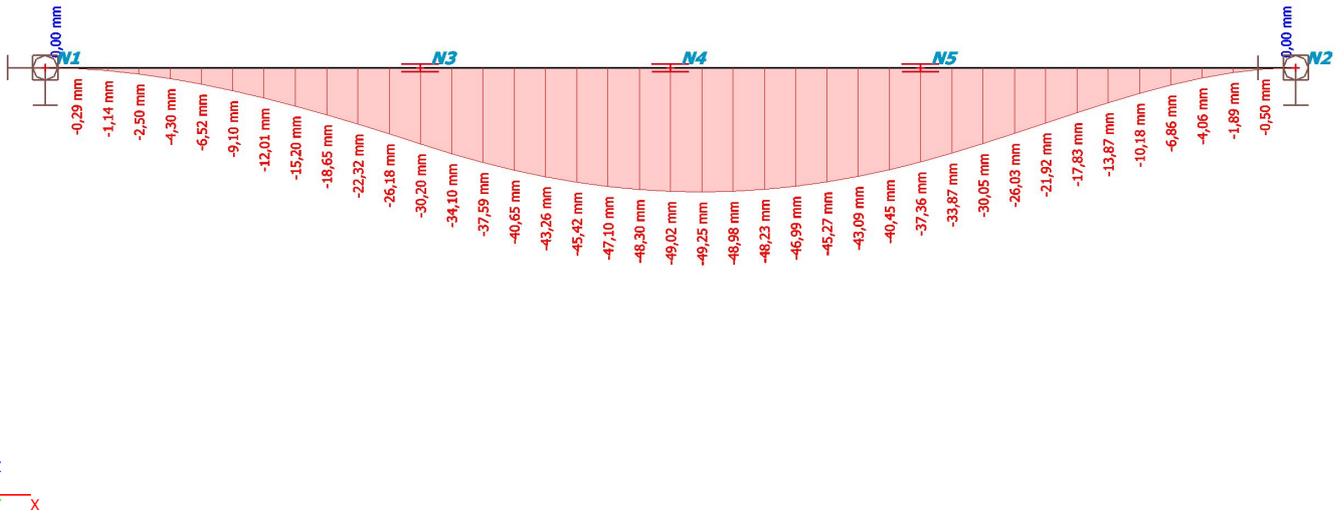
Calcul linéaire

Cas de charge: LC1

Système de coordonnées: Global

Extrême 1D: Section

Sélection: Tout



4.4. Reactions; R_x

Valeur: R_x
Calcul linéaire
Cas de charge: LC1
Système: Global
Extrême: Global
Sélection: Tout



4.5. Reactions

Linear calculation
Load case: LC1
System: Global
Extreme: Global
Selection: All

Nodal reactions

| Name | Case | R _x [kN] | R _y [kN] | R _z [kN] | M _x [kNm] | M _y [kNm] | M _z [kNm] | e _x [mm] | e _y [mm] |
|--------|------|------------------------|------------------------|------------------------|-------------------------|-------------------------|-------------------------|------------------------|------------------------|
| Sn2/N2 | LC1 | -16,00 | 0,00 | 31,46 | 0,00 | 5,93 | 0,00 | -188,49 | 0,00 |
| Sn1/N1 | LC1 | -24,00 | 0,00 | 12,54 | 0,00 | -3,47 | 0,00 | 276,71 | 0,00 |

5. EXPECTED AFNOR RESULTS

Shear Force in node N4 = 0,54 kN

Bending Moment in node N4 = 2,80 kNm

Vertical displacement in node N4 = -49,02 mm

Horizontal reaction in node N1 = -24,00 kN

REFERENCE : "Guide de validation des progiciels de calcul de structures" AFNOR, 1990

1. TESTCASE DESCRIPTION

Influence of shearing stresses (Timoshenko's beam). Length: $L = 1,44$ m, simply supported ends.
 Elastic, linear, isotropic material. Section: $I_z=2810e-8$, $A_x=31e-4$, $A_y=(31E-4/2.42)$, $E=2.1e11$

2. MODEL

2.1. Analysis model



2.2. Nodes

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] | Member | Data |
|------|-------------|-------------|-------------|--------|------|
| N1 | 0,000 | 0,000 | 0,000 | B1 | Sn1 |
| N2 | 1,440 | 0,000 | 0,000 | B1 | Sn2 |
| N3 | 0,720 | 0,000 | 0,000 | B1 | |

2.3. Members

| Name | Cross-section | Material | Length [m] | Beg. node | End node | Type |
|------|-----------------|----------|------------|-----------|----------|-----------|
| B1 | CS2 - Numérique | STEEL | 1,440 | N1 | N2 | beam (80) |

2.4. Nodal supports

| Name | Node | System | Type | X | Y | Z | Rx | Ry | Rz |
|------|------|--------|----------|-------|-------|-------|-------|------|-------|
| Sn1 | N1 | GCS | Standard | Rigid | Rigid | Rigid | Rigid | Free | Rigid |
| Sn2 | N2 | GCS | Standard | Rigid | Rigid | Rigid | Rigid | Free | Rigid |

2.5. Materials

Steel EC3

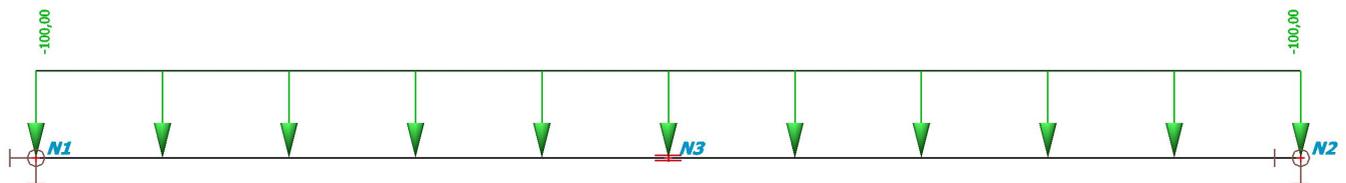
| Name | ρ [kg/m ³] | E_{mod} [MPa] | μ | Limit inférieure [mm] | Limite supérieure [mm] | F_y [MPa] | F_u [MPa] | Colour |
|-------|-----------------------------|-----------------|-----------------|-----------------------|------------------------|-------------|-------------|--------|
| | | G_{mod} [MPa] | α [m/mK] | | | | | |
| STEEL | 7850,00 | 2,0000e+05 | 0.3 | 0 | 40 | 235,0 | 360,0 | ■ |
| | | 7,6923e+04 | 0,01e-003 | 40 | 80 | 215,0 | 360,0 | |

2.6. Cross-sections

| CS2 | | |
|--|------------|------------|
| Detailed | Numerical | |
| A [m ²] | 3,1000e-03 | |
| A _y [m ²], A _z [m ²] | 1,2810e-03 | 1,2810e-03 |
| A _L [m ² /m], A _D [m ² /m] | 0,0000e+00 | 0,0000e+00 |
| c _{y.UCS} [mm], c _{z.UCS} [mm] | 0 | 0 |
| α [deg] | 0,00 | |
| I _y [m ⁴], I _z [m ⁴] | 2,8100e-05 | 2,8100e-05 |
| i _y [mm], i _z [mm] | 95 | 95 |
| W _{el.y} [m ³], W _{el.z} [m ³] | 1,7000e-08 | 1,7000e-08 |
| W _{pl.y} [m ³], W _{pl.z} [m ³] | 1,7000e-08 | 1,7000e-08 |
| M _{pl.y.+} [Nm], M _{pl.y.-} [Nm] | 0,00 | 0,00 |
| M _{pl.z.+} [Nm], M _{pl.z.-} [Nm] | 0,00 | 0,00 |
| d _y [mm], d _z [mm] | 0 | 0 |
| I _E [m ⁴], I _w [m ⁶] | 1,0000e+01 | 0,0000e+00 |
| β _y [mm], β _z [mm] | 0 | 0 |

3. LOAD

3.1. LC1 / Tot. value



3.2. Line force

| Name | Member | Type | Dir | Value - P ₁ [kN/m] | Pos x ₁ | Coor | Orig | Ecc ey [m] |
|------|-----------|--------|--------------|----------------------------------|--------------------|--------|------------|---------------|
| | Load case | System | Distribution | Value - P ₂ [kN/m] | Pos x ₂ | Loc | | Ecc ez [m] |
| LF1 | B1 | Force | Z | -100,00 | 0.000 | Rela | From start | 0,000 |
| | LC1 | LCS | Uniform | | 1.000 | Length | | 0,000 |

4. RESULTS

4.1. 1D deformations; u_z

Valeur: u_z

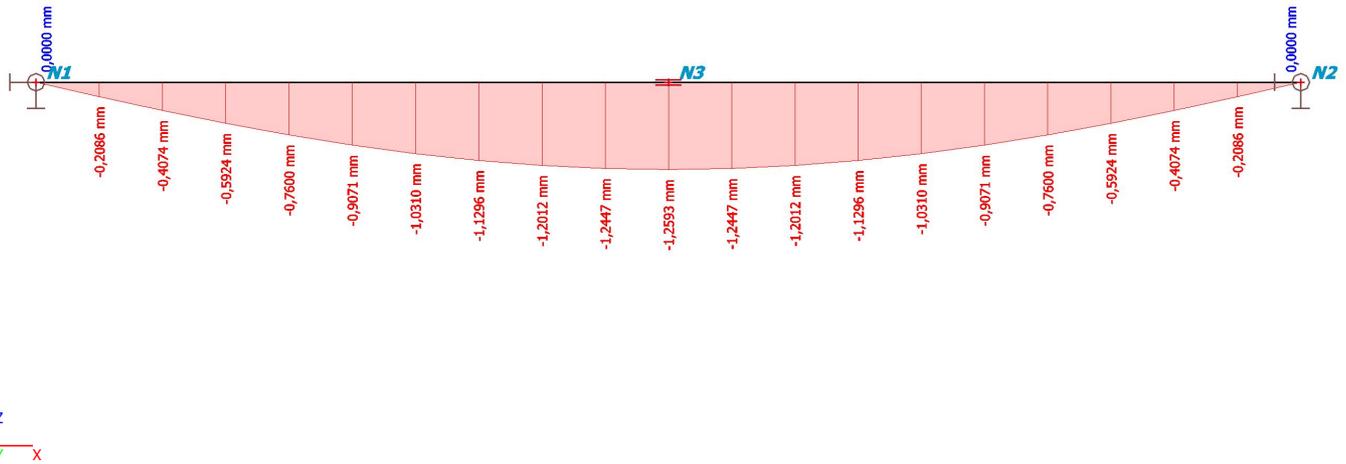
Calcul linéaire

Cas de charge: LC1

Système de coordonnées: Global

Extrême 1D: Section

Sélection: Tout



5. EXPECTED AFNOR RESULTS

Vertical displacement in node N3 = -1,2593 mm

REFERENCE : "Guide de validation des progiciels de calcul de structures" AFNOR, 1990

1. TESTCASE DESCRIPTION

Simple Euler beam under bending with elastic support in the center of length;

Material: elastic, linear, isotropic.

Length: L = 12 m, simply supported at ends and in the middle

Section: $I_z=6.3 \cdot 10^{-4}$, $E=2.1 \cdot 10^{11}$

Stiffness $K_z=2.1 \cdot 10^6$ N/m

2. MODEL

2.1. Analysis model



2.2. Nodes

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] | Member | Data |
|------|-------------|-------------|-------------|--------|------|
| N1 | 0,000 | 0,000 | 0,000 | B1 | Sn1 |
| N2 | 12,000 | 0,000 | 0,000 | B1 | Sn2 |
| N3 | 6,000 | 0,000 | 0,000 | B1 | |

2.3. Members

| Name | Cross-section | Material | Length [m] | Beg. node | End node | Type |
|------|----------------------------|----------|------------|-----------|----------|-----------|
| B1 | CS1 - Rectangle (295; 295) | S 235 | 12,000 | N1 | N2 | beam (80) |

2.4. Nodal supports

| Name | Node | System | Type | X | Y | Z | Rx | Ry | Rz |
|------|------|--------|----------|-------|-------|-------|------|------|------|
| Sn1 | N1 | GCS | Standard | Rigid | Rigid | Rigid | Free | Free | Free |
| Sn2 | N2 | GCS | Standard | Rigid | Rigid | Rigid | Free | Free | Free |

2.5. Materials

Steel EC3

| Name | ρ [kg/m ³] | E_{mod} [MPa] | μ | Limit inférieure [mm] | Limite supérieure [mm] | F_y [MPa] | F_u [MPa] | Colour |
|-------|-----------------------------|-----------------|-----------------|-----------------------|------------------------|-------------|-------------|--------|
| | | G_{mod} [MPa] | α [m/mK] | | | | | |
| S 235 | 7850,00 | 2,1000e+05 | 0.3 | 0 | 40 | 235,0 | 360,0 | ■ |
| | | 8,0769e+04 | 0,01e-003 | 40 | 80 | 215,0 | 360,0 | |

2.6. Cross-sections

| CS1 | | |
|--|------------|------------|
| Type | Rectangle | |
| Detailed | 295; 295 | |
| Item material | S 235 | |
| A [m ²] | 8,6948e-02 | |
| A _y [m ²], A _z [m ²] | 7,2488e-02 | 7,2488e-02 |
| A _L [m ² /m], A _D [m ² /m] | 1,1795e+00 | 1,1795e+00 |
| c _{y,UCS} [mm], c _{z,UCS} [mm] | 147 | 147 |
| α [deg] | 0,00 | |
| I _y [m ⁴], I _z [m ⁴] | 6,3000e-04 | 6,3000e-04 |
| i _y [mm], i _z [mm] | 85 | 85 |
| W _{el,y} [m ³], W _{el,z} [m ³] | 4,2731e-03 | 4,2731e-03 |
| W _{pl,y} [m ³], W _{pl,z} [m ³] | 6,4096e-03 | 6,4096e-03 |
| M _{pl,y,+} [Nm], M _{pl,y,-} [Nm] | 1506258,95 | 1506258,95 |
| M _{pl,z,+} [Nm], M _{pl,z,-} [Nm] | 1506258,95 | 1506258,95 |
| d _y [mm], d _z [mm] | 0 | |
| I _E [m ⁴], I _w [m ⁶] | 1,0632e-03 | 8,8484e-08 |
| β _y [mm], β _z [mm] | 0 | |
| Picture | | |

3. LOAD

3.1. LC2



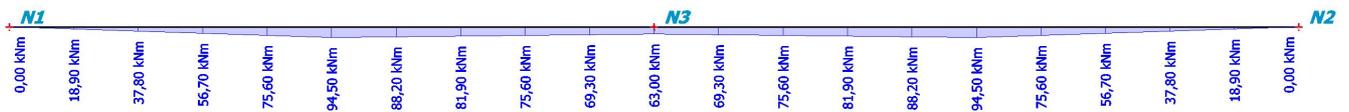
3.2. Point force on beam

| Name | Member | System | Value - F [kN] | Pos x | Coor | Rep (n) |
|------|--------------|--------|-------------------|-------|------------|-----------|
| | Load case | Dir | Type | | Orig | Regularly |
| Fb1 | B1 | GCS | -42,00 | 0.250 | Rela | 1 |
| | LC2 - charge | Z | Force | | From start | |
| Fb2 | B1 | GCS | -42,00 | 0.750 | Rela | 1 |
| | LC2 - charge | Z | Force | | From start | |

4. RESULTS

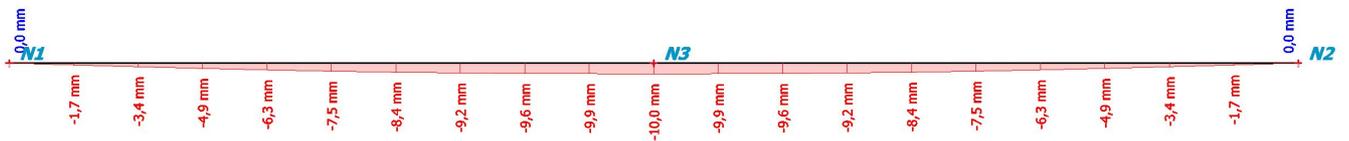
4.1. 1D internal forces; M_y

Valeur: M_y
 Calcul linéaire
 Cas de charge: LC2
 Système de coordonnées: Principal
 Extrême 1D: Section
 Sélection: Tout



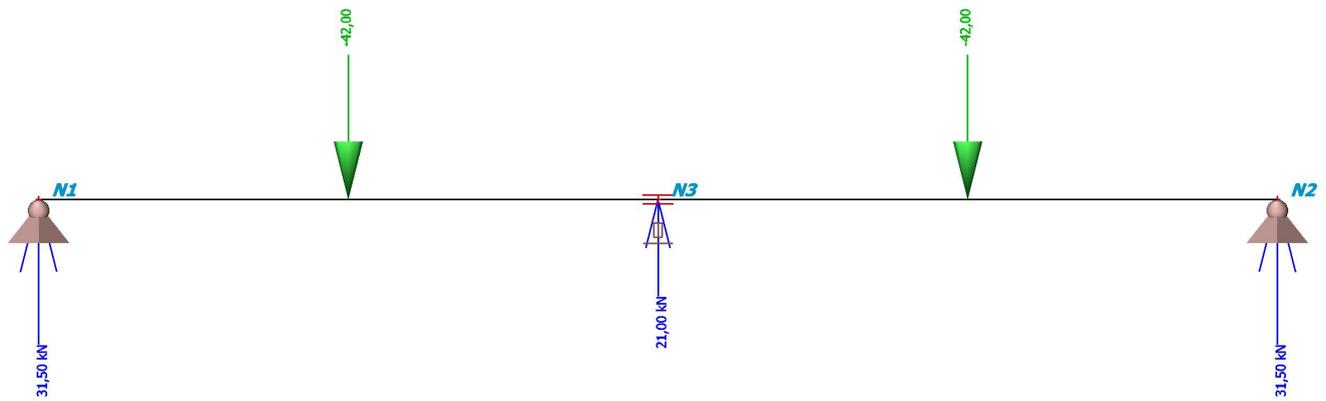
4.2. 1D deformations; u_z

Valeur: u_z
 Calcul linéaire
 Cas de charge: LC2
 Système de coordonnées: Global
 Extrême 1D: Section
 Sélection: Tout



4.3. Reactions; R_z

Valeur: R_z
Calcul linéaire
Cas de charge: LC2
Système: Global
Extrême: Non
Sélection: Tout



5. EXPECTED AFNOR RESULTS

Bending Moment in node N3 = 63,00 kNm

Displacement Uz in node N3 = -10,00 mm

Vertical reaction in node N3 = 21,00 kN

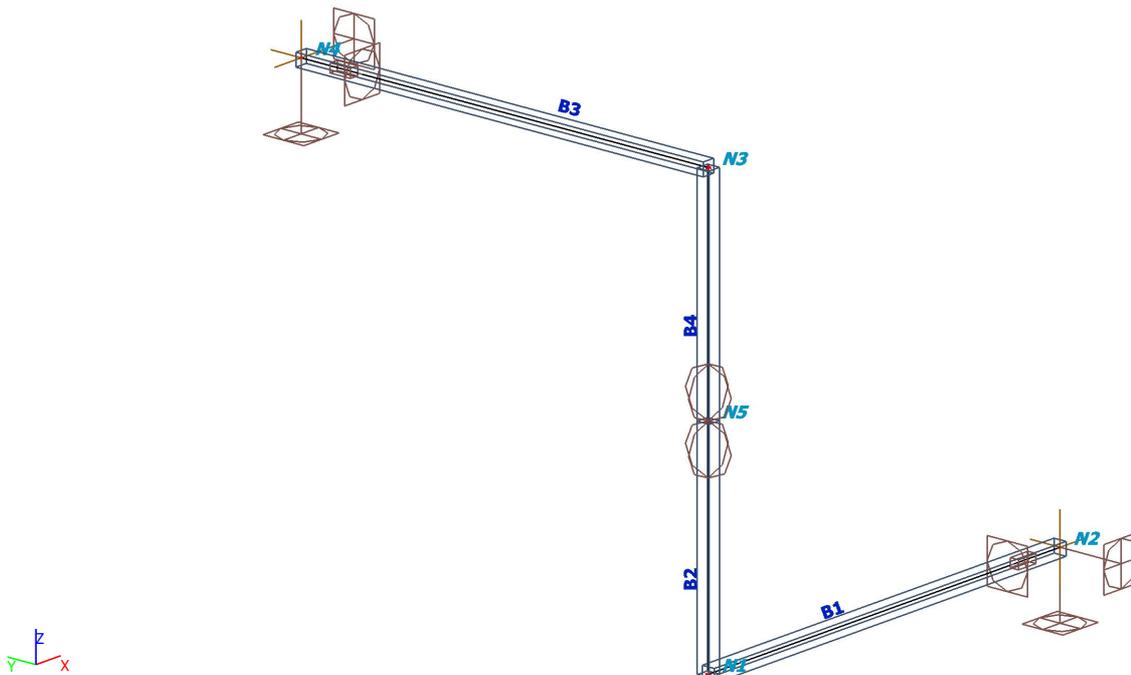
REFERENCE : "Guide de validation des logiciels de calcul de structures" AFNOR, 1990

1. TESTCASE DESCRIPTION

Spatial bar with elastic supports, under bending and torsion; material: elastic, linear, isotropic (non-compressible bars assumed)

2. MODEL

2.1. Analysis model



2.2. Nodes

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] | Member | Data |
|------|-------------|-------------|-------------|----------|------|
| N1 | 0,000 | 0,000 | 0,000 | B1 B2 | |
| N2 | 2,000 | 0,000 | 0,000 | B1 | |
| N3 | 0,000 | 0,000 | 2,000 | B3 B4 | F1 |

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] | Member | Data |
|------|-------------|-------------|-------------|----------|------|
| N4 | 0,000 | 2,000 | 2,000 | B3 | |
| N5 | 0,000 | 0,000 | 1,000 | B2 B4 | |

2.3. Members

| Name | Cross-section | Material | Length [m] | Beg. node | End node | Type |
|------|------------------------------------|----------|------------|-----------|----------|-------------|
| B1 | CS1 - Rectangulaire plein (59; 59) | S 235 | 2,000 | N1 | N2 | general (0) |
| B2 | CS1 - Rectangulaire plein (59; 59) | S 235 | 1,000 | N1 | N5 | general (0) |
| B3 | CS1 - Rectangulaire plein (59; 59) | S 235 | 2,000 | N3 | N4 | general (0) |
| B4 | CS1 - Rectangulaire plein (59; 59) | S 235 | 1,000 | N5 | N3 | general (0) |

2.4. Hinges

| Name | Member | Position | ux | uy | uz | fix | fiy | fiz |
|------|--------|----------|-------|-------|-------|-------|------|------|
| H1 | B4 | Begin | Rigid | Rigid | Rigid | Rigid | Free | Free |
| H2 | B2 | End | Rigid | Rigid | Rigid | Rigid | Free | Free |

2.5. Point supports on member

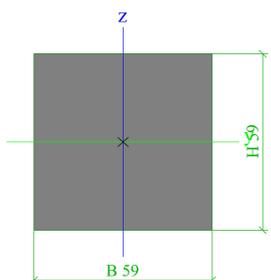
| Name | Type | Coor System | Pos x Orig | dx Rep (n) | X | Y | Z | Rx | Ry | Rz |
|------|----------|-------------|-------------------|------------|----------|-------|-------|-------|----------|----------|
| Sb1 | Standard | Rela LCS | 0.000 From end | 1 | Flexible | Rigid | Rigid | Rigid | Flexible | Flexible |
| Sb2 | Standard | Rela GCS | 0.000 From end | 1 | Flexible | Rigid | Rigid | Rigid | Flexible | Flexible |

2.6. Materials

Steel EC3

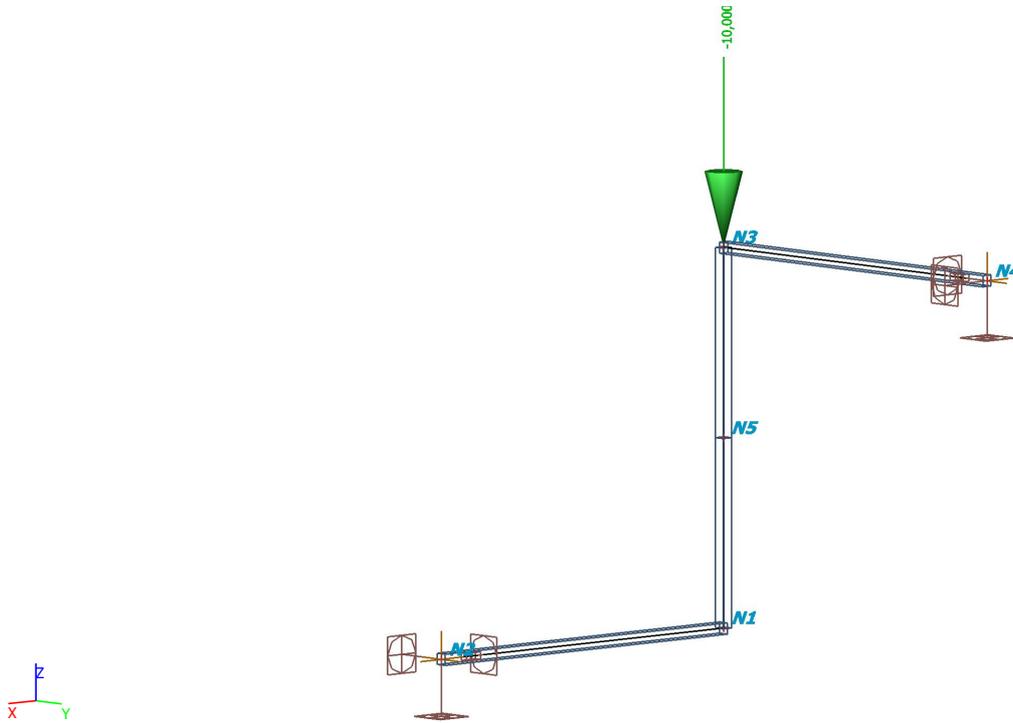
| Name | ρ [kg/m ³] | E_{mod} [MPa] G_{mod} [MPa] | μ α [m/mK] | Limit inférieure [mm] | Limite supérieure [mm] | F_y [MPa] | F_u [MPa] | Colour |
|-------|-----------------------------|------------------------------------|--------------------------|-----------------------|------------------------|----------------|----------------|--------|
| S 235 | 7850,00 | 2,1000e+05 7,8750e+04 | 0.3 0,01e-003 | 0 40 | 40 80 | 235,0 215,0 | 360,0 360,0 | ■ |

2.7. Cross-sections

| CS1 | |
|--|---|
| Type | Rectangulaire plein |
| Detailed | 59; 59 |
| Formcode | 7 - Full rectangular section |
| Item material | S 235 |
| A [m ²] | 1,0000e-03 |
| A_y [m ²], A_z [m ²] | 2,8868e-03 |
| A_L [m ² /m], A_D [m ² /m] | 2,3543e-01 |
| $c_{y,ucs}$ [mm], $c_{z,ucs}$ [mm] | 29 |
| α [deg] | 0,00 |
| I_y [m ⁴], I_z [m ⁴] | 1,0000e-06 |
| i_y [mm], i_z [mm] | 32 |
| $W_{el,y}$ [m ³], $W_{el,z}$ [m ³] | 3,3981e-05 |
| $W_{pl,y}$ [m ³], $W_{pl,z}$ [m ³] | 1,4714e-05 |
| $M_{pl,y,+}$ [Nm], $M_{pl,y,-}$ [Nm] | 3457,83 |
| $M_{pl,z,+}$ [Nm], $M_{pl,z,-}$ [Nm] | 3457,83 |
| d_y [mm], d_z [mm] | 0 |
| I_t [m ⁴], I_w [m ⁶] | 2,0000e-06 |
| β_y [mm], β_z [mm] | 0 |
| Picture |  |

3. LOAD

3.1. LC2 / Valeur totale



3.2. Point force in node

| Name | Node | Load case | System | Dir | Type | Value - F [kN] |
|------|------|-----------------|--------|-----|-------|----------------|
| F1 | N3 | LC2 - Permanent | GCS | Z | Force | -10,000 |

4. RESULTS

4.1. Displacement of nodes

Linear calculation

Load case: LC2

Extreme: Global

Selection: N3, N4

| Name | Case | U _x [mm] | U _y [mm] | U _z [mm] | Φ _x [mrad] | Φ _y [mrad] | Φ _z [mrad] | U _{total} [mm] |
|------|------|------------------------|------------------------|------------------------|--------------------------|--------------------------|--------------------------|----------------------------|
| N4 | LC2 | 0,00 | -29,76 | 0,00 | 160,7 | 0,0 | -59,5 | 29,76 |
| N3 | LC2 | -138,88 | -29,78 | -370,07 | 193,5 | 19,8 | -74,4 | 396,39 |

4.2. 1D internal forces

Linear calculation

Load case: LC2

Coordinate system: Principal

Extreme 1D: Global

Selection: B1, B3

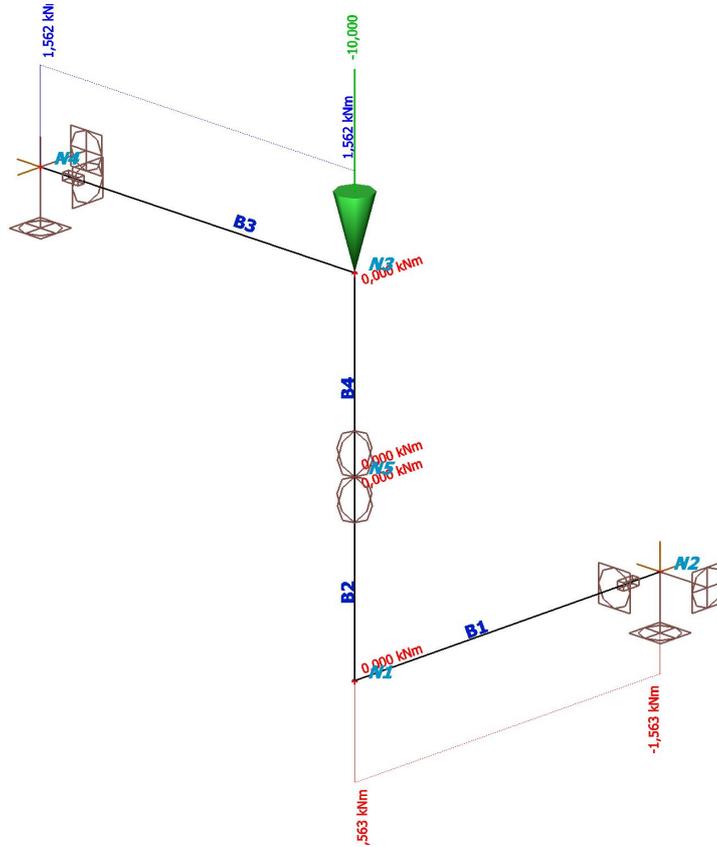
Filter: Cross-section = CS1 - Rectangulaire plein (59; 59)

Selected sections: Inputted

| Name | dx [m] | Case | Cross-section | N [kN] | V _y [kN] | V _z [kN] | M _x [kNm] | M _y [kNm] | M _z [kNm] |
|------|-----------|------|--|---------------|------------------------|------------------------|-------------------------|-------------------------|-------------------------|
| B1 | 2,000 | LC2 | CS1 - Rectangulaire plein (59; 59) | -1,562 | 1,563 | -5,000 | -1,563 | -8,437 | 3,125 |
| B3 | 2,000 | LC2 | CS1 - Rectangulaire plein (59; 59) | 1,563 | 1,562 | -5,000 | 1,562 | -8,438 | 3,125 |

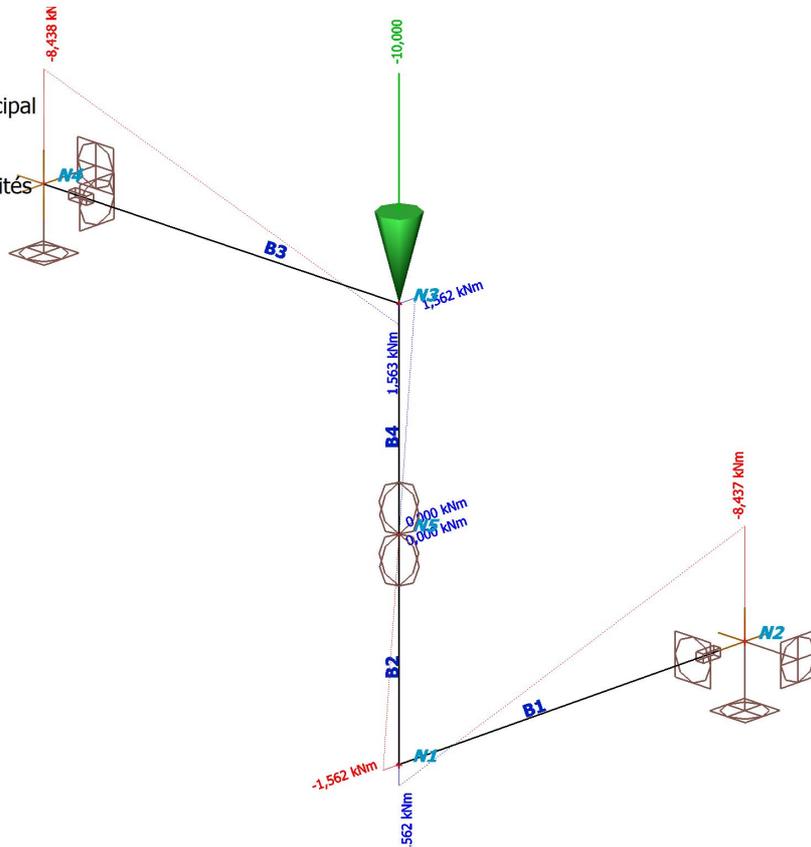
4.3. 1D internal forces; M_x

Valeur: M_x
Calcul linéaire
Cas de charge: LC2
Système de coordonnées: Principal
Extrême 1D: Section
Sélection: Tout
Sections sélectionnées: Extrémités



4.4. 1D internal forces; M_y

Valeur: M_y
Calcul linéaire
Cas de charge: LC2
Système de coordonnées: Principal
Extrême 1D: Section
Sélection: Tout
Sections sélectionnées: Extrémités



4.5. 1D internal forces; M_z

Valeur: M_z

Calcul linéaire

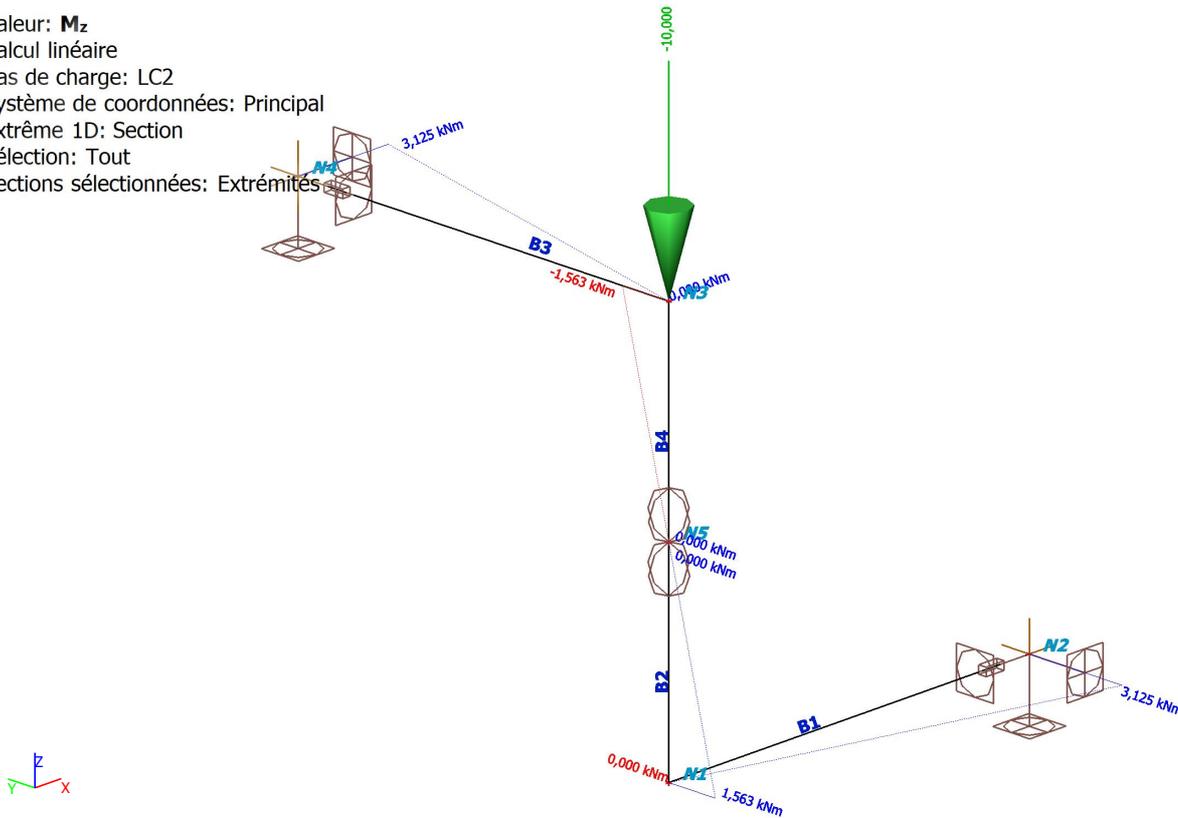
Cas de charge: LC2

Système de coordonnées: Principal

Extrême 1D: Section

Sélection: Tout

Sections sélectionnées: Extrémités



5. EXPECTED AFNOR RESULTS

Moment M_x in node N2 = -1,5625 KN
Moment M_y in node N2 = -8,4375 KN
Moment M_z in node N2 = 3,125 KN
Moment M_x in node N4 = 1,5625 KN
Moment M_y in node N4 = -8,4375 KN
Moment M_z in node N4 = 3,125 KN
Displacement u_y in node N4 = -29,762mm
Rotation R_x in node N4 = 160,71mrad
Displacement u_z in node N3 = -370,04mm

REFERENCE : "Guide de validation des progiciels de calcul de structures" AFNOR, 1990

1. TESTCASE DESCRIPTION

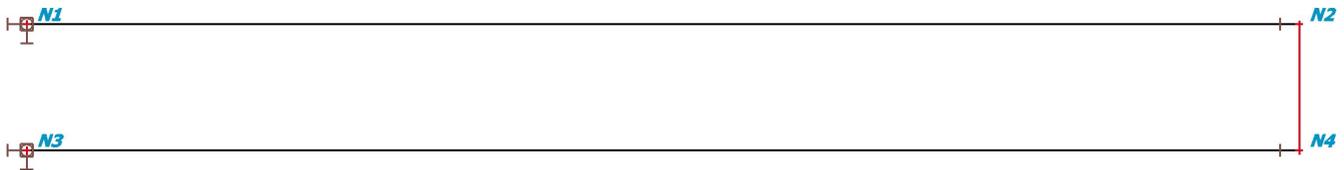
Beams with rigid link – bending of non-compressible bars

GEOMETRY: Length: L = 2 m, distance 0.2 m, Left ends - fixed, right – rigidly linked

Section: $I_z=4/3e-8$, $A_x=1.0$, $E=2e11$

2. MODEL

2.1. Analysis model



2.2. Nodes

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] | Member | Data |
|------|-------------|-------------|-------------|--------|------------------|
| N1 | 0,000 | 0,000 | 0,000 | B1 | Sn1 |
| N2 | 2,000 | 0,000 | 0,000 | B1 | BR1 Sn3 |
| N3 | 0,000 | 0,000 | -0,200 | B2 | Sn2 |
| N4 | 2,000 | 0,000 | -0,200 | B2 | BR1 F1 Sn4 |

2.3. Members

| Name | Cross-section | Material | Length [m] | Beg. node | End node | Type |
|------|--------------------------|----------|------------|-----------|----------|-------------|
| B1 | CS1 - Rectangle (20; 20) | S 235 | 2,000 | N1 | N2 | general (0) |
| B2 | CS1 - Rectangle (20; 20) | S 235 | 2,000 | N3 | N4 | general (0) |

2.4. Nodal supports

| Name | Node | System | Type | X | Y | Z | Rx | Ry | Rz |
|------|------|--------|----------|-------|-------|-------|-------|-------|-------|
| Sn1 | N1 | GCS | Standard | Rigid | Rigid | Rigid | Rigid | Rigid | Rigid |
| Sn2 | N3 | GCS | Standard | Rigid | Rigid | Rigid | Rigid | Rigid | Rigid |
| Sn3 | N2 | GCS | Standard | Rigid | Free | Free | Free | Free | Free |
| Sn4 | N4 | GCS | Standard | Rigid | Free | Free | Free | Free | Free |

2.5. Rigid links

| Name | Master | Slave | Hinge on master | Hinge on slave |
|------|--------|-------|-----------------|----------------|
| BR1 | N2 | N4 | x | x |

2.6. Materials

Steel EC3

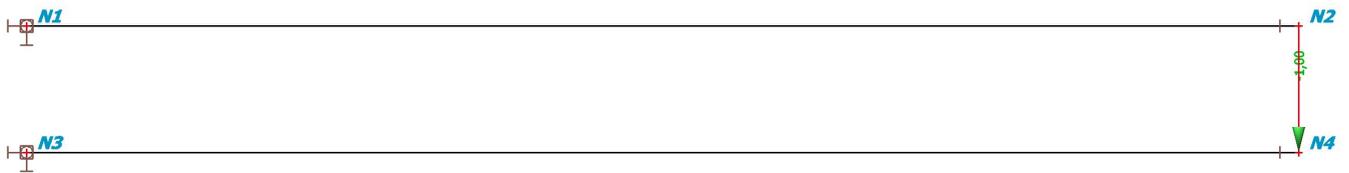
| Name | ρ [kg/m ³] | E_{mod} [MPa] | μ | Limit inférieure [mm] | Limite supérieure [mm] | F_y [MPa] | F_u [MPa] | Colour |
|-------|--------------------------------|--------------------|--------------------|--------------------------|---------------------------|----------------|----------------|--------|
| | | G_{mod} [MPa] | α [m/mK] | | | | | |
| S 235 | 7850,00 | 2,0000e+05 | 0.3 | 0 | 40 | 235,0 | 360,0 | ■ |
| | | 7,6923e+04 | 0,01e-003 | 40 | 80 | 215,0 | 360,0 | |

2.7. Cross-sections

| CS1 | | |
|--|------------|------------|
| Type | Rectangle | |
| Detailed | 20; 20 | |
| Item material | S 235 | |
| A [m ²] | 4,0000e-04 | |
| A _y [m ²], A _z [m ²] | 3,3333e-04 | 3,3333e-04 |
| A _L [m ² /m], A _D [m ² /m] | 8,0000e-02 | 8,0000e-02 |
| c _{y,UCS} [mm], c _{z,UCS} [mm] | 10 | 10 |
| α [deg] | 0,00 | |
| I _y [m ⁴], I _z [m ⁴] | 1,3333e-08 | 1,3333e-08 |
| i _y [mm], i _z [mm] | 6 | 6 |
| W _{el,y} [m ³], W _{el,z} [m ³] | 1,3333e-06 | 1,3333e-06 |
| W _{pl,y} [m ³], W _{pl,z} [m ³] | 2,0000e-06 | 2,0000e-06 |
| M _{pl,y,+} [Nm], M _{pl,y,-} [Nm] | 470,00 | 470,00 |
| M _{pl,z,+} [Nm], M _{pl,z,-} [Nm] | 470,00 | 470,00 |
| d _y [mm], d _z [mm] | 0 | |
| I _E [m ⁴], I _w [m ⁶] | 2,2517e-08 | 0,0000e+00 |
| β _y [mm], β _z [mm] | 0 | |
| Picture | | |

3. LOAD

3.1. LC2



3.2. Point force in node

| Name | Node | Load case | System | Dir | Type | Value - F [kN] |
|------|------|--------------|--------|-----|-------|----------------|
| F1 | N4 | LC2 - Charge | GCS | Z | Force | -1,00 |

4. RESULTS

4.1. 1D internal forces; V_z

Valeur: V_z

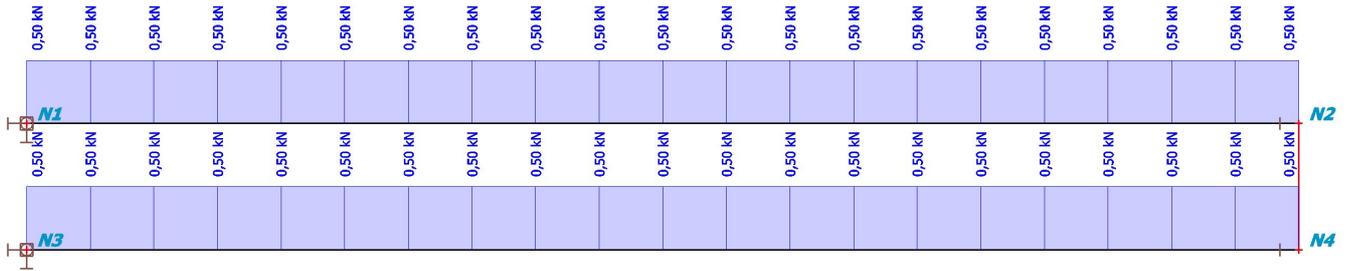
Calcul linéaire

Cas de charge: LC2

Système de coordonnées: Principal

Extrême 1D: Section

Sélection: Tout



4.2. 1D internal forces; M_y

Valeur: M_y

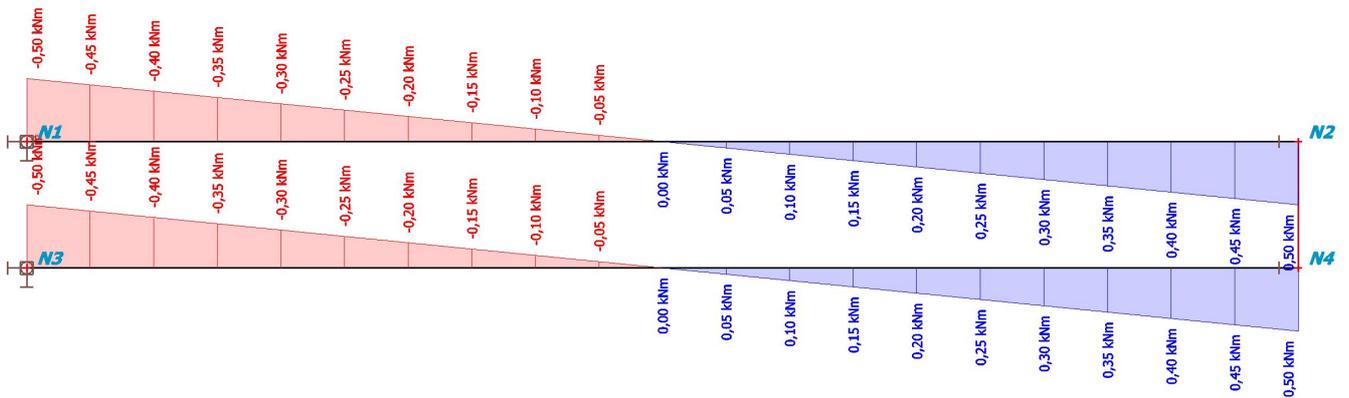
Calcul linéaire

Cas de charge: LC2

Système de coordonnées: Principal

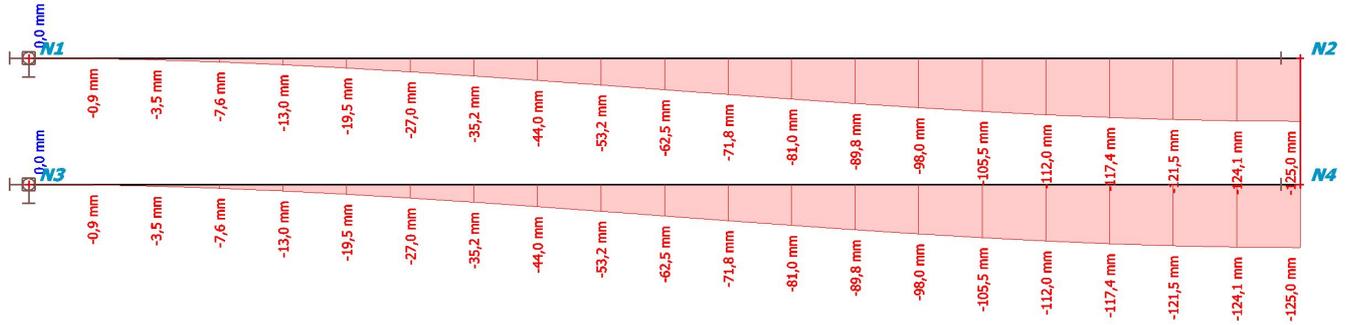
Extrême 1D: Section

Sélection: Tout



4.3. 1D deformations; u_z

Valeur: u_z
 Calcul linéaire
 Cas de charge: LC2
 Système de coordonnées: Global
 Extrême 1D: Section
 Sélection: Tout



5. EXPECTED AFNOR RESULTS

Bending Moment in node N1 & N3 = 0.5 kNm
Displacement Uz in node N2 & N4 = -125 mm
Vertical reaction Vz in node N1 & N3 = 0.5 kN

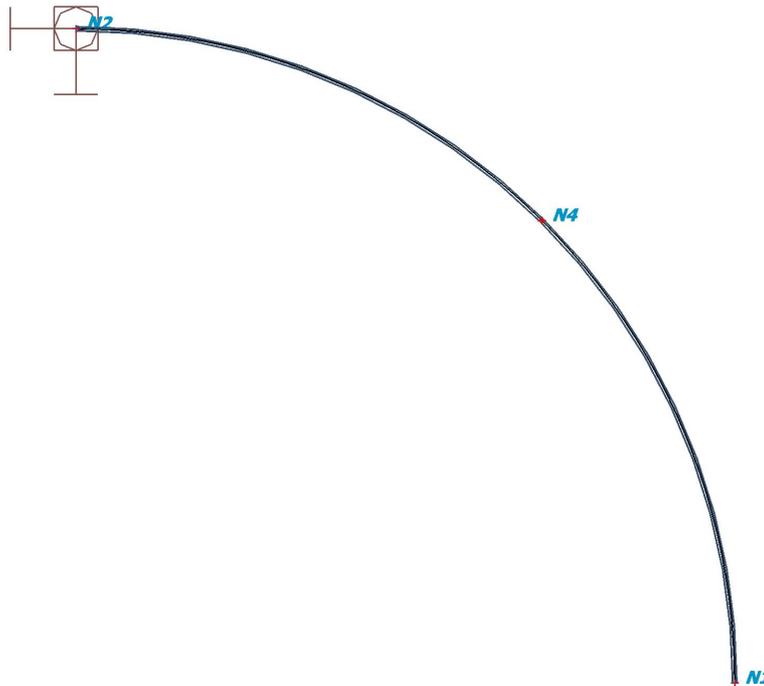
REFERENCE : "Guide de validation des logiciels de calcul de structures" AFNOR, 1990

1. TESTCASE DESCRIPTION

Bending of a quarter circle, fixed at the end, made from hollow round section; elastic linear material, non-compressible bars assumed
 GEOMETRY: Radius of the circle = 3 m, upper end fixed.
 Section: R=10mm, thickness=2mm (Ax=1.0), E=2e11

2. MODEL

2.1. Analysis model



2.2. Nodes

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] | Member | Data |
|------|-------------|-------------|-------------|--------|------|
| N1 | 3,000 | 0,000 | 0,000 | B1 | M1 |
| N2 | 0,000 | 3,000 | 0,000 | B1 | Sn1 |
| N4 | 2,121 | 2,121 | 0,000 | B1 | |

2.3. Members

| Name | Cross-section | Material | Length [m] | Beg. node | End node | Type |
|------|-------------------|----------|------------|-----------|----------|-------------|
| B1 | CS2 - CHS (20; 2) | S 235 | 4,712 | N1 | N2 | general (0) |

2.4. Nodal supports

| Name | Node | System | Type | X | Y | Z | Rx | Ry | Rz |
|------|------|--------|----------|-------|-------|-------|-------|-------|-------|
| Sn1 | N2 | GCS | Standard | Rigid | Rigid | Rigid | Rigid | Rigid | Rigid |

2.5. Materials

Steel EC3

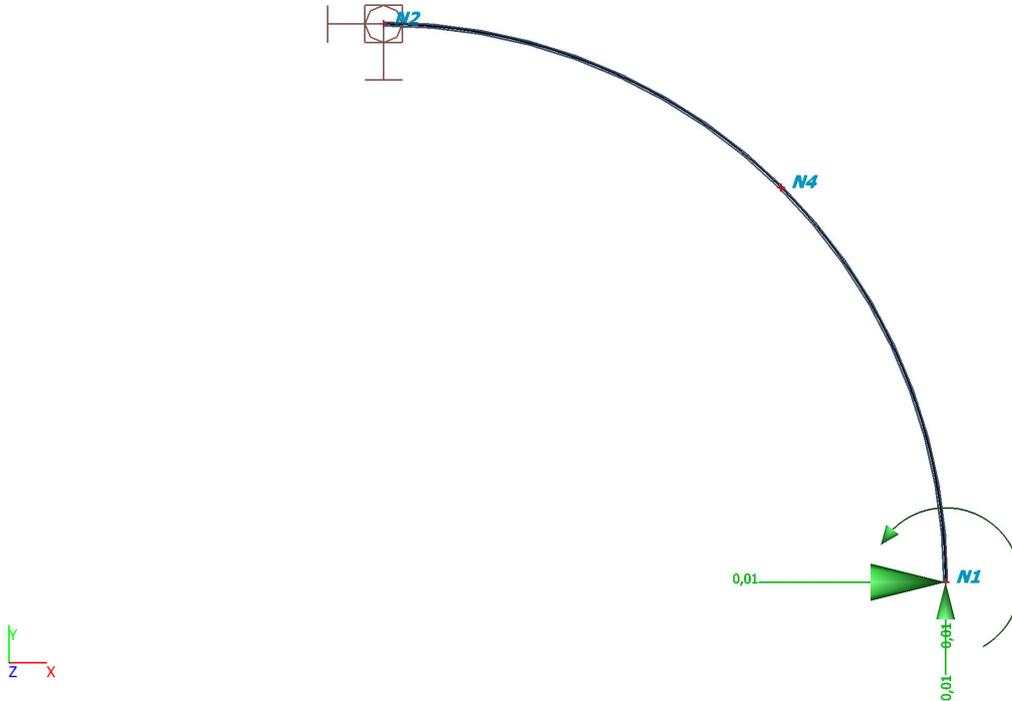
| Name | ρ [kg/m ³] | E_{mod} [MPa] | μ | Limit inférieure [mm] | Limite supérieure [mm] | F_y [MPa] | F_u [MPa] | Colour |
|-------|-----------------------------|-----------------|-----------------|-----------------------|------------------------|-------------|-------------|--------|
| | | G_{mod} [MPa] | α [m/mK] | | | | | |
| S 235 | 7850,00 | 2,0000e+05 | 0.3 | 0 | 40 | 235,0 | 360,0 | ■ |
| | | 7,6923e+04 | 0,01e-003 | 40 | 80 | 215,0 | 360,0 | |

2.6. Cross-sections

| CS2 | | |
|--|-----------------------------|------------|
| Type | CHS | |
| Detailed | 20; 2 | |
| Formcode | 3 - Circular hollow section | |
| Item material | S 235 | |
| A [m ²] | 1,1310e-04 | |
| A _y [m ²], A _z [m ²] | 7,2000e-05 | 7,2000e-05 |
| A _L [m ² /m], A _D [m ² /m] | 6,2829e-02 | 1,1309e-01 |
| c _{y,ucs} [mm], c _{z,ucs} [mm] | 10 | 10 |
| α [deg] | 0,00 | |
| I _y [m ⁴], I _z [m ⁴] | 4,6370e-09 | 4,6370e-09 |
| i _y [mm], i _z [mm] | 6 | 6 |
| W _{el,y} [m ³], W _{el,z} [m ³] | 4,6370e-07 | 4,6370e-07 |
| W _{pl,y} [m ³], W _{pl,z} [m ³] | 6,5067e-07 | 6,5067e-07 |
| M _{pl,y,+} [Nm], M _{pl,y,-} [Nm] | 152,86 | 152,86 |
| M _{pl,z,+} [Nm], M _{pl,z,-} [Nm] | 152,86 | 152,86 |
| d _y [mm], d _z [mm] | 0 | |
| I _t [m ⁴], I _w [m ⁶] | 9,1609e-09 | 1,0996e-45 |
| β _y [mm], β _z [mm] | 0 | |
| Picture | | |

3. LOAD

3.1. LC2 / Valeur totale



3.2. Point force on beam

| Name | Member | System | Value - F [kN] | Pos x | Coor | Rep (n) |
|------|-----------------|--------|----------------|-------|------------|-----------|
| | Load case | Dir | Type | | Orig | Regularly |
| Fb1 | B1 | GCS | 0,01 | 0.000 | Rela | 1 |
| | LC2 - permanent | X | Force | | From start | |
| Fb2 | B1 | GCS | 0,01 | 0.000 | Rela | 1 |
| | LC2 - permanent | Y | Force | | From start | |

3.3. Moment in node

| Name | Node | Load case | System | Dir | Type | Value - M [kNm] |
|------|------|-----------------|--------|-----|--------|-----------------|
| M1 | N1 | LC2 - permanent | GCS | Mz | Moment | 0,01 |

4. RESULTS

4.1. Displacement of nodes

Linear calculation

Load case: LC2

Extreme: Global

Selection: N1

| Name | Case | U _x [mm] | U _y [mm] | U _z [mm] | Φ _x [mrad] | Φ _y [mrad] | Φ _z [mrad] | U _{total} [mm] |
|------|------|------------------------|------------------------|------------------------|--------------------------|--------------------------|--------------------------|----------------------------|
| N1 | LC2 | 379,1 | 241,7 | 0,0 | 0,0 | 0,0 | 165,4 | 449,6 |

5. EXPECTED AFNOR RESULTS

Displacement u_x in node N1 = 379,1mm

Displacement u_y in node N1 = 241,7mm

Rotation R_Z in node N1 = 165,4 mrad

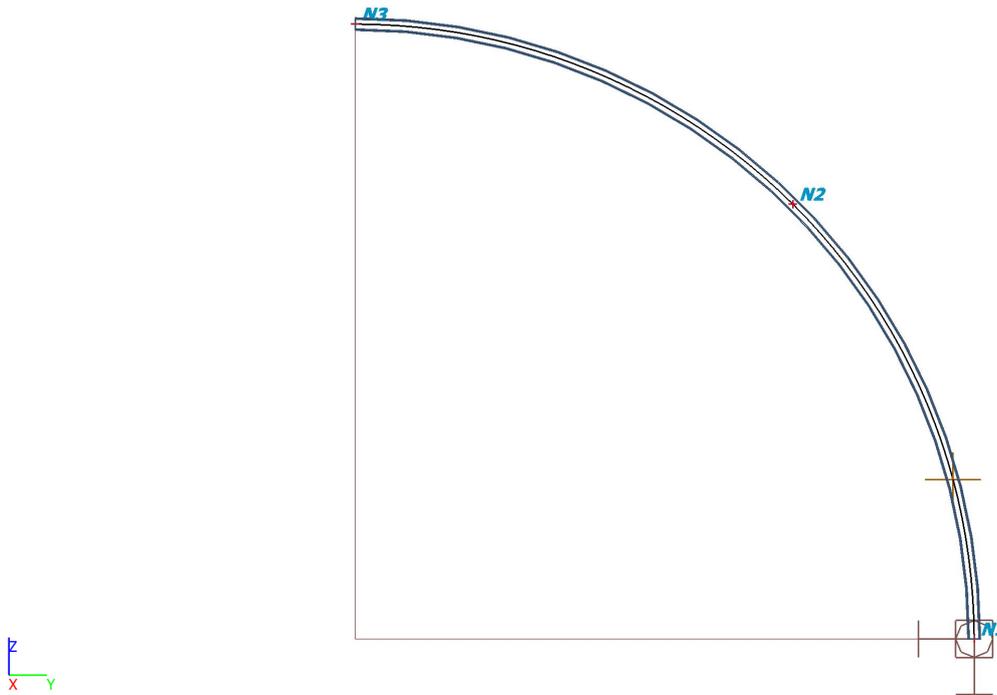
REFERENCE : "Guide de validation des logiciels de calcul de structures" AFNOR, 1990

1. TESTCASE DESCRIPTION

Bending of a quarter circle, fixed at the end, made from hollow round section; elastic linear material, non-compressible bars assumed
 GEOMETRY: Radius of the circle = 3 m, upper end fixed.
 Section: R=10mm, thickness=2mm (Ax=1.0), E=2e11

2. MODEL

2.1. Analysis model



2.2. Nodes

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] | Member | Data |
|------|-------------|-------------|-------------|--------|------|
| N1 | 0,000 | 1,000 | 0,000 | B1 | Sn1 |
| N2 | 0,000 | 0,707 | 0,707 | B1 | |
| N3 | 0,000 | 0,000 | 1,000 | B1 | F1 |

2.3. Members

| Name | Cross-section | Material | Length [m] | Beg. node | End node | Type |
|------|---------------|----------|------------|-----------|----------|-------------|
| B1 | CS1 - RO20X2 | S 235 | 1,571 | N1 | N3 | general (0) |

2.4. Nodal supports

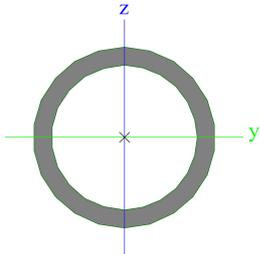
| Name | Node | System | Type | X | Y | Z | Rx | Ry | Rz |
|------|------|--------|----------|-------|-------|-------|-------|-------|-------|
| Sn1 | N1 | GCS | Standard | Rigid | Rigid | Rigid | Rigid | Rigid | Rigid |

2.5. Materials

Steel EC3

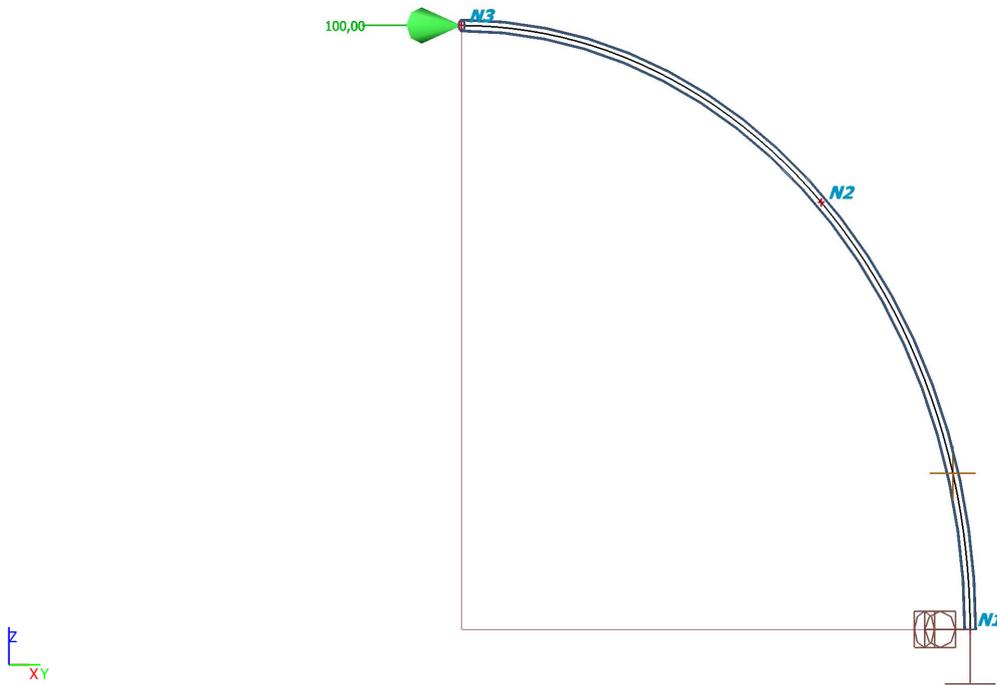
| Name | ρ [kg/m ³] | E_{mod} [MPa] | μ | Limit inférieure [mm] | Limite supérieure [mm] | F_y [MPa] | F_u [MPa] | Colour |
|-------|-----------------------------|-----------------|-----------------|-----------------------|------------------------|-------------|-------------|--------|
| | | G_{mod} [MPa] | α [m/mK] | | | | | |
| S 235 | 7850,00 | 2,0000e+05 | 0.3 | 0 | 40 | 235,0 | 360,0 | ■ |
| | | 7,6923e+04 | 0,01e-003 | 40 | 80 | 215,0 | 360,0 | |

2.6. Cross-sections

| CS1 | | |
|--|--|------------|
| Type | RO20X2 | |
| Formcode | 3 - Circular hollow section | |
| Item material | S 235 | |
| A [m ²] | 1,1300e-04 | |
| A _y [m ²], A _z [m ²] | 7,2000e-05 | 7,2000e-05 |
| A _L [m ² /m], A _D [m ² /m] | 6,2800e-02 | 1,1309e-01 |
| c _{y,UCS} [mm], c _{z,UCS} [mm] | 10 | 10 |
| α [deg] | 0,00 | |
| I _y [m ⁴], I _z [m ⁴] | 4,6400e-09 | 4,6400e-09 |
| i _y [mm], i _z [mm] | 6 | 6 |
| W _{el,y} [m ³], W _{el,z} [m ³] | 4,6400e-07 | 4,6400e-07 |
| W _{pl,y} [m ³], W _{pl,z} [m ³] | 6,4800e-07 | 6,4800e-07 |
| M _{pl,y,+} [Nm], M _{pl,y,-} [Nm] | 152,86 | 152,86 |
| M _{pl,z,+} [Nm], M _{pl,z,-} [Nm] | 152,86 | 152,86 |
| d _y [mm], d _z [mm] | 0 | 0 |
| I _E [m ⁴], I _w [m ⁶] | 9,2800e-09 | 1,0996e-45 |
| β _y [mm], β _z [mm] | 0 | 0 |
| Picture |  | |

3. LOAD

3.1. LC2 / Valeur totale



3.2. Point force in node

| Name | Node | Load case | System | Dir | Type | Value - F [N] |
|------|------|--------------|--------|-----|-------|---------------|
| F1 | N3 | LC2 - Charge | GCS | X | Force | 100,00 |

4. RESULTS

4.1. Displacement of nodes

Linear calculation

Load case: LC2

Extreme: Global

Selection: N3

| Name | Case | U _x [mm] | U _y [mm] | U _z [mm] | Φ _x [mrad] | Φ _y [mrad] | Φ _z [mrad] | U _{total} [mm] |
|------|------|------------------------|------------------------|------------------------|--------------------------|--------------------------|--------------------------|----------------------------|
| N3 | LC2 | 134,56 | 0,00 | 0,00 | 0,0 | 54,6 | 123,9 | 134,56 |

4.2. 1D internal forces

Linear calculation

Load case: LC2

Coordinate system: Principal

Extreme 1D: Global

Selection: All

Filter: Cross-section = CS1 - RO20X2

Selected sections: Inputted

| Name | dx [m] | Case | Cross-section | N [N] | V _y [N] | V _z [N] | M _x [Nm] | M _y [Nm] | M _z [Nm] |
|------|-----------|------|---------------|-------------|-----------------------|-----------------------|------------------------|------------------------|------------------------|
| B1 | 0,262- | LC2 | CS1 - RO20X2 | 0,00 | -100,00 | 0,00 | -74,11 | 0,00 | 96,60 |

5. EXPECTED AFNOR RESULTS

Displacement u_x in node N3 = 134,62mm

Moment M_x for ($\theta=15^\circ$) = 74,11 N.m

Moment M_z for ($\theta=15^\circ$) = 96,59 N.m

REFERENCE : "Guide de validation des logiciels de calcul de structures" AFNOR, 1990

1. TESTCASE DESCRIPTION

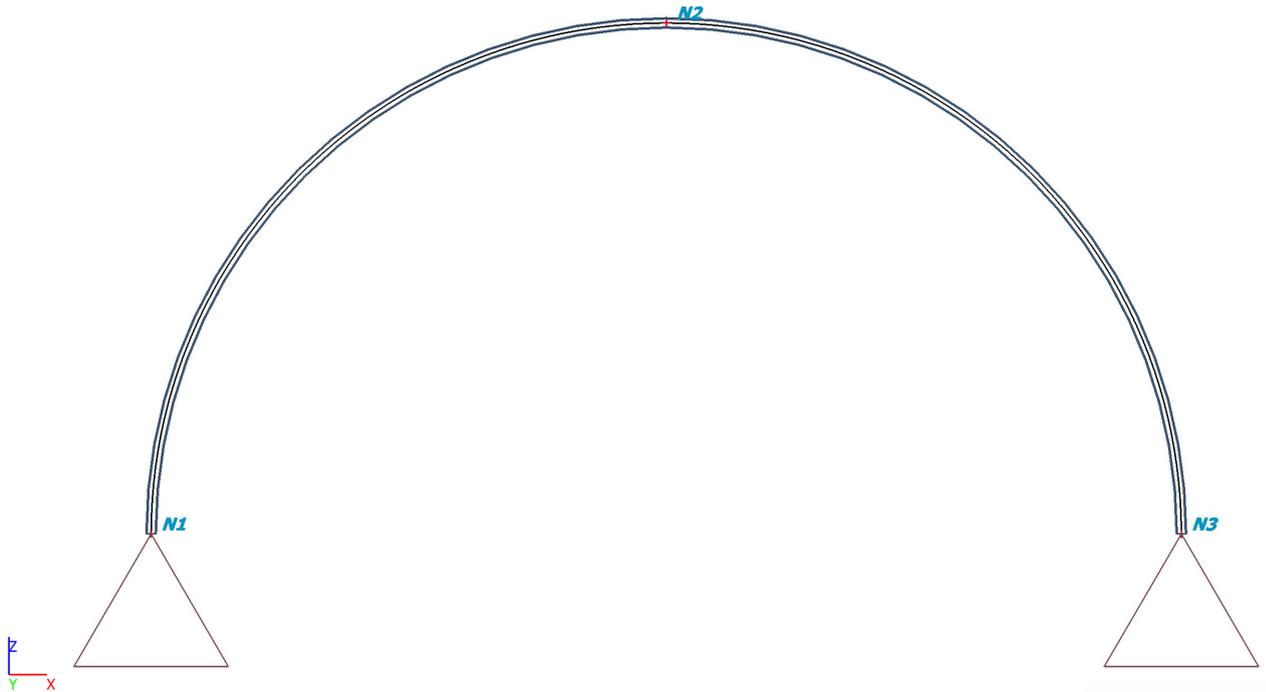
A half circle simply supported at the ends, bending of a thin-walled (hollow) round section; material elastic linear isotropic.

GEOMETRY: Radius of the circle = 3 m, upper end fixed.

Section: R=10mm, thickness=2mm (Ax=1.0), E=2e11

2. MODEL

2.1. Analysis model



2.2. Nodes

| Name | Coord X [m] | Coord Z [m] | Member | Data |
|------|-------------|-------------|--------|------|
| N1 | -1,000 | 0,000 | B1 | Sn1 |
| N2 | 0,000 | 1,000 | B1 | |
| N3 | 1,000 | 0,000 | B1 | Sn2 |

2.3. Members

| Name | Cross-section | Material | Length [m] | Beg. node | End node | Type |
|------|-------------------|----------|------------|-----------|----------|-------------|
| B1 | CS1 - CHS (20; 2) | S 235 | 3,142 | N1 | N3 | general (0) |

2.4. Nodal supports

| Name | Node | System | Type | X | Z | Ry |
|------|------|--------|----------|-------|-------|------|
| Sn1 | N1 | GCS | Standard | Rigid | Rigid | Free |
| Sn2 | N3 | GCS | Standard | Free | Rigid | Free |

2.5. Materials

Steel EC3

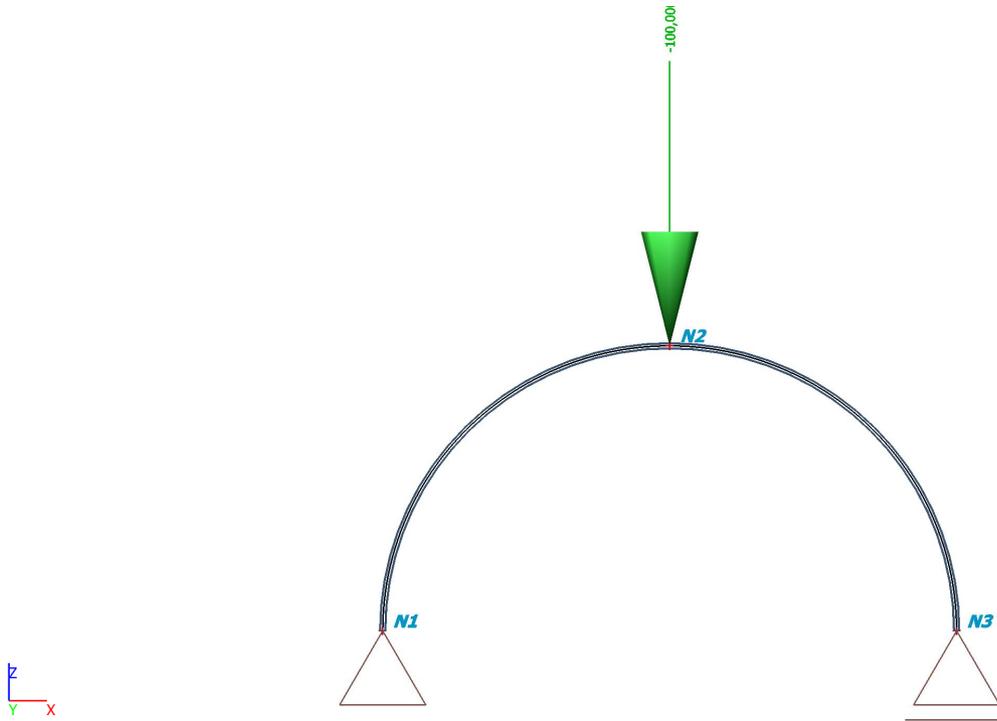
| Name | ρ [kg/m ³] | E_{mod} [MPa] | μ | Limit inférieure [mm] | Limite supérieure [mm] | F_y [MPa] | F_u [MPa] | Colour |
|-------|--------------------------------|--------------------|--------------------|--------------------------|---------------------------|----------------|----------------|--------|
| | | G_{mod} [MPa] | α [m/mK] | | | | | |
| S 235 | 7850,00 | 2,0000e+05 | 0.3 | 0 | 40 | 235,0 | 360,0 | ■ |
| | | 7,6923e+04 | 0,01e-003 | 40 | 80 | 215,0 | 360,0 | |

2.6. Cross-sections

| CS1 | | |
|--|-----------------------------|------------|
| Type | CHS | |
| Detailed | 20; 2 | |
| Formcode | 3 - Circular hollow section | |
| Item material | S 235 | |
| A [m ²] | 1,1310e-04 | |
| A _y [m ²], A _z [m ²] | 7,2000e-05 | 7,2000e-05 |
| A _L [m ² /m], A _D [m ² /m] | 6,2829e-02 | 1,1309e-01 |
| c _{y,ucs} [mm], c _{z,ucs} [mm] | 10 | 10 |
| α [deg] | 0,00 | |
| I _y [m ⁴], I _z [m ⁴] | 4,6370e-09 | 4,6370e-09 |
| i _y [mm], i _z [mm] | 6 | 6 |
| W _{el,y} [m ³], W _{el,z} [m ³] | 4,6370e-07 | 4,6370e-07 |
| W _{pl,y} [m ³], W _{pl,z} [m ³] | 6,5067e-07 | 6,5067e-07 |
| M _{pl,y,+} [Nm], M _{pl,y,-} [Nm] | 152,86 | 152,86 |
| M _{pl,z,+} [Nm], M _{pl,z,-} [Nm] | 152,86 | 152,86 |
| d _y [mm], d _z [mm] | 0 | 0 |
| I _t [m ⁴], I _w [m ⁶] | 9,1609e-09 | 1,0996e-45 |
| β_y [mm], β_z [mm] | 0 | 0 |
| Picture | | |

3. LOAD

3.1. LC2 / Valeur totale



3.2. Point force on beam

| Name | Member | System | Value - F [N] | Pos x | Coor | Rep (n) |
|------|-----------------|--------|---------------|-------|------------|-----------|
| | Load case | Dir | Type | | Orig | Regularly |
| Fb1 | B1 | GCS | -100,0000 | 0.500 | Rela | 1 |
| | LC2 - Permanent | Z | Force | | From start | |

4. RESULTS

4.1. Displacement of nodes

Linear calculation

Load case: LC2

Extreme: Global

Selection: All

| Name | Case | U _x [mm] | U _z [mm] | Φ _y [mrad] | U _{total} [mm] |
|------|------|------------------------|------------------------|--------------------------|----------------------------|
| N1 | LC2 | 0,000 | 0,000 | 30,774 | 0,000 |
| N2 | LC2 | 26,960 | -19,213 | 0,000 | 33,106 |
| N3 | LC2 | 53,921 | 0,000 | -30,774 | 53,921 |

5. EXPECTED AFNOR RESULTS

Displacement u_x in node N3 = 53,912mm

Displacement u_z in node N2 = -19,206mm

Rotation φ_y in node N1= -30,774mrad

Rotation φ_y in node N3= 30,774mrad

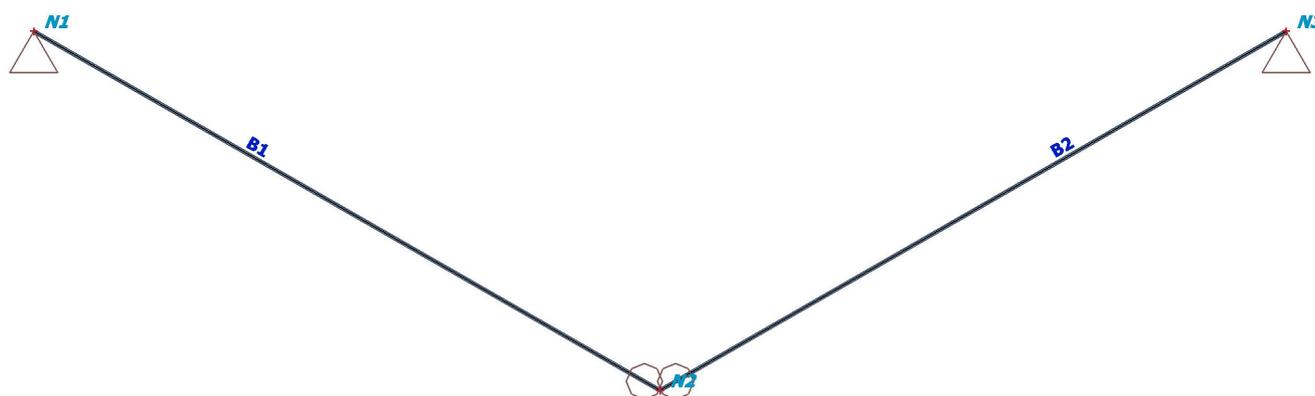
REFERENCE : "Guide de validation des progiciels de calcul de structures" AFNOR, 1990

1. TESTCASE DESCRIPTION

Truss made of two bars; material: elastic, linear, isotropic.

2. MODEL

2.1. Analysis model



2.2. Nodes

| Name | Coord X [m] | Coord Z [m] | Member | Data |
|------|-------------|-------------|----------|------|
| N1 | 0,000 | 0,000 | B1 | Sn1 |
| N2 | 3,897 | -2,250 | B1 B2 | F1 |
| N3 | 7,794 | 0,000 | B2 | Sn2 |

2.3. Members

| Name | Cross-section | Material | Length [m] | Beg. node | End node | Type |
|------|-------------------|----------|------------|-----------|----------|-------------|
| B1 | CS3 - Cercle (20) | S 235 | 4,500 | N1 | N2 | general (0) |
| B2 | CS3 - Cercle (20) | S 235 | 4,500 | N3 | N2 | general (0) |

2.4. Hinges

| Name | Member | Position | ux | uy | uz | fix | fiy | fiz |
|------|--------|----------|-------|----|-------|-----|------|-----|
| H1 | B1 | End | Rigid | | Rigid | | Free | |
| H2 | B2 | End | Rigid | | Rigid | | Free | |

2.5. Nodal supports

| Name | Node | System | Type | X | Z | Ry |
|------|------|--------|----------|-------|-------|------|
| Sn1 | N1 | GCS | Standard | Rigid | Rigid | Free |
| Sn2 | N3 | GCS | Standard | Rigid | Rigid | Free |

2.6. Materials

Steel EC3

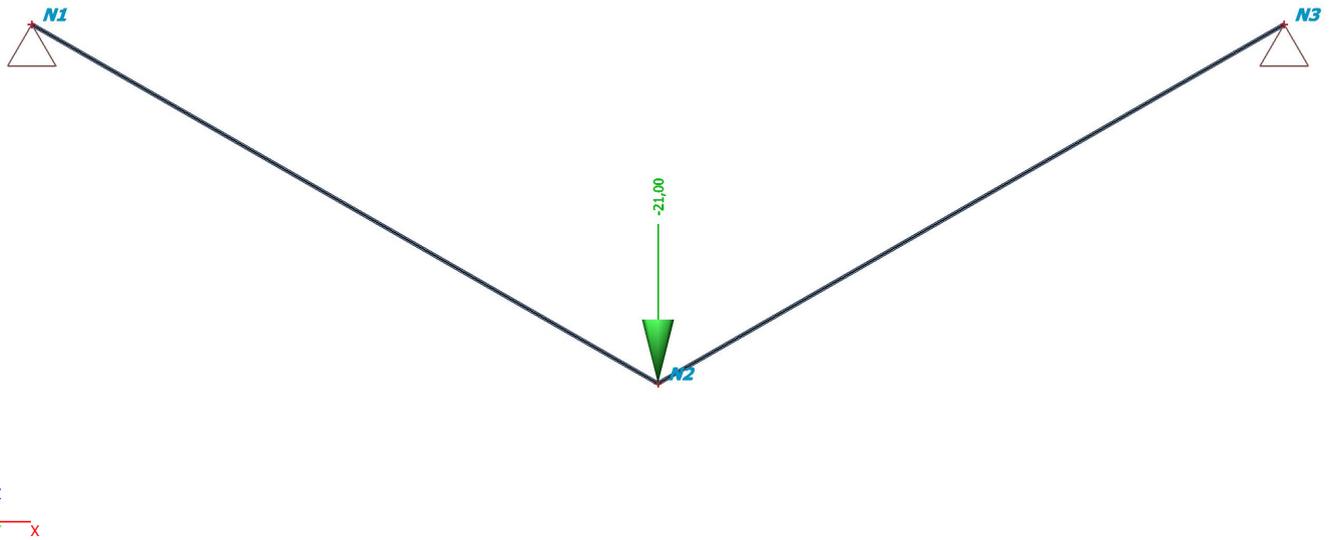
| Name | ρ [kg/m ³] | E_{mod} [MPa] | μ | Limite inférieure [mm] | Limite supérieure [mm] | F_y [MPa] | F_u [MPa] | Colour |
|-------|--------------------------------|--------------------|--------------------|---------------------------|---------------------------|----------------|----------------|--------|
| | | G_{mod} [MPa] | α [m/mK] | | | | | |
| S 235 | 7850,00 | 2,1000e+05 | 0.3 | 0 | 40 | 235,0 | 360,0 | ■ |
| | | 8,0769e+04 | 0,01e-003 | 40 | 80 | 215,0 | 360,0 | |

2.7. Cross-sections

| CS3 | | |
|--|------------|------------|
| Type | Cercle | |
| Detailed | 20 | |
| Item material | S 235 | |
| A [m ²] | 3,0000e-04 | |
| A _y [m ²], A _z [m ²] | 2,7000e-04 | 2,7000e-04 |
| A _L [m ² /m], A _D [m ² /m] | 6,1396e-02 | 6,1396e-02 |
| c _{y,UCS} [mm], c _{z,UCS} [mm] | 10 | 10 |
| α [deg] | 0,00 | |
| I _y [m ⁴], I _z [m ⁴] | 7,1620e-09 | 7,1620e-09 |
| i _y [mm], i _z [mm] | 5 | 5 |
| W _{el,y} [m ³], W _{el,z} [m ³] | 7,3290e-07 | 7,3290e-07 |
| W _{pl,y} [m ³], W _{pl,z} [m ³] | 1,2442e-06 | 1,2442e-06 |
| M _{pl,y,+} [Nm], M _{pl,y,-} [Nm] | 292,30 | 292,30 |
| M _{pl,z,+} [Nm], M _{pl,z,-} [Nm] | 292,30 | 292,30 |
| d _y [mm], d _z [mm] | 0 | |
| I _t [m ⁴], I _w [m ⁶] | 1,4324e-08 | 0,0000e+00 |
| β_y [mm], β_z [mm] | 0 | |
| Picture | | |

3. LOAD

3.1. LC2 / Valeur totale



3.2. Point force in node

| Name | Node | Load case | System | Dir | Type | Value - F [kN] |
|------|------|-----------------|--------|-----|-------|----------------|
| F1 | N2 | LC2 - Permanent | GCS | Z | Force | -21,00 |

4. RESULTS

4.1. Displacement of nodes

Linear calculation
Load case: LC2
Extreme: Global
Selection: All

| Name | Case | U _z [mm] |
|------|------|------------------------|
| N2 | LC2 | -3,0 |
| N1 | LC2 | 0,0 |

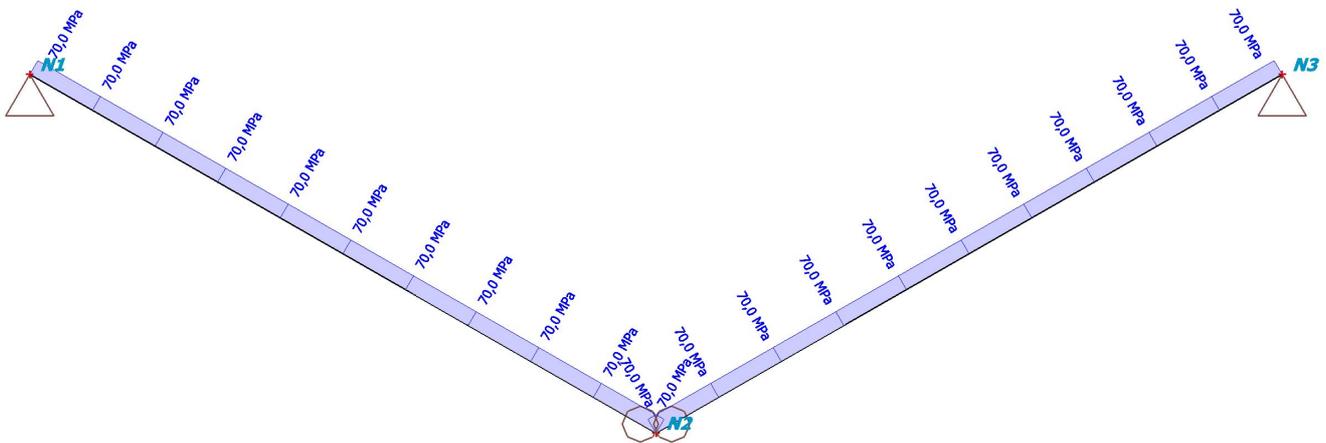
4.2. 1D stresses

Linear calculation
Load case: LC2
Coordinate system: Principal
Extreme 1D: Member
Selection: B1, B2

| Name | dx [m] | Fibre | Case | σ _x [MPa] |
|------|-----------|-------|------|-------------------------|
| B1 | 0,000 | 1 | LC2 | 70,0 |
| B2 | 0,000 | 1 | LC2 | 70,0 |

4.3. 1D stresses; σ_x

Valeur: σ_x
Calcul linéaire
Cas de charge: LC2
Système de coordonnées: Principal
Extrême 1D: Section
Sélection: Tout



5. EXPECTED AFNOR RESULTS

Displacement uz in node N2 = -3mm

Stress σ_x in the element B1 = 70 Mpa

Stress σ_x in the element B2 = 70 Mpa

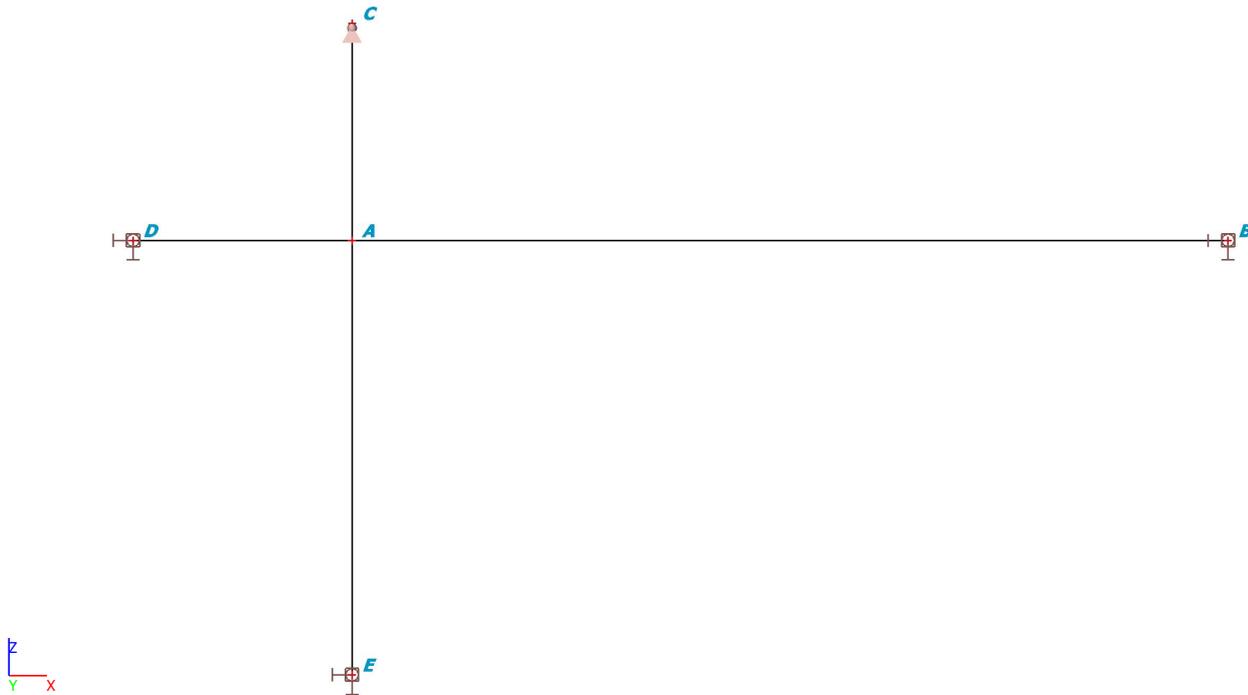
REFERENCE : "Guide de validation des logiciels de calcul de structures" AFNOR, 1990

1. TESTCASE DESCRIPTION

Frame made of four bars with different moments of inertia; material: elastic, linear, isotropic

2. MODEL

2.1. Analysis model



2.2. Nodes

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] | Member | Data |
|------|-------------|-------------|-------------|--------|------|
| D | 0,000 | 0,000 | 0,000 | B1 | Sn2 |
| A | 1,000 | 0,000 | 0,000 | B1 | |
| | | | | B2 | |
| | | | | B3 | |
| | | | | B5 | |
| B | 5,000 | 0,000 | 0,000 | B2 | Sn3 |

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] | Member | Data |
|------|-------------|-------------|-------------|--------|------|
| C | 1,000 | 0,000 | 1,000 | B3 | Sn4 |
| E | 1,000 | 0,000 | -2,000 | B5 | Sn1 |

2.3. Members

| Name | Cross-section | Material | Length [m] | Beg. node | End node | Type |
|------|---------------------------------------|----------|------------|-----------|----------|-------------|
| B1 | Section AC et AD - Rectangle (10; 10) | S 235 | 1,000 | D | A | general (0) |
| B2 | Section AB - Rectangle (40; 40) | S 235 | 4,000 | A | B | general (0) |
| B3 | Section AC et AD - Rectangle (10; 10) | S 235 | 1,000 | A | C | general (0) |
| B5 | Section AE - Rectangle (20; 20) | S 235 | 2,000 | A | E | general (0) |

2.4. Nodal supports

| Name | Node | System | Type | X | Y | Z | Rx | Ry | Rz |
|------|------|--------|----------|-------|-------|-------|-------|-------|-------|
| Sn1 | E | GCS | Standard | Rigid | Rigid | Rigid | Rigid | Rigid | Rigid |
| Sn2 | D | GCS | Standard | Rigid | Rigid | Rigid | Rigid | Rigid | Rigid |
| Sn3 | B | GCS | Standard | Rigid | Rigid | Rigid | Rigid | Rigid | Rigid |
| Sn4 | C | GCS | Standard | Rigid | Rigid | Rigid | Free | Free | Free |

2.5. Materials

| |
|-------------|
| Empty table |
|-------------|

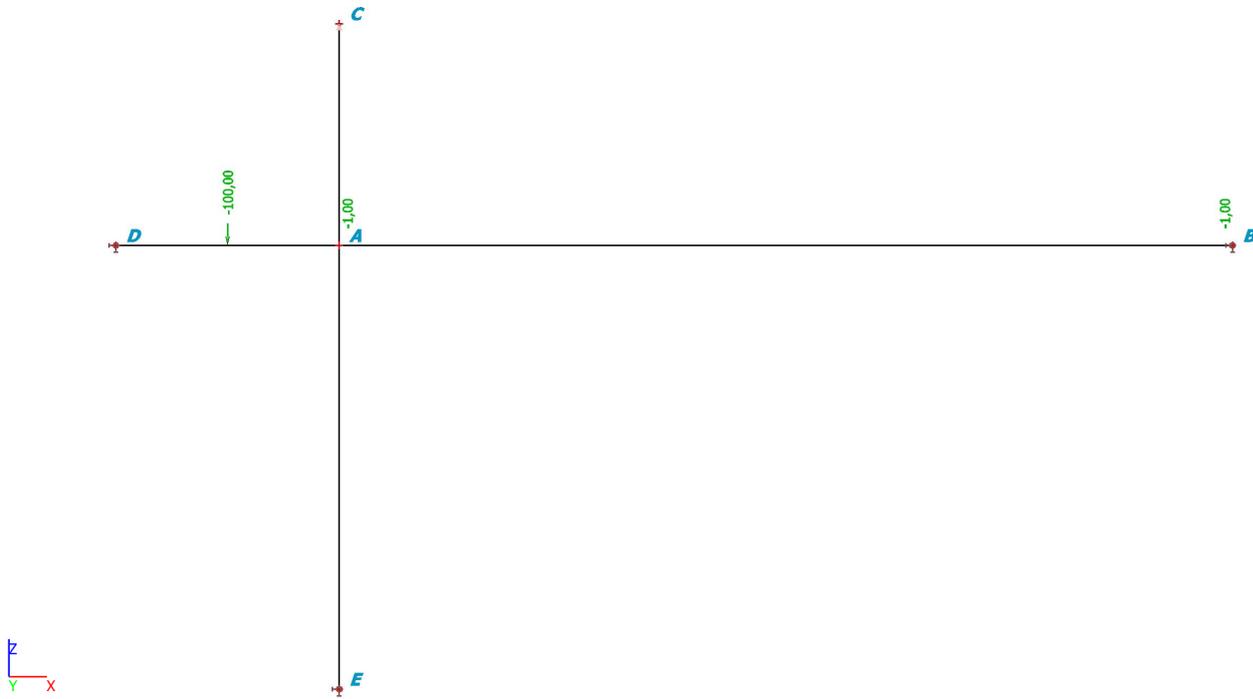
2.6. Cross-sections

| Section AB | | |
|--|------------|------------|
| Type | Rectangle | |
| Detailed | 40; 40 | |
| Item material | S 235 | |
| A [m ²] | 1,6000e-03 | |
| A _y [m ²], A _z [m ²] | 1,3333e-03 | 1,3333e-03 |
| A _L [m ² /m], A _D [m ² /m] | 1,6000e-01 | 1,6000e-01 |
| c _{y,UCS} [mm], c _{z,UCS} [mm] | 20 | 20 |
| α [deg] | 0,00 | |
| I _y [m ⁴], I _z [m ⁴] | 2,1333e-07 | 2,1333e-07 |
| i _y [mm], i _z [mm] | 12 | 12 |
| W _{el,y} [m ³], W _{el,z} [m ³] | 1,0667e-05 | 1,0667e-05 |
| W _{pl,y} [m ³], W _{pl,z} [m ³] | 1,6000e-05 | 1,6000e-05 |
| M _{pl,y,+} [Nm], M _{pl,y,-} [Nm] | 3760,00 | 3760,00 |
| M _{pl,z,+} [Nm], M _{pl,z,-} [Nm] | 3760,00 | 3760,00 |
| d _y [mm], d _z [mm] | 0 | |
| I _t [m ⁴], I _w [m ⁶] | 3,6027e-07 | 0,0000e+00 |
| β _y [mm], β _z [mm] | 0 | |
| Picture | | |
| Section AC et AD | | |
| Type | Rectangle | |
| Detailed | 10; 10 | |
| Item material | S 235 | |
| A [m ²] | 1,0000e-04 | |
| A _y [m ²], A _z [m ²] | 8,3333e-05 | 8,3333e-05 |
| A _L [m ² /m], A _D [m ² /m] | 4,0000e-02 | 4,0000e-02 |
| c _{y,UCS} [mm], c _{z,UCS} [mm] | 5 | 5 |
| α [deg] | 0,00 | |
| I _y [m ⁴], I _z [m ⁴] | 8,3333e-10 | 8,3333e-10 |
| i _y [mm], i _z [mm] | 3 | 3 |
| W _{el,y} [m ³], W _{el,z} [m ³] | 1,6667e-07 | 1,6667e-07 |
| W _{pl,y} [m ³], W _{pl,z} [m ³] | 2,5000e-07 | 2,5000e-07 |
| M _{pl,y,+} [Nm], M _{pl,y,-} [Nm] | 58,75 | 58,75 |
| M _{pl,z,+} [Nm], M _{pl,z,-} [Nm] | 58,75 | 58,75 |
| d _y [mm], d _z [mm] | 0 | |
| I _t [m ⁴], I _w [m ⁶] | 1,4073e-09 | 0,0000e+00 |
| β _y [mm], β _z [mm] | 0 | |
| Picture | | |

| Section AE | | |
|--|------------|------------|
| Type | Rectangle | |
| Detailed | 20; 20 | |
| Item material | S 235 | |
| A [m ²] | 4,0000e-04 | |
| A _y [m ²], A _z [m ²] | 3,3333e-04 | 3,3333e-04 |
| A _L [m ² /m], A _D [m ² /m] | 8,0000e-02 | 8,0000e-02 |
| c _{y,UCS} [mm], c _{z,UCS} [mm] | 10 | 10 |
| α [deg] | 0,00 | |
| I _y [m ⁴], I _z [m ⁴] | 1,3333e-08 | 1,3333e-08 |
| i _y [mm], i _z [mm] | 6 | 6 |
| W _{el,y} [m ³], W _{el,z} [m ³] | 1,3333e-06 | 1,3333e-06 |
| W _{pl,y} [m ³], W _{pl,z} [m ³] | 2,0000e-06 | 2,0000e-06 |
| M _{pl,y,+} [Nm], M _{pl,y,-} [Nm] | 470,00 | 470,00 |
| M _{pl,z,+} [Nm], M _{pl,z,-} [Nm] | 470,00 | 470,00 |
| d _y [mm], d _z [mm] | 0 | |
| I _t [m ⁴], I _w [m ⁶] | 2,2517e-08 | 0,0000e+00 |
| β _y [mm], β _z [mm] | 0 | |
| Picture | | |

3. LOAD

3.1. LC1 / Tot. value



3.2. Line force

| Name | Member | Type | Dir | Value - P ₁ [kN/m] | Pos x ₁ | Coor | Orig | Ecc ey [m] |
|------|-----------|--------|--------------|----------------------------------|--------------------|--------|------------|---------------|
| | Load case | System | Distribution | Value - P ₂ [kN/m] | Pos x ₂ | Loc | | Ecc ez [m] |
| LF2 | B2 | Force | Z | -1,00 | 0.000 | Rela | From start | 0,000 |
| | LC1 | GCS | Uniform | | 1.000 | Length | | 0,000 |

3.3. Point force on beam

| Name | Member | System | Value - F [kN] | Pos x | Coor | Rep (n) |
|------|-----------|--------|-------------------|-------|------------|-----------|
| | Load case | Dir | Type | | Orig | Regularly |
| Fb2 | B1 | GCS | -100,00 | 0.500 | Rela | 1 |
| | LC1 | Z | Force | | From start | |

4. RESULTS

4.1. 1D internal forces; M_y

Valeur: M_y

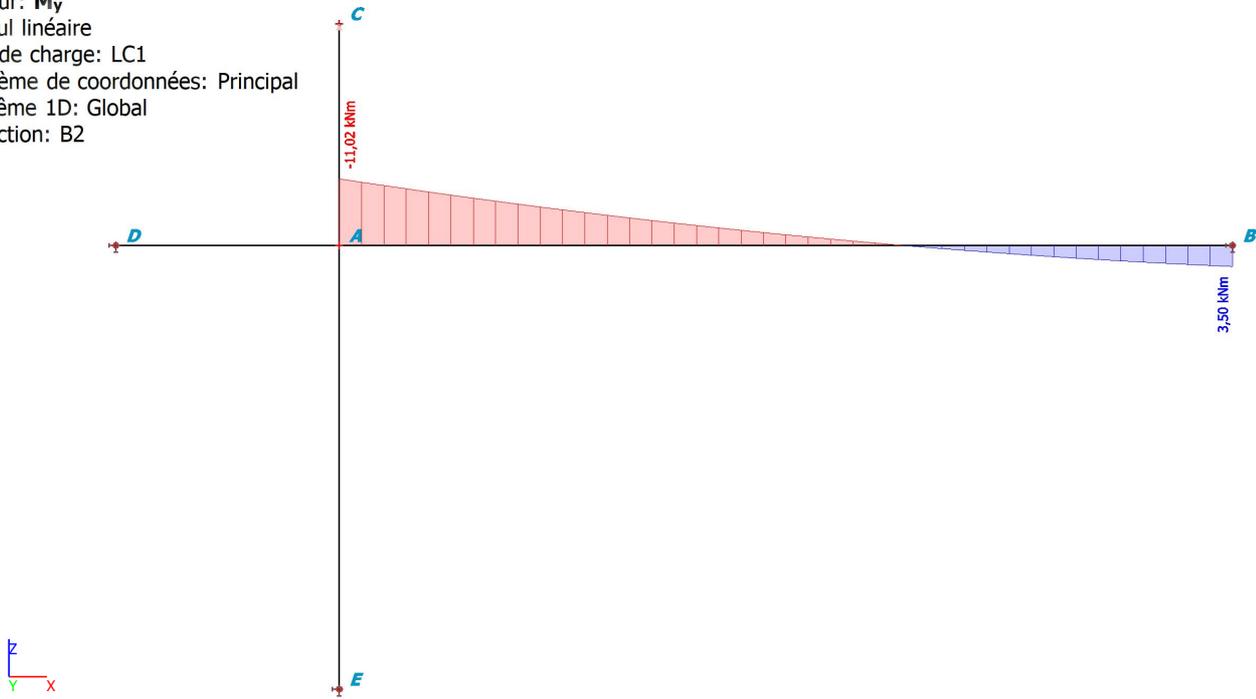
Calcul linéaire

Cas de charge: LC1

Système de coordonnées: Principal

Extrême 1D: Global

Sélection: B2



4.2. 1D internal forces; M_y

Valeur: M_y

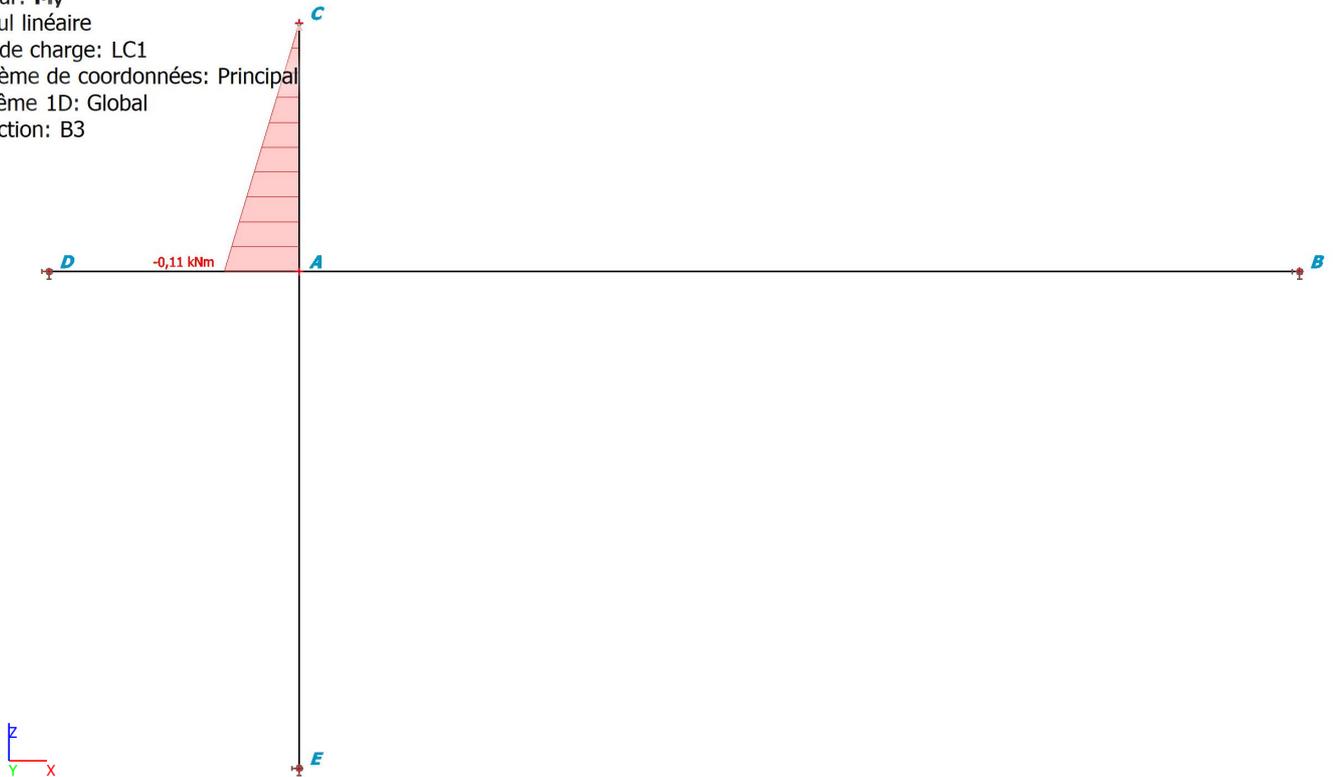
Calcul linéaire

Cas de charge: LC1

Système de coordonnées: Principal

Extrême 1D: Global

Sélection: B3



4.3. 1D internal forces; M_y

Valeur: M_y

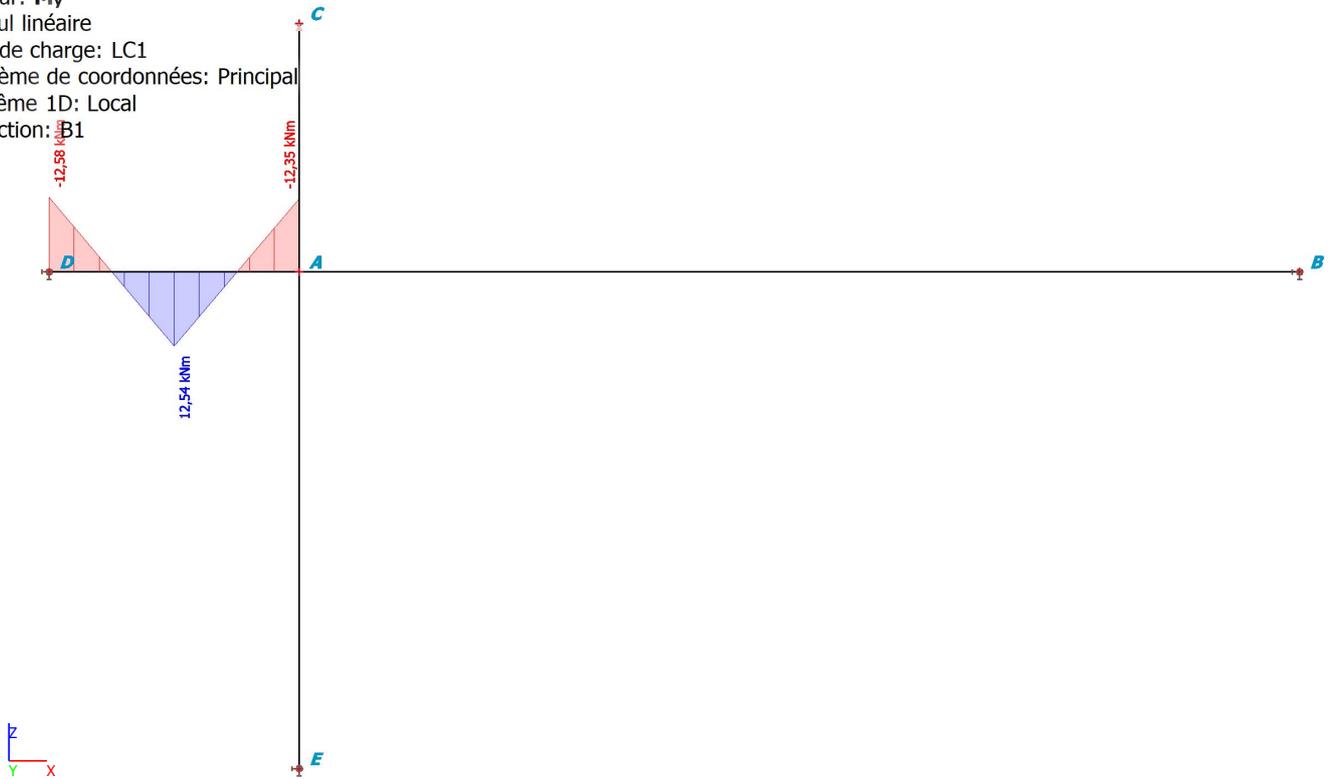
Calcul linéaire

Cas de charge: LC1

Système de coordonnées: Principal

Extrême 1D: Local

Sélection: B1



4.4. 1D internal forces; M_y

Valeur: M_y

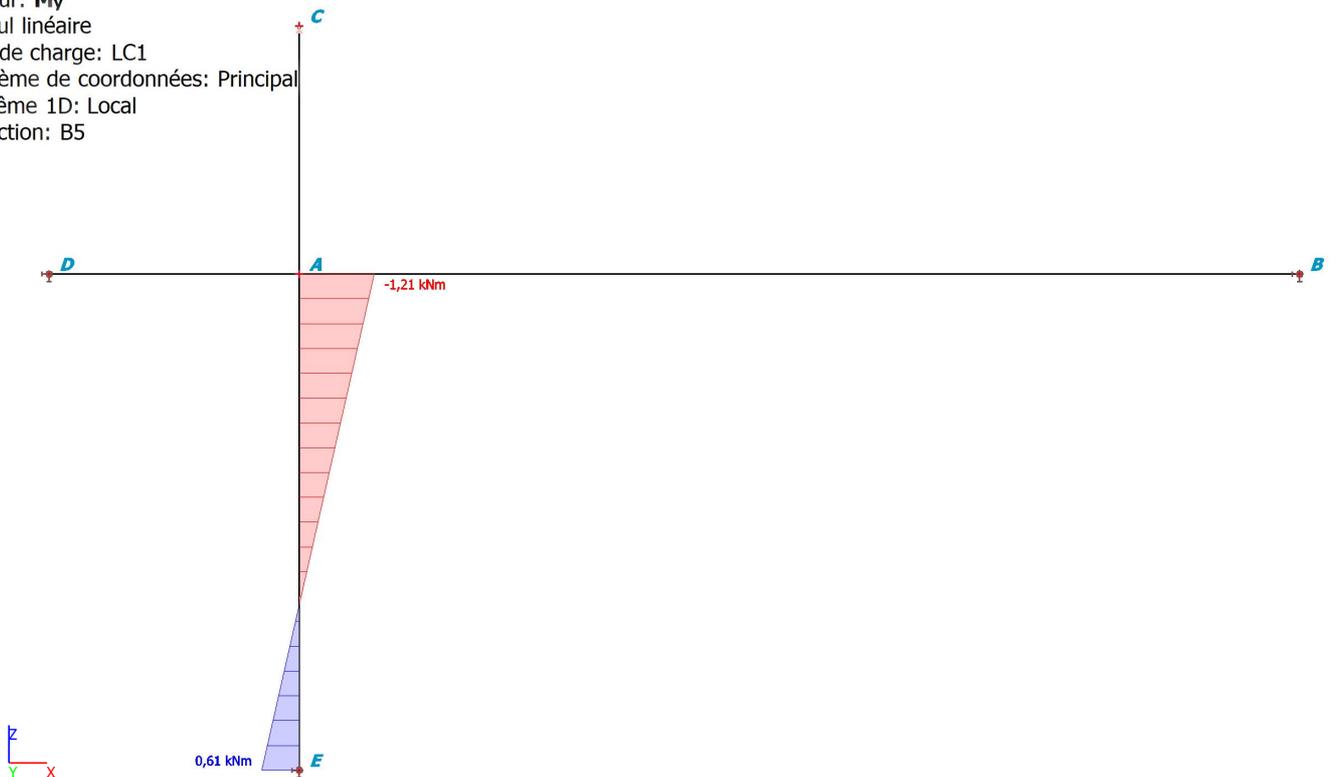
Calcul linéaire

Cas de charge: LC1

Système de coordonnées: Principal

Extrême 1D: Local

Sélection: B5



4.5. Displacement of nodes

Linear calculation

Load case: LC1

Extreme: Global

Selection: A

| Name | Case | Φ_y [mrad] |
|------|------|--------------------|
| A | LC1 | -216,6 |

5. EXPECTED AFNOR RESULTS

Bending Moment poutre AB in node A = 11.02 kNm

Bending Moment poutre AC in node A = 0.11 kNm

Bending Moment poutre AD in node A = -12.35 kNm

Bending Moment poutre AE in node A = 1.21 kNm

Rotation ϕ_{iy} in node A = 227.118 mrad

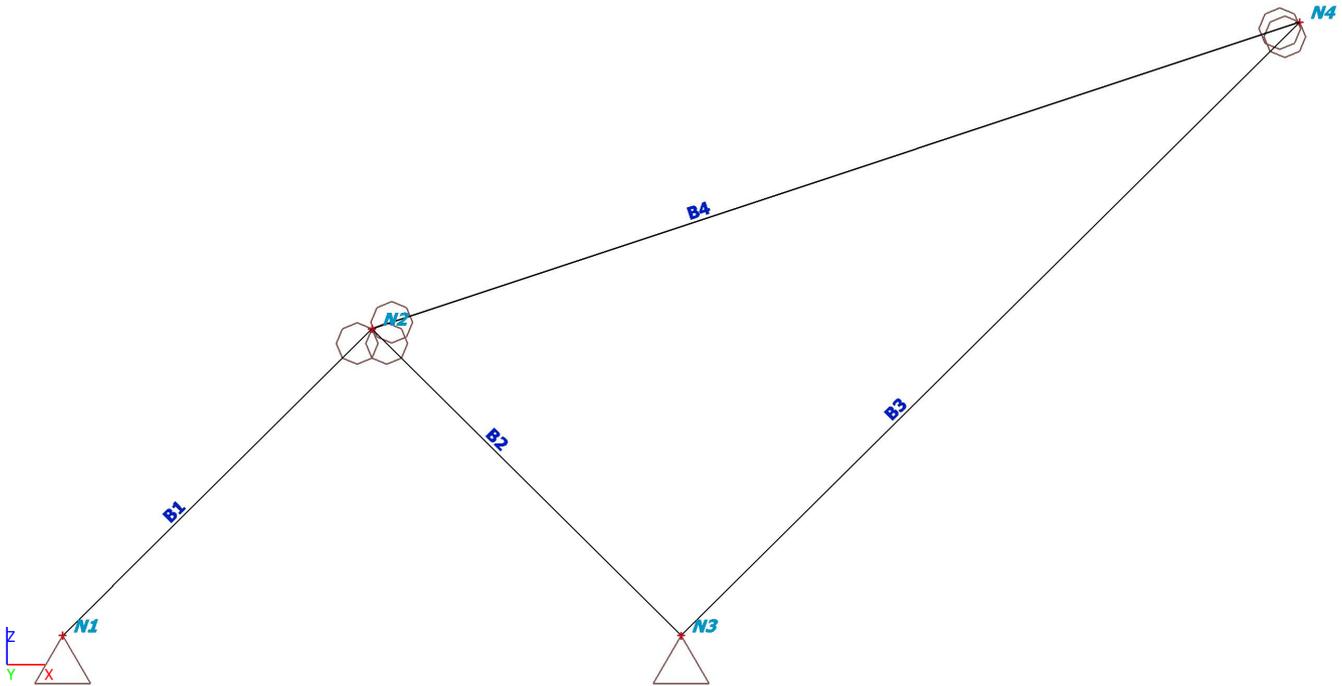
REFERENCE : "Guide de validation des progiciels de calcul de structures" AFNOR, 1990

1. TESTCASE DESCRIPTION

Truss made of four bars of different cross sections; material: elastic, linear, isotropic (non-compressible bars assumed).

2. MODEL

2.1. Analysis model



2.2. Nodes

| Name | Coord X [m] | Coord Z [m] | Member | Data |
|------|-------------|-------------|----------------|------|
| N1 | 0,000 | 0,000 | B1 | Sn2 |
| N2 | 0,500 | 0,500 | B1 B2 B4 | |
| N3 | 1,000 | 0,000 | B2 B3 | Sn1 |
| N4 | 2,000 | 1,000 | B3 B4 | F1 |

2.3. Members

| Name | Cross-section | Material | Length [m] | Beg. node | End node | Type |
|------|--------------------------------|----------|------------|-----------|----------|-------------|
| B1 | Section AC et CB - Cercle (16) | S 235 | 0,707 | N1 | N2 | general (0) |
| B2 | Section AC et CB - Cercle (16) | S 235 | 0,707 | N2 | N3 | general (0) |
| B3 | Section CD et BD - Cercle (11) | S 235 | 1,414 | N3 | N4 | general (0) |
| B4 | Section CD et BD - Cercle (11) | S 235 | 1,581 | N2 | N4 | general (0) |

2.4. Hinges

| Name | Member | Position | ux | uy | uz | fix | fiy | fiz |
|------|--------|----------|-------|----|-------|-----|------|-----|
| H1 | B4 | Both | Rigid | | Rigid | | Free | |
| H2 | B3 | End | Rigid | | Rigid | | Free | |
| H3 | B1 | End | Rigid | | Rigid | | Free | |
| H4 | B2 | Begin | Rigid | | Rigid | | Free | |

2.5. Nodal supports

| Name | Node | System | Type | X | Z | Ry |
|------|------|--------|----------|-------|-------|------|
| Sn1 | N3 | GCS | Standard | Rigid | Rigid | Free |
| Sn2 | N1 | GCS | Standard | Rigid | Rigid | Free |

2.6. Materials

Steel EC3

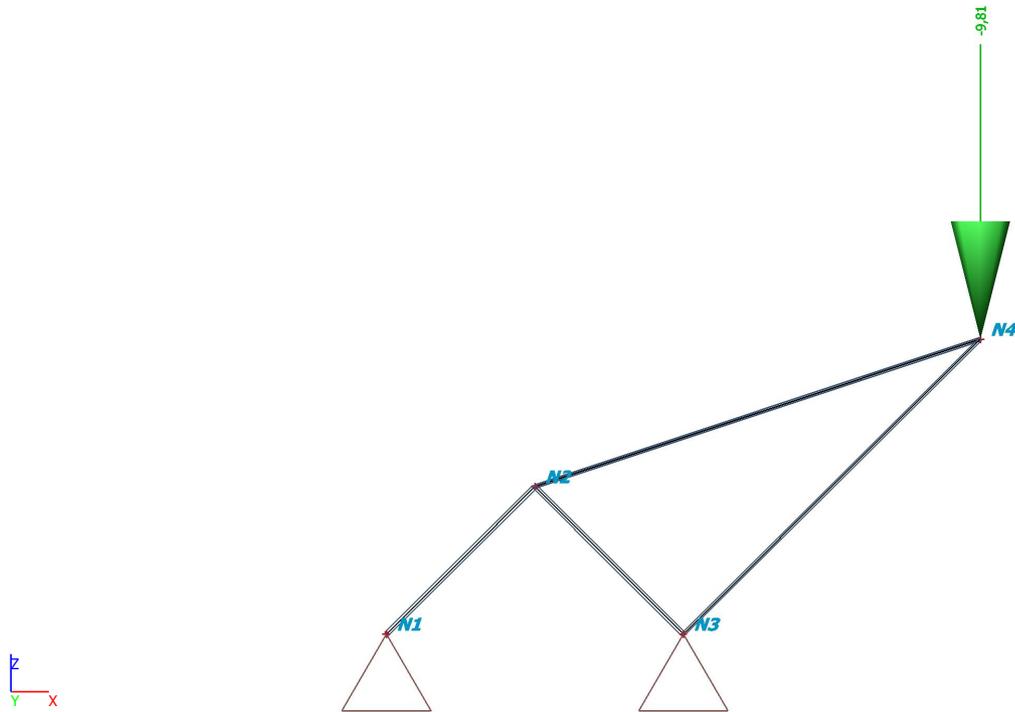
| Name | ρ [kg/m ³] | E_{mod} [MPa] | μ | Limite inférieure [mm] | Limite supérieure [mm] | F_y [MPa] | F_u [MPa] | Colour |
|-------|--------------------------------|--------------------|--------------------|---------------------------|---------------------------|----------------|----------------|--------|
| | | G_{mod} [MPa] | α [m/mK] | | | | | |
| S 235 | 7850,00 | 1,9620e+05 | 0.3 | 0 | 40 | 235,0 | 360,0 | ■ |
| | | 7,5462e+04 | 0,01e-003 | 40 | 80 | 215,0 | 360,0 | |

2.7. Cross-sections

| Section AC et CB | | |
|--|------------|------------|
| Type | Cercle | |
| Detailed | 16 | |
| Item material | S 235 | |
| A [m ²] | 2,0000e-04 | |
| A _y [m ²], A _z [m ²] | 1,8000e-04 | 1,8000e-04 |
| A _L [m ² /m], A _D [m ² /m] | 5,0130e-02 | 5,0130e-02 |
| c _{y,UCS} [mm], c _{z,UCS} [mm] | 8 | 8 |
| α [deg] | 0,00 | |
| I _y [m ⁴], I _z [m ⁴] | 3,1831e-09 | 3,1831e-09 |
| i _y [mm], i _z [mm] | 4 | 4 |
| W _{el,y} [m ³], W _{el,z} [m ³] | 3,9894e-07 | 3,9894e-07 |
| W _{pl,y} [m ³], W _{pl,z} [m ³] | 6,7727e-07 | 6,7727e-07 |
| M _{pl,y,+} [Nm], M _{pl,y,-} [Nm] | 159,11 | 159,11 |
| M _{pl,z,+} [Nm], M _{pl,z,-} [Nm] | 159,11 | 159,11 |
| d _y [mm], d _z [mm] | 0 | |
| I _e [m ⁴], I _w [m ⁶] | 6,3662e-09 | 0,0000e+00 |
| β_y [mm], β_z [mm] | 0 | |
| Picture | | |
| Section CD et BD | | |
| Type | Cercle | |
| Detailed | 11 | |
| Item material | S 235 | |
| A [m ²] | 1,0000e-04 | |
| A _y [m ²], A _z [m ²] | 9,0000e-05 | 9,0000e-05 |
| A _L [m ² /m], A _D [m ² /m] | 3,5447e-02 | 3,5447e-02 |
| c _{y,UCS} [mm], c _{z,UCS} [mm] | 6 | 6 |
| α [deg] | 0,00 | |
| I _y [m ⁴], I _z [m ⁴] | 7,9577e-10 | 7,9577e-10 |
| i _y [mm], i _z [mm] | 3 | 3 |
| W _{el,y} [m ³], W _{el,z} [m ³] | 1,4105e-07 | 1,4105e-07 |
| W _{pl,y} [m ³], W _{pl,z} [m ³] | 2,3945e-07 | 2,3945e-07 |
| M _{pl,y,+} [Nm], M _{pl,y,-} [Nm] | 56,25 | 56,25 |
| M _{pl,z,+} [Nm], M _{pl,z,-} [Nm] | 56,25 | 56,25 |
| d _y [mm], d _z [mm] | 0 | |
| I _e [m ⁴], I _w [m ⁶] | 1,5915e-09 | 0,0000e+00 |
| β_y [mm], β_z [mm] | 0 | |
| Picture | | |

3. LOAD

3.1. LC2 / Valeur totale



3.2. Point force in node

| Name | Node | Load case | System | Dir | Type | Value - F [kN] |
|------|------|-----------------|--------|-----|-------|----------------|
| F1 | N4 | LC2 - Permanent | GCS | Z | Force | -9,81 |

4. RESULTS

4.1. Displacement of node N2

Linear calculation

Load case: LC2

Extreme: Global

Selection: N2

| Name | Case | U _x [mm] | U _z [mm] |
|------|------|------------------------|------------------------|
| N2 | LC2 | 0,26523 | 0,08842 |

4.2. Displacement of node N4

Linear calculation

Load case: LC2

Extreme: Global

Selection: N4

| Name | Case | U _x [mm] | U _z [mm] |
|------|------|------------------------|------------------------|
| N4 | LC2 | 3,47916 | -5,60048 |

5. EXPECTED AFNOR RESULTS

Displacement ux in node N2 = 0,26517mm

Displacement uz in node N2 = 0,08839mm

Displacement ux in node N4 = 3,47902mm

Displacement uz in node N4 = -5,60084mm

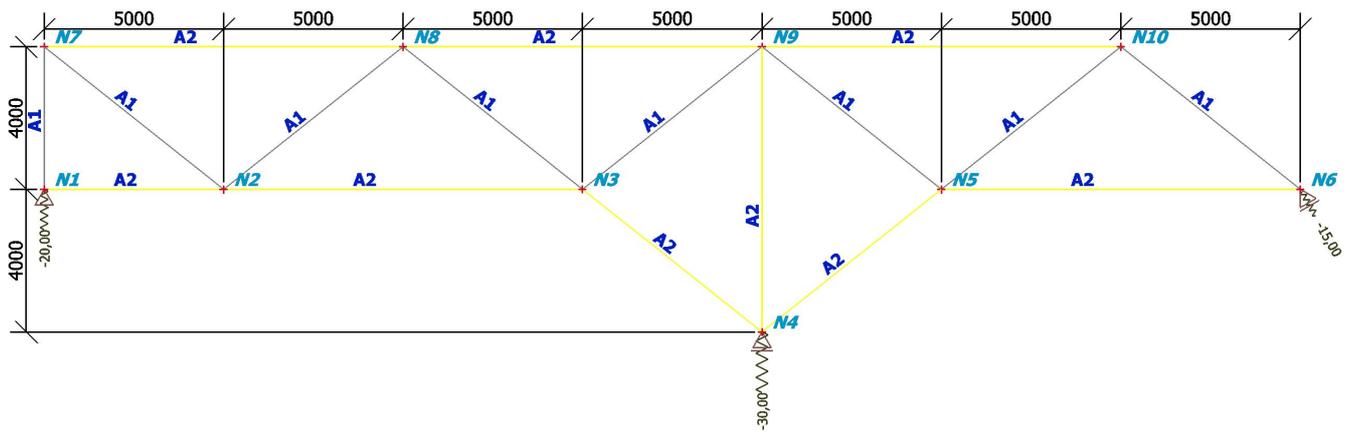
REFERENCE : "Guide de validation des progiciels de calcul de structures" AFNOR, 1990

1. TESTCASE DESCRIPTION

Triangular system of hinged bar under concentrated load, imposed displacement and thermal load.

2. MODEL

2.1. Analysis model



2.2. Nodes

| Name | Coord X [m] | Coord Z [m] | Member | LCS | Data |
|------|-------------|-------------|------------------------|-----|------|
| N1 | 0,000 | 0,000 | B1 B6 | * | Sn2 |
| N2 | 5,000 | 0,000 | B1 B2 B10 B11 | * | |
| N3 | 15,000 | 0,000 | B2 B3 B12 B13 | * | |
| N4 | 20,000 | -4,000 | B3 B4 B17 | * | Sn3 |
| N5 | 25,000 | 0,000 | B4 B5 B14 B15 | * | |

| Name | Coord X [m] | Coord Z [m] | Member | LCS | Data |
|------|-------------|-------------|-------------------------------|-----|------|
| N6 | 35,000 | 0,000 | B5 B16 | ✓ | Sn1 |
| N7 | 0,000 | 4,000 | B6 B7 B10 | * | |
| N8 | 10,000 | 4,000 | B7 B8 B11 B12 | * | F1 |
| N9 | 20,000 | 4,000 | B8 B9 B13 B14 B17 | * | |
| N10 | 30,000 | 4,000 | B9 B15 B16 | * | F2 |

2.3. Members

| Name | Cross-section | Material | Length [m] | Beg. node | End node | Type |
|------|------------------|----------|------------|-----------|----------|-------------|
| B1 | A2 - Cercle (60) | S 235 | 5,000 | N1 | N2 | general (0) |
| B2 | A2 - Cercle (60) | S 235 | 10,000 | N2 | N3 | general (0) |
| B3 | A2 - Cercle (60) | S 235 | 6,403 | N3 | N4 | general (0) |
| B4 | A2 - Cercle (60) | S 235 | 6,403 | N4 | N5 | general (0) |
| B5 | A2 - Cercle (60) | S 235 | 10,000 | N5 | N6 | general (0) |

| Name | Cross-section | Material | Length [m] | Beg. node | End node | Type |
|------|------------------|----------|------------|-----------|----------|-------------|
| B6 | A1 - Cercle (42) | S 235 | 4,000 | N1 | N7 | general (0) |
| B7 | A2 - Cercle (60) | S 235 | 10,000 | N7 | N8 | general (0) |
| B8 | A2 - Cercle (60) | S 235 | 10,000 | N8 | N9 | general (0) |
| B9 | A2 - Cercle (60) | S 235 | 10,000 | N9 | N10 | general (0) |
| B10 | A1 - Cercle (42) | S 235 | 6,403 | N7 | N2 | general (0) |
| B11 | A1 - Cercle (42) | S 235 | 6,403 | N2 | N8 | general (0) |
| B12 | A1 - Cercle (42) | S 235 | 6,403 | N8 | N3 | general (0) |
| B13 | A1 - Cercle (42) | S 235 | 6,403 | N3 | N9 | general (0) |
| B14 | A1 - Cercle (42) | S 235 | 6,403 | N9 | N5 | general (0) |
| B15 | A1 - Cercle (42) | S 235 | 6,403 | N5 | N10 | general (0) |
| B16 | A1 - Cercle (42) | S 235 | 6,403 | N10 | N6 | general (0) |
| B17 | A2 - Cercle (60) | S 235 | 8,000 | N4 | N9 | general (0) |

2.4. Nodal supports

| Name | Node | System | Type | X | Z | Ry |
|------|------|-------------|----------|-------|-------|------|
| Sn1 | N6 | LCS of node | Standard | Free | Rigid | Free |
| Sn2 | N1 | GCS | Standard | Rigid | Rigid | Free |
| Sn3 | N4 | GCS | Standard | Free | Rigid | Free |

2.5. Materials

Steel EC3

| Name | ρ [kg/m ³] | E_{mod} [MPa] | μ | Limit inférieure [mm] | Limite supérieure [mm] | F_y [MPa] | F_u [MPa] | Colour |
|-------|--------------------------------|--------------------|--------------------|--------------------------|---------------------------|----------------|----------------|--------|
| | | G_{mod} [MPa] | α [m/mK] | | | | | |
| S 235 | 7850,00 | 2,1000e+05 | 0.3 | 0 | 40 | 235,0 | 360,0 | ■ |
| | | 8,0769e+04 | 0,01e-003 | 40 | 80 | 215,0 | 360,0 | |

2.6. Cross-sections

| A1 | | |
|--|------------|------------|
| Type | Cercle | |
| Detailed | 42 | |
| Item material | S 235 | |
| A [m ²] | 1,4100e-03 | |
| A _y [m ²], A _z [m ²] | 1,2690e-03 | 1,2690e-03 |
| A _L [m ² /m], A _D [m ² /m] | 1,3310e-01 | 1,3310e-01 |
| c _{y,UCS} [mm], c _{z,UCS} [mm] | 21 | 21 |
| α [deg] | 0,00 | |
| I _y [m ⁴], I _z [m ⁴] | 1,5821e-07 | 1,5821e-07 |
| i _y [mm], i _z [mm] | 11 | 11 |
| W _{el,y} [m ³], W _{el,z} [m ³] | 7,4678e-06 | 7,4678e-06 |
| W _{pl,y} [m ³], W _{pl,z} [m ³] | 1,2678e-05 | 1,2678e-05 |
| M _{pl,y,+} [Nm], M _{pl,y,-} [Nm] | 2978,37 | 2978,37 |
| M _{pl,z,+} [Nm], M _{pl,z,-} [Nm] | 2978,37 | 2978,37 |
| d _y [mm], d _z [mm] | 0 | 0 |
| I _e [m ⁴], I _w [m ⁶] | 3,1642e-07 | 0,0000e+00 |
| β _y [mm], β _z [mm] | 0 | 0 |
| Picture | | |
| A2 | | |
| Type | Cercle | |
| Detailed | 60 | |
| Item material | S 235 | |
| A [m ²] | 2,8200e-03 | |
| A _y [m ²], A _z [m ²] | 2,5380e-03 | 2,5380e-03 |
| A _L [m ² /m], A _D [m ² /m] | 1,8824e-01 | 1,8824e-01 |
| c _{y,UCS} [mm], c _{z,UCS} [mm] | 30 | 30 |
| α [deg] | 0,00 | |
| I _y [m ⁴], I _z [m ⁴] | 6,3283e-07 | 6,3283e-07 |
| i _y [mm], i _z [mm] | 15 | 15 |
| W _{el,y} [m ³], W _{el,z} [m ³] | 2,1122e-05 | 2,1122e-05 |
| W _{pl,y} [m ³], W _{pl,z} [m ³] | 3,5858e-05 | 3,5858e-05 |
| M _{pl,y,+} [Nm], M _{pl,y,-} [Nm] | 8424,09 | 8424,09 |
| M _{pl,z,+} [Nm], M _{pl,z,-} [Nm] | 8424,09 | 8424,09 |
| d _y [mm], d _z [mm] | 0 | 0 |
| I _e [m ⁴], I _w [m ⁶] | 1,2657e-06 | 0,0000e+00 |
| β _y [mm], β _z [mm] | 0 | 0 |
| Picture | | |

3. LOAD

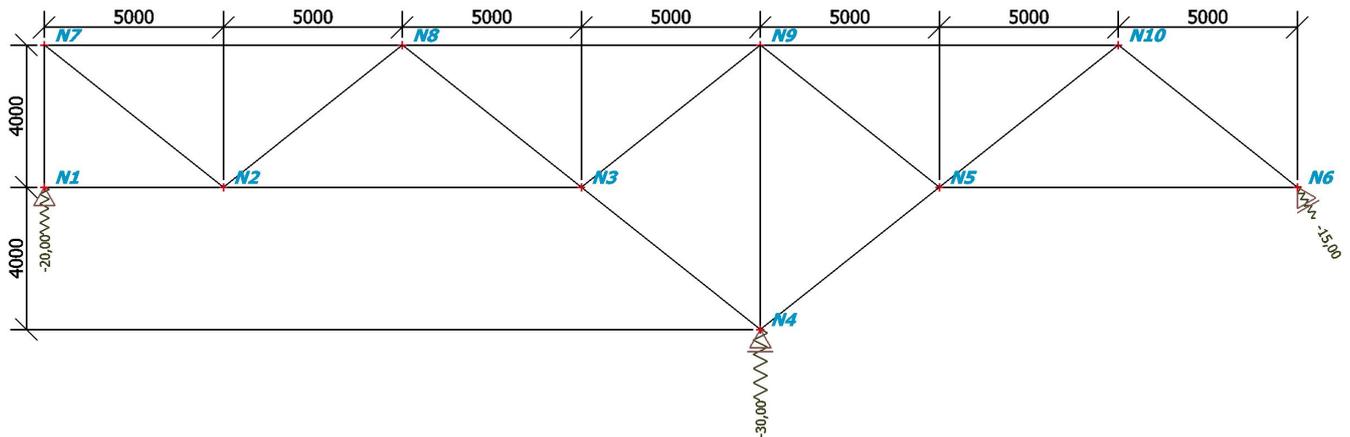
3.1. Load cases

| Name | Description | Action type | Load group |
|------|--------------|-------------|------------|
| | Spec | Load type | |
| LC1 | Displacement | Permanent | LG1 |
| | | Standard | |
| LC2 | Permanent | Permanent | LG1 |
| | | Standard | |
| LC3 | Temperature | Permanent | LG1 |
| | | Standard | |

3.2. Combinations

| Name | Description | Type | Load cases | Coeff. [-] |
|---------------|-------------|-------------------|--------------------|------------|
| comb lineaire | | Linear - ultimate | LC1 - Displacement | 1,000 |
| | | | LC2 - Permanent | 1,000 |
| | | | LC3 - Temperature | 1,000 |

3.3. LC1 - Displacement

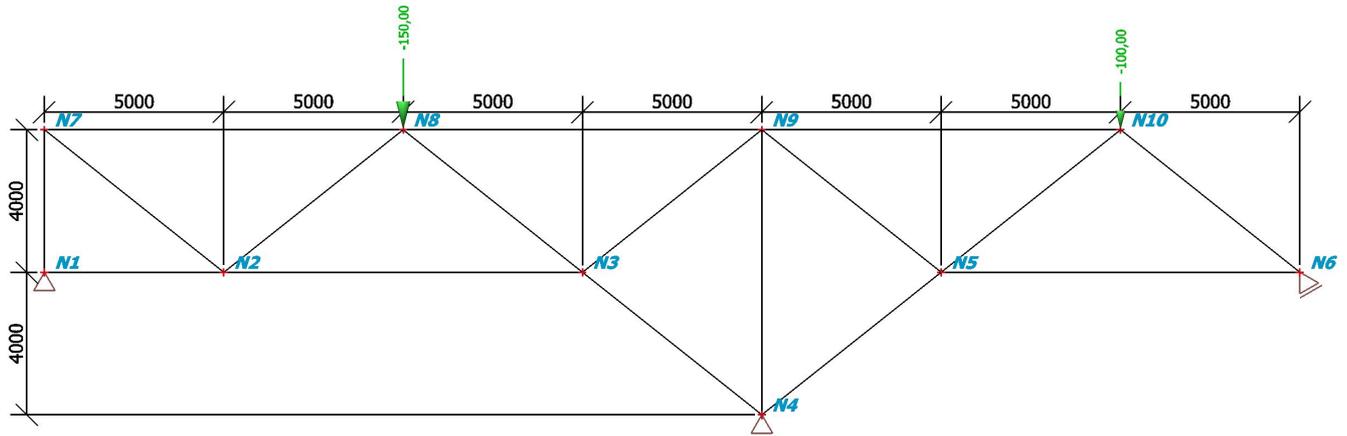


3.4. Point translation

| Name | Support in node | Load case | System | Dir | Value - U [mm] |
|------|-----------------|--------------------|--------|-----|----------------|
| TRS1 | Sn1 | LC1 - Displacement | LCS | Z | -15,00 |
| TRS2 | Sn2 | LC1 - Displacement | LCS | Z | -20,00 |
| TRS3 | Sn3 | LC1 - Displacement | LCS | Z | -30,00 |

| Explanations of symbols | |
|-------------------------|--------------|
| Load case | Displacement |

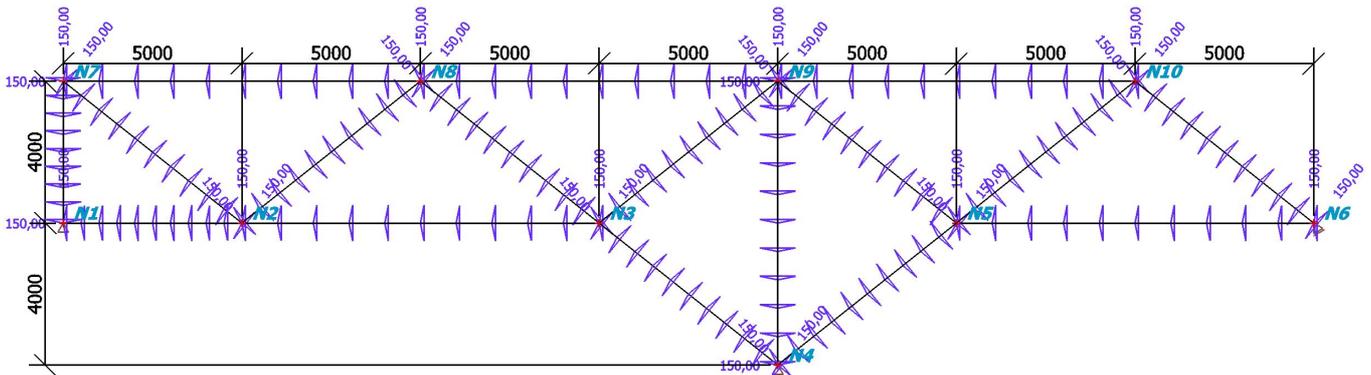
3.5. LC2 - Forces



3.6. Point force in node

| Name | Node | Load case | System | Dir | Type | Value - F [kN] |
|------|------|-----------------|--------|-----|-------|----------------|
| F1 | N8 | LC2 - Permanent | GCS | Z | Force | -150,00 |
| F2 | N10 | LC2 - Permanent | GCS | Z | Force | -100,00 |

3.7. LC3 - Thermal load



3.8. Thermal load

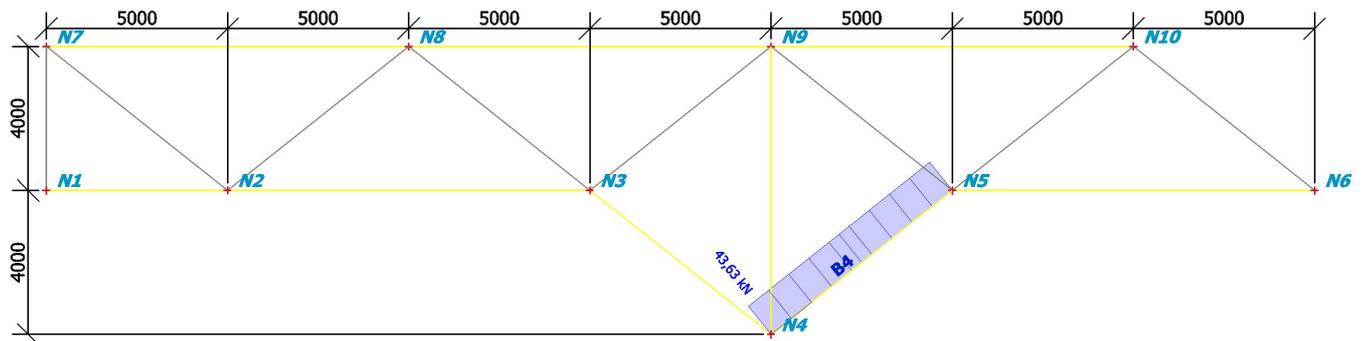
| Name | Member | Load case | Pos x ₁ | Coor | Orig | Distribution | Delta [°C] |
|------|--------|-------------------|--------------------|------|------------|--------------|------------|
| | | | Pos x ₂ | | | | |
| LT1 | B1 | LC3 - Temperature | 0.000 1.000 | Rela | From start | Constant | 150,00 |
| LT2 | B2 | LC3 - Temperature | 0.000 1.000 | Rela | From start | Constant | 150,00 |
| LT3 | B3 | LC3 - Temperature | 0.000 1.000 | Rela | From start | Constant | 150,00 |
| LT4 | B4 | LC3 - Temperature | 0.000 1.000 | Rela | From start | Constant | 150,00 |
| LT5 | B5 | LC3 - Temperature | 0.000 1.000 | Rela | From start | Constant | 150,00 |
| LT6 | B6 | LC3 - Temperature | 0.000 1.000 | Rela | From start | Constant | 150,00 |
| LT7 | B7 | LC3 - Temperature | 0.000 1.000 | Rela | From start | Constant | 150,00 |
| LT8 | B8 | LC3 - Temperature | 0.000 1.000 | Rela | From start | Constant | 150,00 |
| LT9 | B9 | LC3 - Temperature | 0.000 1.000 | Rela | From start | Constant | 150,00 |
| LT10 | B10 | LC3 - Temperature | 0.000 1.000 | Rela | From start | Constant | 150,00 |
| LT11 | B11 | LC3 - Temperature | 0.000 1.000 | Rela | From start | Constant | 150,00 |
| LT12 | B12 | LC3 - Temperature | 0.000 1.000 | Rela | From start | Constant | 150,00 |
| LT13 | B13 | LC3 - Temperature | 0.000 1.000 | Rela | From start | Constant | 150,00 |
| LT14 | B14 | LC3 - Temperature | 0.000 1.000 | Rela | From start | Constant | 150,00 |

| Name | Member | Load case | Pos x ₁ | Coor | Orig | Distribution | Delta [°C] |
|------|--------|-------------------|--------------------|------|------------|--------------|------------|
| | | | Pos x ₂ | | | | |
| LT15 | B15 | LC3 - Temperature | 0.000 | Rela | From start | Constant | 150,00 |
| | | | 1.000 | | | | |
| LT16 | B16 | LC3 - Temperature | 0.000 | Rela | From start | Constant | 150,00 |
| | | | 1.000 | | | | |
| LT17 | B17 | LC3 - Temperature | 0.000 | Rela | From start | Constant | 150,00 |
| | | | 1.000 | | | | |

4. RESULTS

4.1. 1D internal forces; N

Valeur: N
Calcul linéaire
Combinaison: comb lineaire
Système de coordonnées: Elément
Extrême 1D: Elément
Sélection: B4



4.2. 1D internal forces

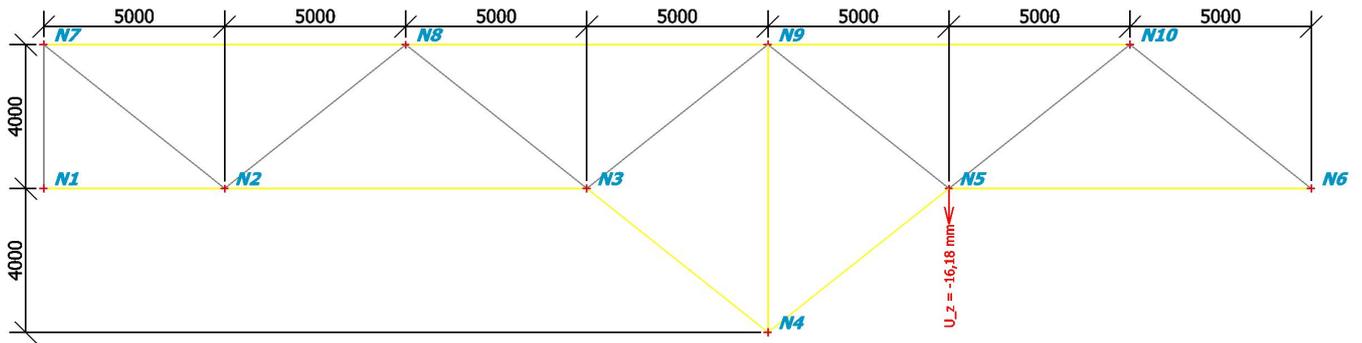
Linear calculation
Combinaison: comb lineaire
Coordinate system: Member
Extreme 1D: Global
Selection: B4

| Name | dx [m] | Case | N [kN] | V _z [kN] | M _y [kNm] |
|------|--------|-----------------|--------------|---------------------|----------------------|
| B4 | 0,000 | comb lineaire/1 | 43,63 | 0,00 | 0,00 |

| Name | Combination key |
|-----------------|-----------------|
| comb lineaire/1 | LC1 + LC2 + LC3 |

4.3. Displacement of nodes; U_z

Valeur: U_z
Calcul linéaire
Combinaison: comb lineaire
Extrême: Global
Sélection: N5



4.4. Displacement of nodes

Linear calculation
Combinaison: comb lineaire
Extreme: Global
Selection: N5

| Name | Case | U _z [mm] |
|------|-----------------|------------------------|
| N5 | comb lineaire/1 | -16,18 |

| Name | Combinaison key |
|-----------------|-----------------|
| comb lineaire/1 | LC1 + LC2 + LC3 |

5. EXPECTED AFNOR RESULTS

Normal force in element B4 = 43.63 kN

Vertical displacement in node N5 = -16.18 mm

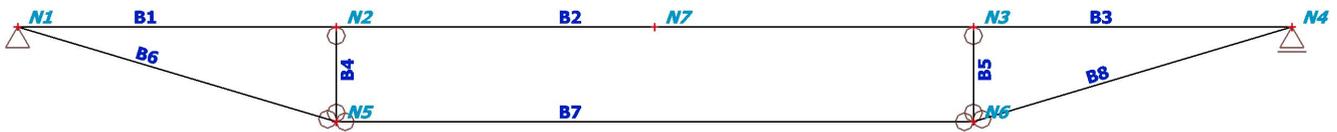
REFERENCE : "Guide de validation des progiciels de calcul de structures" AFNOR, 1990

1. TESTCASE DESCRIPTION

Simply supported beam with truss elements (hinged joints), shortening of bars; elastic, linear, isotropic material.

2. MODEL

2.1. Analysis model



2.2. Nodes

| Name | Coord X [m] | Coord Z [m] | Member | Data |
|------|-------------|-------------|----------------|------|
| N1 | 0,000 | 0,000 | B1 B6 | Sn1 |
| N2 | 2,000 | 0,000 | B1 B2 B4 | |
| N3 | 6,000 | 0,000 | B2 B3 B5 | |
| N4 | 8,000 | 0,000 | B3 B8 | Sn2 |

| Name | Coord X [m] | Coord Z [m] | Member | Data |
|------|-------------|-------------|----------------|------|
| N5 | 2,000 | -0,600 | B4 B6 B7 | |
| N6 | 6,000 | -0,600 | B5 B7 B8 | |
| N7 | 4,000 | 0,000 | B2 | |

2.3. Members

| Name | Cross-section | Material | Length [m] | Beg. node | End node | Type |
|------|---|----------|------------|-----------|----------|-------------|
| B1 | Poutre - Rectangulaire plein (123; 123) | S 235 | 2,000 | N1 | N2 | general (0) |
| B2 | Poutre - Rectangulaire plein (123; 123) | S 235 | 4,000 | N2 | N3 | general (0) |
| B3 | Poutre - Rectangulaire plein (123; 123) | S 235 | 2,000 | N3 | N4 | general (0) |
| B4 | Barre A3 - Rectangulaire plein (59; 59) | S 235 | 0,600 | N2 | N5 | general (0) |
| B5 | Barre A3 - Rectangulaire plein (59; 59) | S 235 | 0,600 | N3 | N6 | general (0) |
| B6 | Barre A1 - Rectangulaire plein (67; 67) | S 235 | 2,088 | N1 | N5 | general (0) |
| B7 | Barre A1 - Rectangulaire plein (67; 67) | S 235 | 4,000 | N5 | N6 | general (0) |
| B8 | Barre A1 - Rectangulaire plein (67; 67) | S 235 | 2,088 | N6 | N4 | general (0) |

2.4. Nodal supports

| Name | Node | System | Type | X | Z | Ry |
|------|------|--------|----------|-------|-------|------|
| Sn1 | N1 | GCS | Standard | Rigid | Rigid | Free |
| Sn2 | N4 | GCS | Standard | Free | Rigid | Free |

2.5. Hinges

| Name | Member | Position | ux | uy | uz | fix | fiy | fiz |
|------|--------|----------|-------|----|-------|-----|------|-----|
| H1 | B8 | Begin | Rigid | | Rigid | | Free | |
| H2 | B6 | End | Rigid | | Rigid | | Free | |
| H3 | B7 | Both | Rigid | | Rigid | | Free | |
| H4 | B5 | Both | Rigid | | Rigid | | Free | |
| H5 | B4 | Both | Rigid | | Rigid | | Free | |

2.6. Materials

Steel EC3

| Name | ρ [kg/m ³] | E_{mod} [MPa] | μ | Limit inférieure [mm] | Limite supérieure [mm] | F_y [MPa] | F_u [MPa] | Colour |
|-------|--------------------------------|--------------------|--------------------|--------------------------|---------------------------|----------------|----------------|--------|
| | | G_{mod} [MPa] | α [m/mK] | | | | | |
| S 235 | 7850,00 | 2,1000e+05 | 0.3 | 0 | 40 | 235,0 | 360,0 | ■ |
| | | 8,4000e+04 | 0,01e-003 | 40 | 80 | 215,0 | 360,0 | |

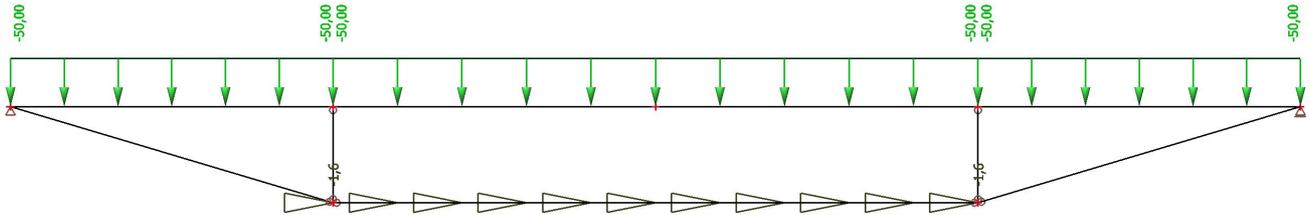
2.7. Cross-sections

| Poutre | | |
|--|------------------------------|------------|
| Type | Rectangulaire plein | |
| Detailed | 123; 123 | |
| Formcode | 7 - Full rectangular section | |
| Item material | S 235 | |
| A [m ²] | 1,5160e-02 | |
| A _y [m ²], A _z [m ²] | 1,2633e-02 | 1,2633e-02 |
| A _L [m ² /m], A _D [m ² /m] | 4,9250e-01 | 4,9250e-01 |
| c _{y.ucs} [mm], c _{z.ucs} [mm] | 62 | 62 |
| α [deg] | 0,00 | |
| I _y [m ⁴], I _z [m ⁴] | 2,1740e-04 | 2,1740e-04 |
| i _y [mm], i _z [mm] | 120 | 120 |
| W _{el.y} [m ³], W _{el.z} [m ³] | 3,5314e-03 | 3,5314e-03 |
| W _{pl.y} [m ³], W _{pl.z} [m ³] | 4,6665e-04 | 4,6665e-04 |
| M _{pl.y.+} [Nm], M _{pl.y.-} [Nm] | 109662,13 | 109662,13 |
| M _{pl.z.+} [Nm], M _{pl.z.-} [Nm] | 109662,13 | 109662,13 |
| d _y [mm], d _z [mm] | 0 | 0 |
| I _t [m ⁴], I _w [m ⁶] | 3,2344e-05 | 0,0000e+00 |
| β _y [mm], β _z [mm] | 0 | 0 |
| Picture | | |
| Barre A1 | | |
| Type | Rectangulaire plein | |
| Detailed | 67; 67 | |
| Formcode | 7 - Full rectangular section | |
| Item material | S 235 | |
| A [m ²] | 4,5000e-03 | |
| A _y [m ²], A _z [m ²] | 3,7500e-03 | 3,7500e-03 |
| A _L [m ² /m], A _D [m ² /m] | 2,6833e-01 | 2,6833e-01 |
| c _{y.ucs} [mm], c _{z.ucs} [mm] | 34 | 34 |
| α [deg] | 0,00 | |
| I _y [m ⁴], I _z [m ⁴] | 1,6875e-06 | 1,6875e-06 |
| i _y [mm], i _z [mm] | 19 | 19 |
| W _{el.y} [m ³], W _{el.z} [m ³] | 5,0312e-05 | 5,0312e-05 |
| W _{pl.y} [m ³], W _{pl.z} [m ³] | 7,5467e-05 | 7,5467e-05 |
| M _{pl.y.+} [Nm], M _{pl.y.-} [Nm] | 17734,81 | 17734,81 |
| M _{pl.z.+} [Nm], M _{pl.z.-} [Nm] | 17734,81 | 17734,81 |
| d _y [mm], d _z [mm] | 0 | 0 |
| I _t [m ⁴], I _w [m ⁶] | 2,8498e-06 | 0,0000e+00 |
| β _y [mm], β _z [mm] | 0 | 0 |
| Picture | | |
| Barre A3 | | |
| Type | Rectangulaire plein | |
| Detailed | 59; 59 | |
| Formcode | 7 - Full rectangular section | |

| | | |
|--|------------|------------|
| Item material | S 235 | |
| A [m ²] | 3,4800e-03 | |
| A _y [m ²], A _z [m ²] | 2,9000e-03 | 2,9000e-03 |
| A _L [m ² /m], A _D [m ² /m] | 2,3597e-01 | 2,3597e-01 |
| c _{y,UCS} [mm], c _{z,UCS} [mm] | 29 | 29 |
| α [deg] | 0,00 | |
| I _y [m ⁴], I _z [m ⁴] | 1,0092e-06 | 1,0092e-06 |
| i _y [mm], i _z [mm] | 17 | 17 |
| W _{el,y} [m ³], W _{el,z} [m ³] | 3,4215e-05 | 3,4215e-05 |
| W _{pl,y} [m ³], W _{pl,z} [m ³] | 5,1323e-05 | 5,1323e-05 |
| M _{pl,y,+} [Nm], M _{pl,y,-} [Nm] | 12060,82 | 12060,82 |
| M _{pl,z,+} [Nm], M _{pl,z,-} [Nm] | 12060,82 | 12060,82 |
| d _y [mm], d _z [mm] | 0 | 0 |
| I _t [m ⁴], I _w [m ⁶] | 1,7043e-06 | 0,0000e+00 |
| β _y [mm], β _z [mm] | 0 | 0 |
| Picture | | |

3. LOAD

3.1. LC2 / Tot. value



3.2. Line force

| Name | Member | Type | Dir | Value - P ₁ [kN/m] | Pos x ₁ | Coor | Orig | Ecc ey [m] |
|------|-----------------|--------|--------------|----------------------------------|--------------------|--------|------------|---------------|
| | Load case | System | Distribution | Value - P ₂ [kN/m] | Pos x ₂ | Loc | | Ecc ez [m] |
| LF1 | B2 | Force | Z | -50,00 | 0.000 | Rela | From start | |
| | LC2 - Permanent | LCS | Uniform | | 1.000 | Length | | 0,000 |
| LF2 | B1 | Force | Z | -50,00 | 0.000 | Rela | From start | |
| | LC2 - Permanent | LCS | Uniform | | 1.000 | Length | | 0,000 |
| LF3 | B3 | Force | Z | -50,00 | 0.000 | Rela | From start | |
| | LC2 - Permanent | LCS | Uniform | | 1.000 | Length | | 0,000 |

3.3. Line translation

| Name | System | Loc | Dir | Distribution | Value - U ₁ [mm/m] |
|------|--------|--------|-----|--------------|----------------------------------|
| LTR1 | LCS | Length | X | Uniform | -1,6 |

4. RESULTS

4.1. 1D internal forces; N

Valeur: **N**

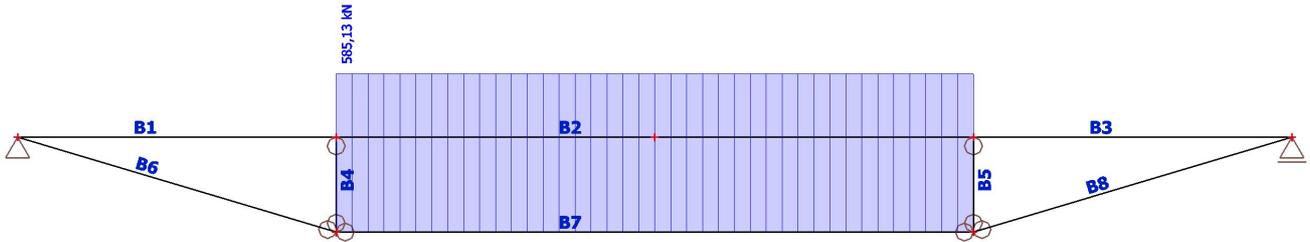
Calcul linéaire

Cas de charge: LC2

Système de coordonnées: Elément

Extrême 1D: Elément

Sélection: B7



4.2. 1D internal forces; M_y

Valeur: **M_y**

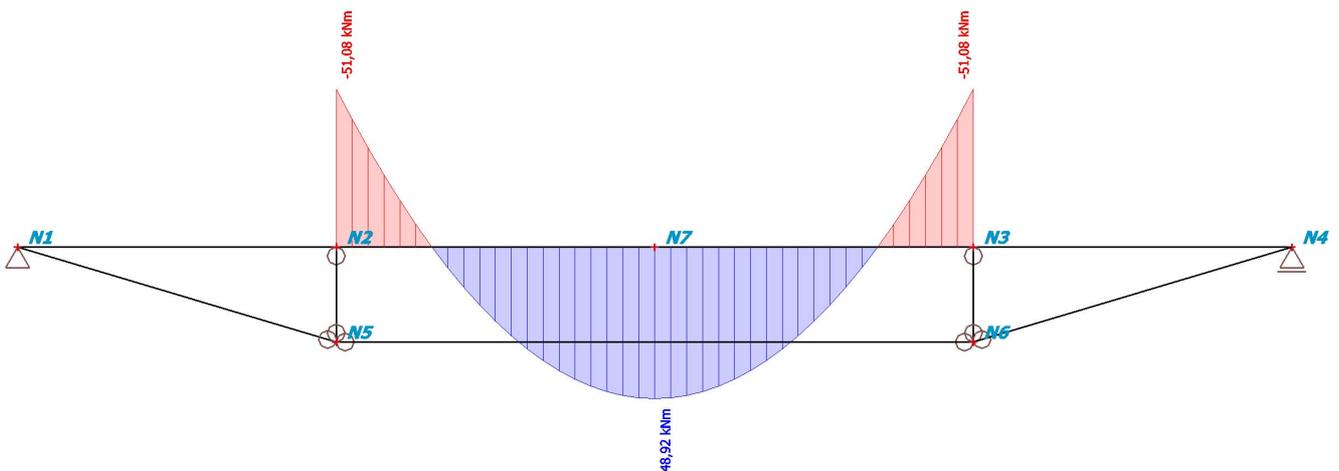
Calcul linéaire

Cas de charge: LC2

Système de coordonnées: Elément

Extrême 1D: Local

Sélection: B2



4.3. Displacement of nodes

Linear calculation

Load case: LC2

Extreme: Global

Selection: N2

| Name | Case | U_z [mm] |
|------|------|---------------|
| N2 | LC2 | -0,6 |

4.4. Displacement of nodes; U_z

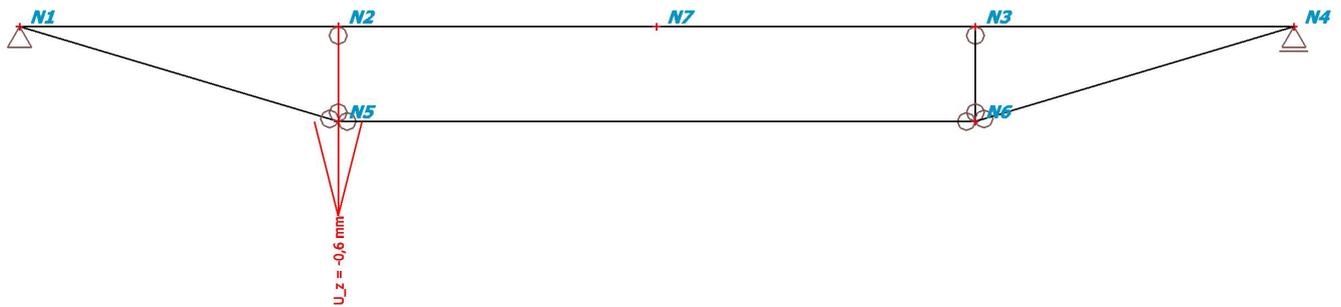
Valeur: U_z

Calcul linéaire

Cas de charge: LC2

Extrême: Global

Sélection: N2



5. EXPECTED AFNOR RESULTS

Shear Force in node B7 = 584.584 kN

Bending Moment in node N7 = 49.249 kNm

Vertical displacement in node N2 = -0.543 mm

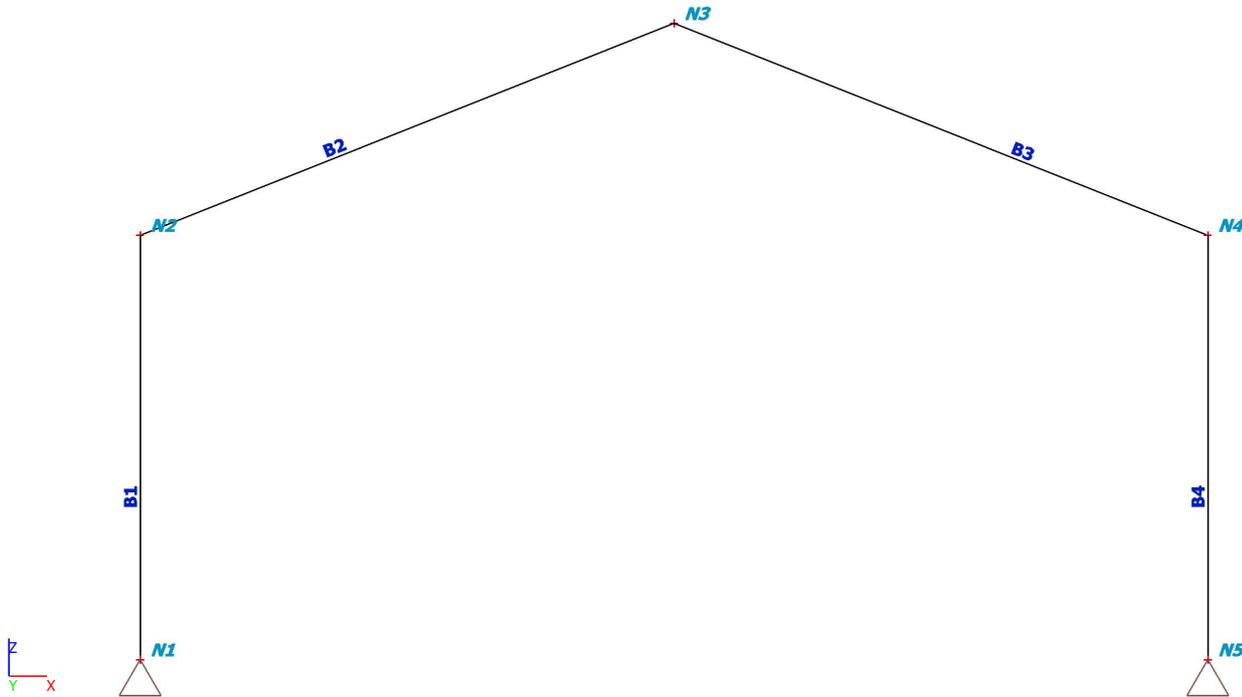
REFERENCE : "Guide de validation des progiciels de calcul de structures" AFNOR, 1990

1. TESTCASE DESCRIPTION

Simply supported symmetrical frame with asymmetric load; material: elastic, linear, isotropic

2. MODEL

2.1. Analysis model



2.2. Nodes

| Name | Coord X [m] | Coord Z [m] | Member | Data |
|------|-------------|-------------|--------|------|
| N1 | 0,000 | 0,000 | B1 | Sn1 |
| N2 | 0,000 | 8,000 | B1 | F2 |
| | | | B2 | M1 |
| N3 | 10,000 | 12,000 | B2 | F1 |
| | | | B3 | |

| Name | Coord X [m] | Coord Z [m] | Member | Data |
|------|-------------|-------------|--------|------|
| N4 | 20,000 | 8,000 | B3 | |
| | | | B4 | |
| N5 | 20,000 | 0,000 | B4 | Sn2 |

2.3. Members

| Name | Cross-section | Material | Length [m] | Beg. node | End node | Type |
|------|---|----------|------------|-----------|----------|--------------|
| B1 | Poteau - Rectangulaire plein (278; 278) | S 235 | 8,000 | N1 | N2 | column (100) |
| B2 | Poutre - Rectangulaire plein (234; 234) | S 235 | 10,770 | N2 | N3 | beam (80) |
| B3 | Poutre - Rectangulaire plein (234; 234) | S 235 | 10,770 | N4 | N3 | beam (80) |
| B4 | Poteau - Rectangulaire plein (278; 278) | S 235 | 8,000 | N5 | N4 | column (100) |

2.4. Nodal supports

| Name | Node | System | Type | X | Z | Ry |
|------|------|--------|----------|-------|-------|------|
| Sn1 | N1 | GCS | Standard | Rigid | Rigid | Free |
| Sn2 | N5 | GCS | Standard | Rigid | Rigid | Free |

2.5. Materials

Steel EC3

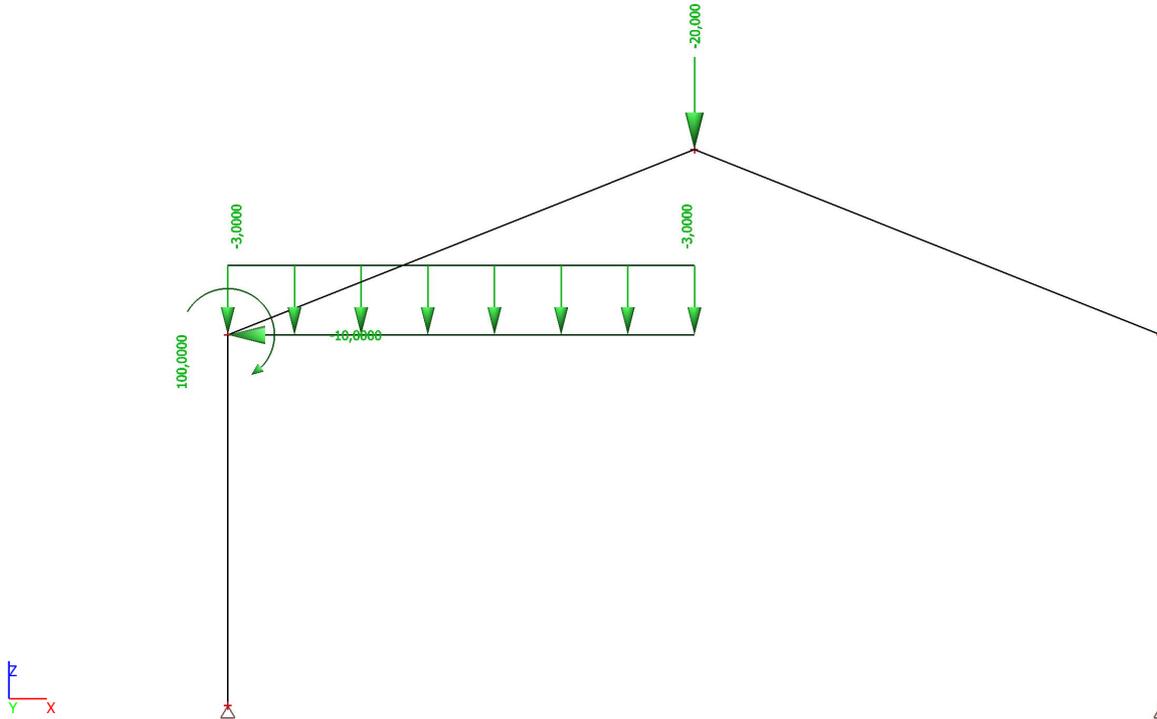
| Name | ρ [kg/m ³] | E_{mod} [MPa] | μ | Limit inférieure [mm] | Limite supérieure [mm] | F_y [MPa] | F_u [MPa] | Colour |
|-------|--------------------------------|--------------------|--------------------|--------------------------|---------------------------|----------------|----------------|--------|
| | | G_{mod} [MPa] | α [m/mK] | | | | | |
| S 235 | 7850,00 | 2,1000e+05 | 0.3 | 0 | 40 | 235,0 | 360,0 | ■ |
| | | 8,0769e+04 | 0,01e-003 | 40 | 80 | 215,0 | 360,0 | |

2.6. Cross-sections

| Poteau | | |
|--|------------------------------|------------|
| Type | Rectangulaire plein | |
| Detailed | 278; 278 | |
| Formcode | 7 - Full rectangular section | |
| Item material | S 235 | |
| A [m ²] | 7,7460e-02 | |
| A _y [m ²], A _z [m ²] | 6,4550e-02 | 6,4550e-02 |
| A _L [m ² /m], A _D [m ² /m] | 1,1133e+00 | 1,1133e+00 |
| c _{y,UCS} [mm], c _{z,UCS} [mm] | 139 | 139 |
| α [deg] | 0,00 | |
| I _y [m ⁴], I _z [m ⁴] | 5,0000e-04 | 5,0000e-04 |
| i _y [mm], i _z [mm] | 80 | 80 |
| W _{el,y} [m ³], W _{el,z} [m ³] | 3,5930e-03 | 3,5930e-03 |
| W _{pl,y} [m ³], W _{pl,z} [m ³] | 5,3896e-03 | 5,3896e-03 |
| M _{pl,y,+} [Nm], M _{pl,y,-} [Nm] | 1266547,00 | 1266547,00 |
| M _{pl,z,+} [Nm], M _{pl,z,-} [Nm] | 1266547,00 | 1266547,00 |
| d _y [mm], d _z [mm] | 0 | 0 |
| I _t [m ⁴], I _w [m ⁶] | 8,4439e-04 | 0,0000e+00 |
| β _y [mm], β _z [mm] | 0 | 0 |
| Picture | | |
| Poutre | | |
| Type | Rectangulaire plein | |
| Detailed | 234; 234 | |
| Formcode | 7 - Full rectangular section | |
| Item material | S 235 | |
| A [m ²] | 5,4772e-02 | |
| A _y [m ²], A _z [m ²] | 4,5644e-02 | 4,5644e-02 |
| A _L [m ² /m], A _D [m ² /m] | 9,3614e-01 | 9,3614e-01 |
| c _{y,UCS} [mm], c _{z,UCS} [mm] | 117 | 117 |
| α [deg] | 0,00 | |
| I _y [m ⁴], I _z [m ⁴] | 2,5000e-04 | 2,5000e-04 |
| i _y [mm], i _z [mm] | 68 | 68 |
| W _{el,y} [m ³], W _{el,z} [m ³] | 2,1364e-03 | 2,1364e-03 |
| W _{pl,y} [m ³], W _{pl,z} [m ³] | 3,2047e-03 | 3,2047e-03 |
| M _{pl,y,+} [Nm], M _{pl,y,-} [Nm] | 753093,35 | 753093,35 |
| M _{pl,z,+} [Nm], M _{pl,z,-} [Nm] | 753093,35 | 753093,35 |
| d _y [mm], d _z [mm] | 0 | 0 |
| I _t [m ⁴], I _w [m ⁶] | 4,2219e-04 | 0,0000e+00 |
| β _y [mm], β _z [mm] | 0 | 0 |
| Picture | | |

3. LOAD

3.1. LC2 / Tot. value



3.2. Point force in node

| Name | Node | Load case | System | Dir | Type | Value - F [kN] |
|------|------|-----------------|--------|-----|-------|----------------|
| F1 | N3 | LC2 - Permanent | GCS | Z | Force | -20,000 |
| F2 | N2 | LC2 - Permanent | GCS | X | Force | -10,000 |

3.3. Moment in node

| Name | Node | Load case | System | Dir | Type | Value - M [kNm] |
|------|------|-----------------|--------|-----|--------|-----------------|
| M1 | N2 | LC2 - Permanent | GCS | My | Moment | 100,000 |

3.4. Line force

| Name | Member | Type | Dir | Value - P ₁ [kN/m] | Pos x ₁ | Coor | Orig | Ecc ey [m] |
|------|-----------------|--------|--------------|-------------------------------|--------------------|------------|------------|------------|
| | Load case | System | Distribution | Value - P ₂ [kN/m] | Pos x ₂ | Loc | | Ecc ez [m] |
| LF1 | B2 | Force | Z | -3,000 | 0.000 | Rela | From start | |
| | LC2 - Permanent | GCS | Uniform | | 1.000 | Projection | | 0,000 |

4. RESULTS

4.1. Reactions

Linear calculation

Load case: LC2

System: Global

Extreme: Global

Selection: Sn1

Nodal reactions

| Name | Case | R _x [kN] | R _z [kN] | M _y [kNm] | e _x [mm] |
|--------|------|------------------------|------------------------|-------------------------|------------------------|
| Sn1/N1 | LC2 | 20,2388 | 31,5000 | 0,0000 | 0,00 |

4.2. Reactions; R_z

Valeur: R_z

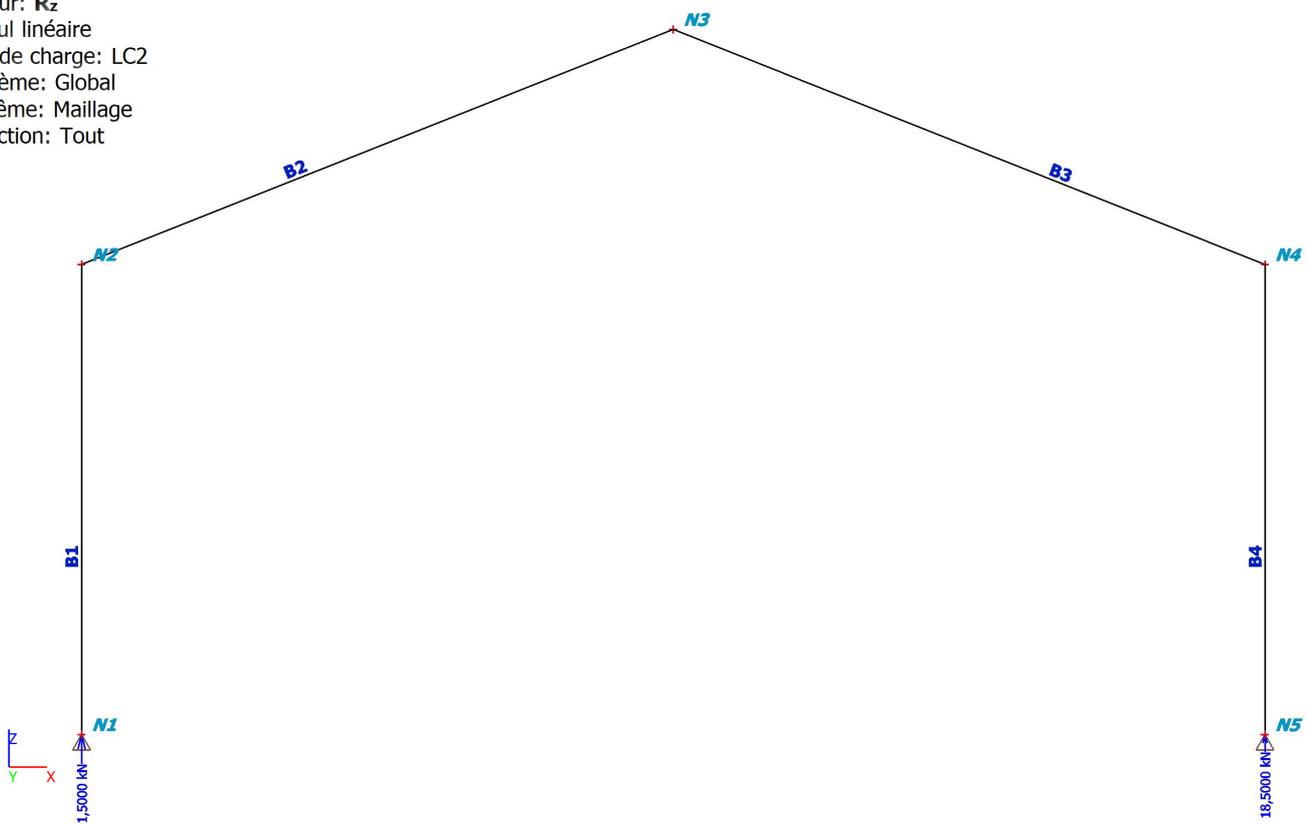
Calcul linéaire

Cas de charge: LC2

Système: Global

Extrême: Maillage

Sélection: Tout



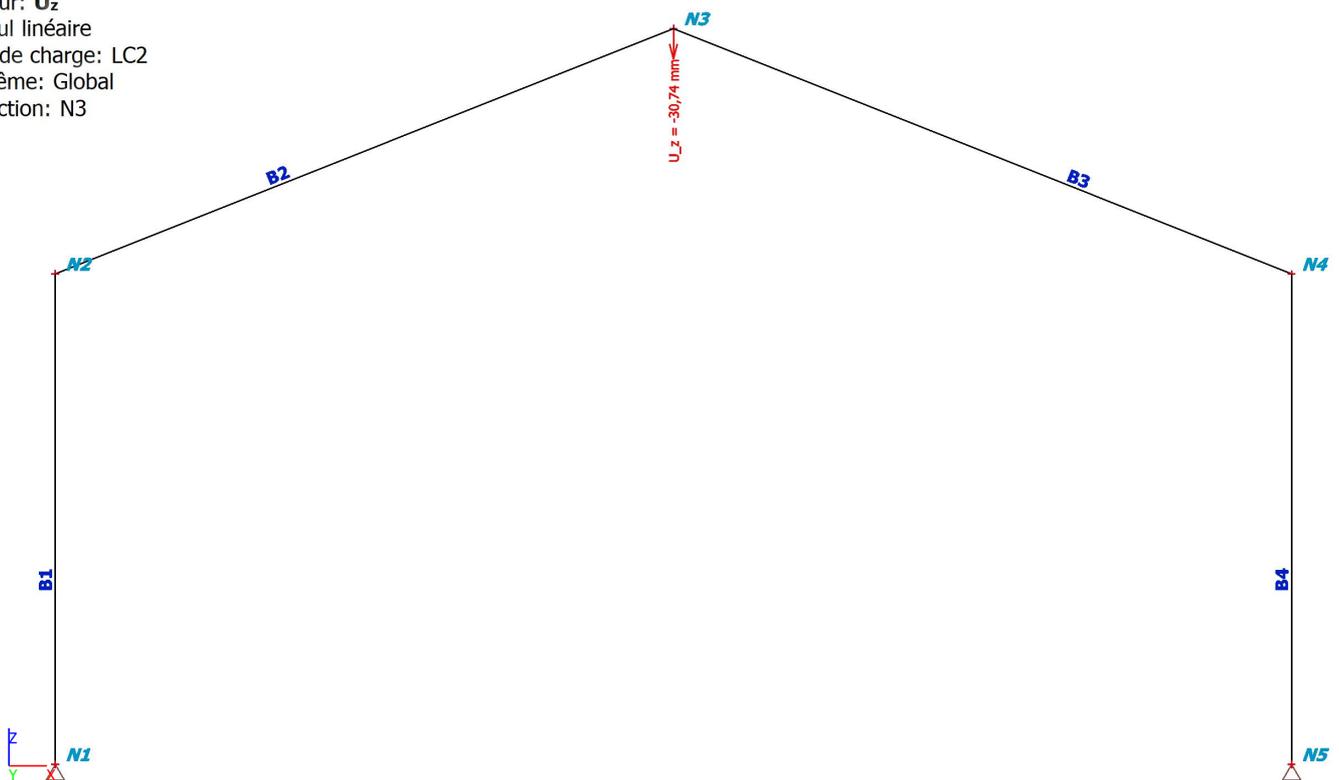
4.3. Displacement of nodes

Linear calculation
 Load case: LC2
 Extreme: Global
 Selection: N3

| Name | Case | U _z [mm] |
|------|------|--------------------------|
| N3 | LC2 | -30,74 |

4.4. Displacement of nodes; U_z

Valeur: U_z
 Calcul linéaire
 Cas de charge: LC2
 Extrême: Global
 Sélection: N3



5. EXPECTED AFNOR RESULTS

Vertical displacement in node N3 = -30,72mm

Vertical reaction in node N1= 31,5KN

Horizontal reaction in N1=20,24 KN

REFERENCE : "Guide de validation des progiciels de calcul de structures" AFNOR, 1990

1. TESTCASE DESCRIPTION

Simple beam on bidirectional, elastic foundation (Winkler's foundation), elastic, linear, isotropic material

2. MODEL

2.1. Analysis model



2.2. Nodes

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] | Member |
|------|-------------|-------------|-------------|--------|
| N1 | 0,000 | 0,000 | 0,000 | B1 |
| N2 | 4,967 | 0,000 | 0,000 | B1 |
| N3 | 2,484 | 0,000 | 0,000 | B1 |

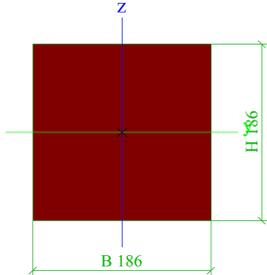
2.3. Members

| Name | Cross-section | Material | Length [m] | Beg. node | End node | Type |
|------|--------------------------------------|----------|------------|-----------|----------|-------------|
| B1 | CS2 - Rectangulaire plein (186; 186) | S 235 | 4,967 | N1 | N2 | general (0) |

2.4. Line supports on member

| Name | Type | Member System | Pos x ₁ Pos x ₂ | Coor Orig | X | Y | Z | Rx | Ry | Rz |
|------|------|---------------|--|------------|-------|-------|----------|-------|------|------|
| Slb1 | Line | B1 | 0.000 | Rela | Rigid | Rigid | Flexible | Rigid | Free | Free |
| | | LCS | 1.000 | From start | | | | | | |

2.5. Cross-sections

| CS2 | | |
|--|--|------------|
| Type | Rectangulaire plein | |
| Detailed | 186; 186 | |
| Formcode | 7 - Full rectangular section | |
| Item material | S 235 | |
| A [m ²] | 3,4641e-02 | |
| A _y [m ²], A _z [m ²] | 2,8868e-02 | 2,8868e-02 |
| A _L [m ² /m], A _D [m ² /m] | 7,4448e-01 | 7,4448e-01 |
| C _{y,UCS} [mm], C _{z,UCS} [mm] | 93 | 93 |
| α [deg] | 0,00 | |
| I _y [m ⁴], I _z [m ⁴] | 1,0000e-04 | 1,0000e-04 |
| i _y [mm], i _z [mm] | 54 | 54 |
| W _{el,y} [m ³], W _{el,z} [m ³] | 1,0746e-03 | 1,0746e-03 |
| W _{pl,y} [m ³], W _{pl,z} [m ³] | 1,6119e-03 | 1,6119e-03 |
| M _{pl,y,+} [Nm], M _{pl,y,-} [Nm] | 378785,90 | 378785,90 |
| M _{pl,z,+} [Nm], M _{pl,z,-} [Nm] | 378785,90 | 378785,90 |
| d _y [mm], d _z [mm] | 0 | |
| I _t [m ⁴], I _w [m ⁶] | 1,6888e-04 | 0,0000e+00 |
| β _y [mm], β _z [mm] | 0 | |
| Picture |  | |

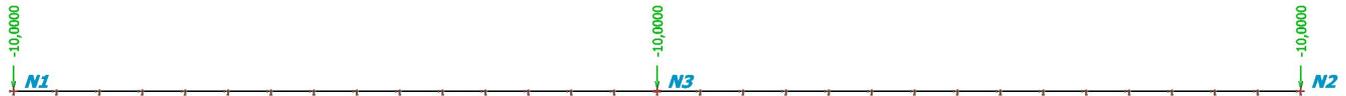
2.6. Materials

Steel EC3

| Name | ρ [kg/m ³] | E _{mod} [MPa] | μ | Limit inférieure [mm] | Limite supérieure [mm] | F _y [MPa] | F _u [MPa] | Colour |
|-------|------------------------|------------------------|-----------|-----------------------|------------------------|----------------------|----------------------|--------|
| | | G _{mod} [MPa] | α [m/mK] | | | | | |
| S 235 | 7850,00 | 2,1000e+05 | 0.3 | 0 | 40 | 235,0 | 360,0 | ■ |
| | | 8,0769e+04 | 0,01e-003 | 40 | 80 | 215,0 | 360,0 | |

3. LOAD

3.1. LC2 / Tot. value



3.2. Point force on beam

| Name | Member | System | Value - F [kN] | Pos x | Coor | Rep (n) |
|------|-----------------|--------|----------------|-------|------------|-----------|
| | Load case | Dir | Type | | Orig | Regularly |
| Fb1 | B1 | GCS | -10,0000 | 0.000 | Rela | 1 |
| | LC2 - permanent | Z | Force | | From start | |
| Fb2 | B1 | GCS | -10,0000 | 0.500 | Rela | 1 |
| | LC2 - permanent | Z | Force | | From start | |
| Fb3 | B1 | GCS | -10,0000 | 1.000 | Rela | 1 |
| | LC2 - permanent | Z | Force | | From start | |

4. RESULTS

4.1. 1D internal forces

Linear calculation

Load case: LC2

Coordinate system: Principal

Extreme 1D: Global

Selection: All

Filter: Cross-section = CS2 - Rectangulaire plein (186; 186)

Selected sections: Inputted

| Name | dx [m] | Case | Cross-section | N [kN] | V _y [kN] | V _z [kN] | M _x [kNm] | M _y [kNm] | M _z [kNm] |
|------|--------|------|--------------------------------------|---------------|---------------------|---------------------|----------------------|----------------------|----------------------|
| B1 | 2,484+ | LC2 | CS2 - Rectangulaire plein (186; 186) | 0,0000 | 0,0000 | -4,7026 | 0,0000 | -5,7567 | 0,0000 |
| B1 | 2,484- | LC2 | CS2 - Rectangulaire plein (186; 186) | 0,0000 | 0,0000 | 4,7026 | 0,0000 | -5,7567 | 0,0000 |

4.2. 1D internal forces; M_y

Valeur: M_y

Calcul linéaire

Cas de charge: LC2

Système de coordonnées: Principal

Extrême 1D: Local

Sélection: Tout



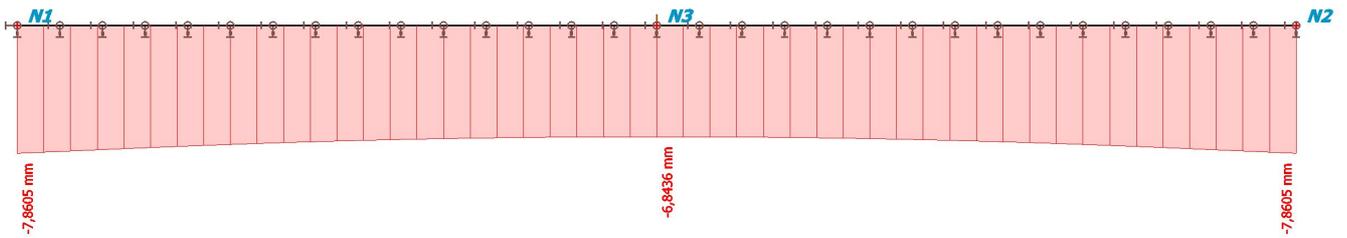
4.3. Displacement of nodes

Linear calculation
Load case: LC2
Extreme: Global
Selection: N1, N3

| Name | Case | U _x [mm] | U _y [mm] | U _z [mm] | Φ _x [mrad] | Φ _y [mrad] | Φ _z [mrad] | U _{total} [mm] |
|------|------|------------------------|------------------------|------------------------|--------------------------|--------------------------|--------------------------|----------------------------|
| N3 | LC2 | 0,0000 | 0,0000 | -6,8436 | 0,000 | 0,000 | 0,000 | 6,8436 |
| N1 | LC2 | 0,0000 | 0,0000 | -7,8605 | 0,000 | -0,705 | 0,000 | 7,8605 |

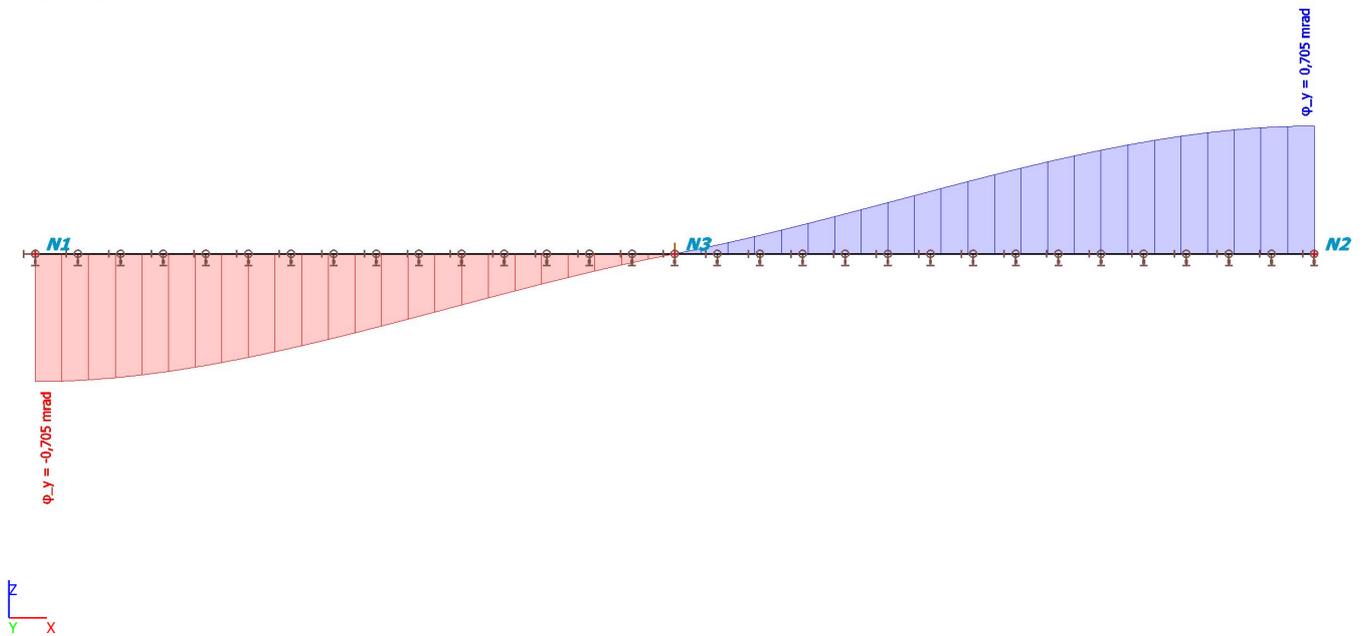
4.4. 1D deformations; u_z

Valeur: u_z
Calcul linéaire
Cas de charge: LC2
Système de coordonnées: Global
Extrême 1D: Local
Sélection: Tout



4.5. 1D deformations; φ_y

Valeur: φ_y
Calcul linéaire
Cas de charge: LC2
Système de coordonnées: Global
Extrême 1D: Local
Sélection: Tout



5. EXPECTED AFNOR RESULTS

Moment M_y in node N3=5,759 KN.m

Vertical displacement in node N3 = -6,844mm

Vertical displacement in node N1= -7,854mm

Rotation R_y in node N1=0,706mrad

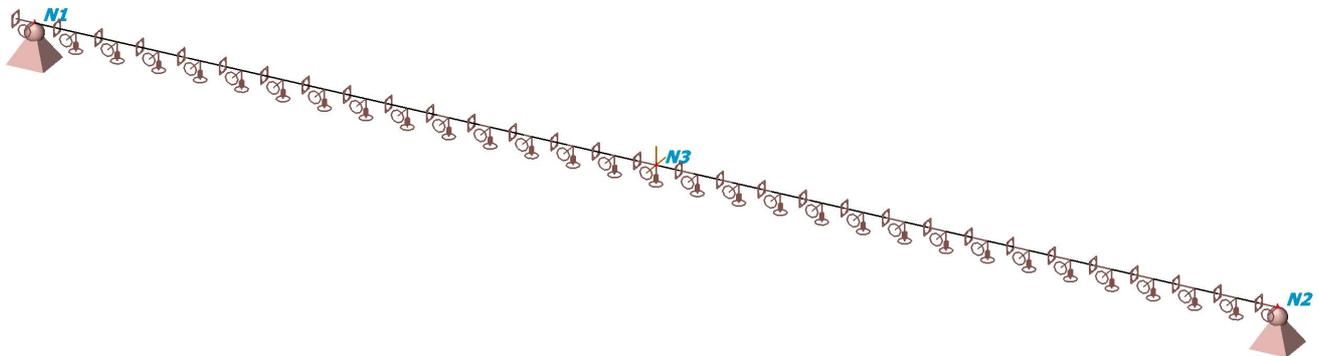
REFERENCE : "Guide de validation des progiciels de calcul de structures" AFNOR, 1990

1. TESTCASE DESCRIPTION

Simple beam on bidirectional, elastic foundation (Winkler's foundation)
elastic, linear, isotropic material

2. MODEL

2.1. Analysis model



2.2. Nodes

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] | Member | Data |
|------|-------------|-------------|-------------|--------|------|
| N1 | 0,000 | 0,000 | 0,000 | B1 | Sn1 |
| N2 | 4,967 | 0,000 | 0,000 | B1 | Sn2 |
| N3 | 2,484 | 0,000 | 0,000 | B1 | |

2.3. Members

| Name | Cross-section | Material | Length [m] | Beg. node | End node | Type |
|------|--------------------------------------|----------|------------|-----------|----------|-------------|
| B1 | CS1 - Rectangulaire plein (186; 186) | S 235 | 4,967 | N1 | N2 | general (0) |

2.4. Nodal supports

| Name | Node | System | Type | X | Y | Z | Rx | Ry | Rz |
|------|------|--------|----------|-------|-------|-------|------|------|------|
| Sn1 | N1 | GCS | Standard | Rigid | Rigid | Rigid | Free | Free | Free |
| Sn2 | N2 | GCS | Standard | Rigid | Rigid | Rigid | Free | Free | Free |

2.5. Materials

Steel EC3

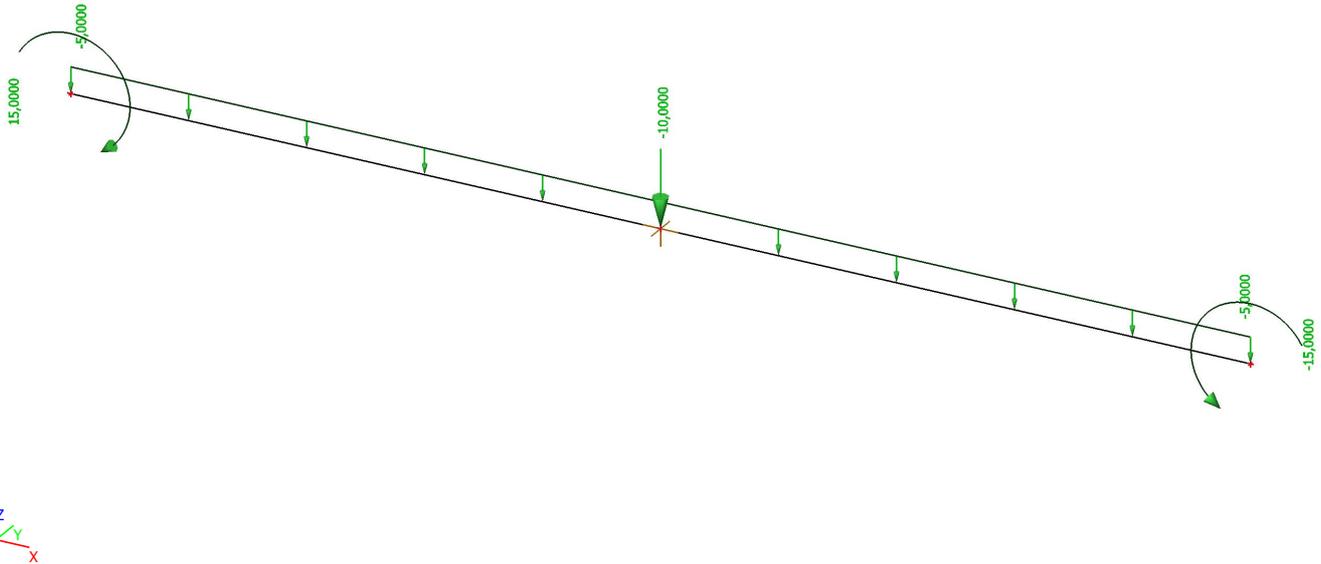
| Name | ρ [kg/m ³] | E_{mod} [MPa] | μ | Limit inférieure [mm] | Limite supérieure [mm] | F_y [MPa] | F_u [MPa] | Colour |
|-------|-----------------------------|-----------------|-----------------|-----------------------|------------------------|-------------|-------------|--------|
| | | G_{mod} [MPa] | α [m/mK] | | | | | |
| S 235 | 7850,00 | 2,1000e+05 | 0.3 | 0 | 40 | 235,0 | 360,0 | ■ |
| | | 8,0769e+04 | 0,01e-003 | 40 | 80 | 215,0 | 360,0 | |

2.6. Cross-sections

| CS1 | | |
|--|------------------------------|------------|
| Type | Rectangulaire plein | |
| Detailed | 186; 186 | |
| Formcode | 7 - Full rectangular section | |
| Item material | S 235 | |
| A [m ²] | 3,4641e-02 | |
| A _y [m ²], A _z [m ²] | 2,8868e-02 | 2,8868e-02 |
| A _L [m ² /m], A _D [m ² /m] | 7,4448e-01 | 7,4448e-01 |
| c _{y,UCS} [mm], c _{z,UCS} [mm] | 93 | 93 |
| α [deg] | 0,00 | |
| I _y [m ⁴], I _z [m ⁴] | 1,0000e-04 | 1,0000e-04 |
| i _y [mm], i _z [mm] | 54 | 54 |
| W _{el,y} [m ³], W _{el,z} [m ³] | 1,0746e-03 | 1,0746e-03 |
| W _{pl,y} [m ³], W _{pl,z} [m ³] | 1,6119e-03 | 1,6119e-03 |
| M _{pl,y,+} [Nm], M _{pl,y,-} [Nm] | 378785,90 | 378785,90 |
| M _{pl,z,+} [Nm], M _{pl,z,-} [Nm] | 378785,90 | 378785,90 |
| d _y [mm], d _z [mm] | 0 | 0 |
| I _t [m ⁴], I _w [m ⁶] | 1,6888e-04 | 0,0000e+00 |
| β _y [mm], β _z [mm] | 0 | 0 |
| Picture | | |

3. LOAD

3.1. LC2 / Tot. value



3.2. Point force on beam

| Name | Member | System | Value - F [kN] | Pos x | Coor | Rep (n) |
|------|-----------------|--------|----------------|-------|------------|-----------|
| | Load case | Dir | Type | | Orig | Regularly |
| Fb1 | B1 | GCS | -10,000 | 0.500 | Rela | 1 |
| | LC2 - Permanent | Z | Force | | From start | |

3.3. Moment on beam

| Name | Member | System | Value - M [kNm] | Pos x | Coor | Rep (n) |
|------|-----------------|--------|-----------------|-------|------------|---------|
| | Load case | Dir | Type | | Orig | dx |
| M1 | B1 | LCS | 15,000 | 0.000 | Rela | 1 |
| | LC2 - Permanent | My | Moment | | From start | |
| M2 | B1 | LCS | -15,000 | 1.000 | Rela | 1 |
| | LC2 - Permanent | My | Moment | | From start | |

3.4. Line force

| Name | Member | Type | Dir | Value - P ₁ [kN/m] | Pos x ₁ | Coor | Orig | Ecc ey [m] |
|------|-----------------|--------|--------------|-------------------------------|--------------------|--------|------------|------------|
| | Load case | System | Distribution | Value - P ₂ [kN/m] | Pos x ₂ | Loc | | Ecc ez [m] |
| LF1 | B1 | Force | Z | -5,000 | 0.000 | Rela | From start | 0,000 |
| | LC2 - Permanent | LCS | Uniform | | 1.000 | Length | | 0,000 |

4. RESULTS

4.1. Displacement of nodes

Linear calculation
Load case: LC2
Extreme: Global
Selection: N1, N3

| Name | Case | U _x [mm] | U _y [mm] | U _z [mm] | Φ _x [mrad] | Φ _y [mrad] | Φ _z [mrad] | U _{total} [mm] |
|------|------|------------------------|------------------------|------------------------|--------------------------|--------------------------|--------------------------|----------------------------|
| N3 | LC2 | 0,000 | 0,000 | -4,233 | 0,0 | 0,0 | 0,0 | 4,233 |
| N1 | LC2 | 0,000 | 0,000 | 0,000 | 0,0 | 3,0 | 0,0 | 0,000 |

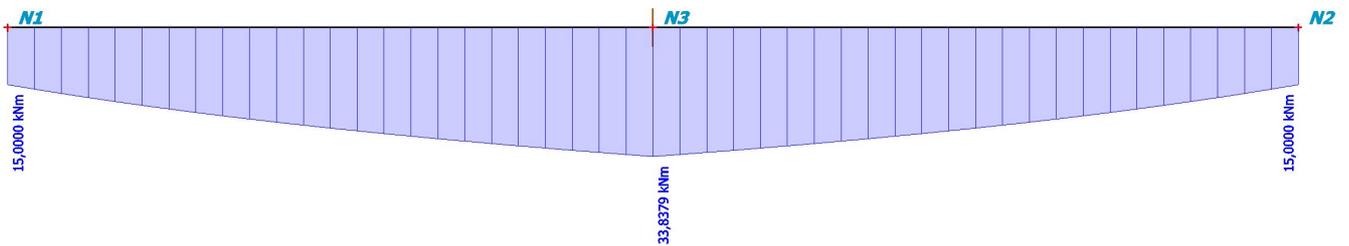
4.2. 1D internal forces

Linear calculation
Load case: LC2
Coordinate system: Principal
Extreme 1D: Global
Selection: B1
Filter: Cross-section = CS1 - Rectangulaire plein (186; 186)
Selected sections: Inputted

| Name | dx [m] | Case | Cross-section | N [kN] | V _y [kN] | V _z [kN] | M _x [kNm] | M _y [kNm] | M _z [kNm] |
|------|-----------|------|--------------------------------------|-----------|------------------------|------------------------|-------------------------|-------------------------|-------------------------|
| B1 | 2,484+ | LC2 | CS1 - Rectangulaire plein (186; 186) | 0,0000 | 0,0000 | -5,0747 | 0,0000 | 33,8379 | 0,0000 |
| B1 | 2,484- | LC2 | CS1 - Rectangulaire plein (186; 186) | 0,0000 | 0,0000 | 5,0747 | 0,0000 | 33,8379 | 0,0000 |

4.3. 1D internal forces; M_y

Valeur: M_y
Calcul linéaire
Cas de charge: LC2
Système de coordonnées: Principal
Extrême 1D: Local
Sélection: Tout



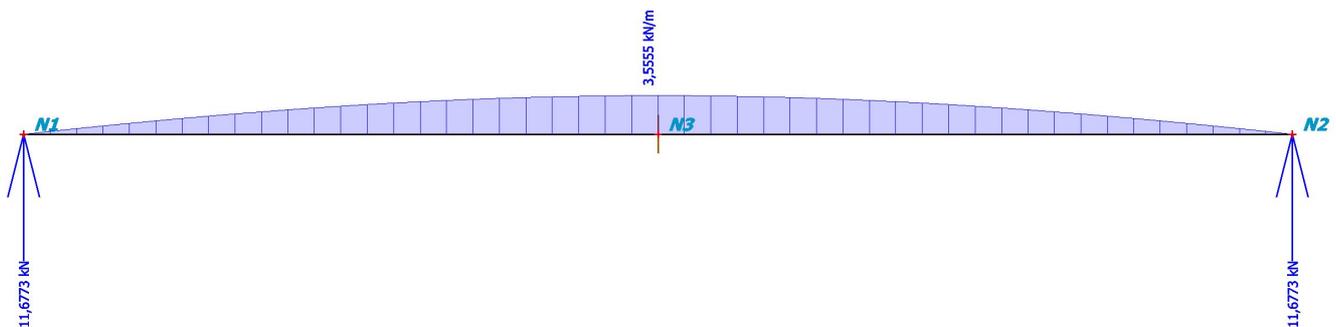
4.4. Reactions

Linear calculation
Load case: LC2
System: Global
Extreme: Global
Selection: Sn1
Nodal reactions

| Name | Case | R _x [kN] | R _y [kN] | R _z [kN] | M _x [kNm] | M _y [kNm] | M _z [kNm] | e _x [mm] | e _y [mm] | E/W/N |
|--------|------|------------------------|------------------------|------------------------|-------------------------|-------------------------|-------------------------|------------------------|------------------------|--------------|
| Sn1/N1 | LC2 | 0,0000 | 0,0000 | 11,6773 | 0,0000 | 0,0000 | 0,0000 | 0,000 | 0,000 | N_RES_OVER01 |

4.5. Reactions; R_z

Valeur: R_z
Calcul linéaire
Cas de charge: LC2
Système: Global
Extrême: Global
Sélection: Tout



5. EXPECTED AFNOR RESULTS

Rotation Ry in node N1 = -3,045 mrad

Displacement uz in node N3 = -4,23326mm

Moment My in node N3 = -33,84N.m

Vertical reaction in node N1 = 11,674KN

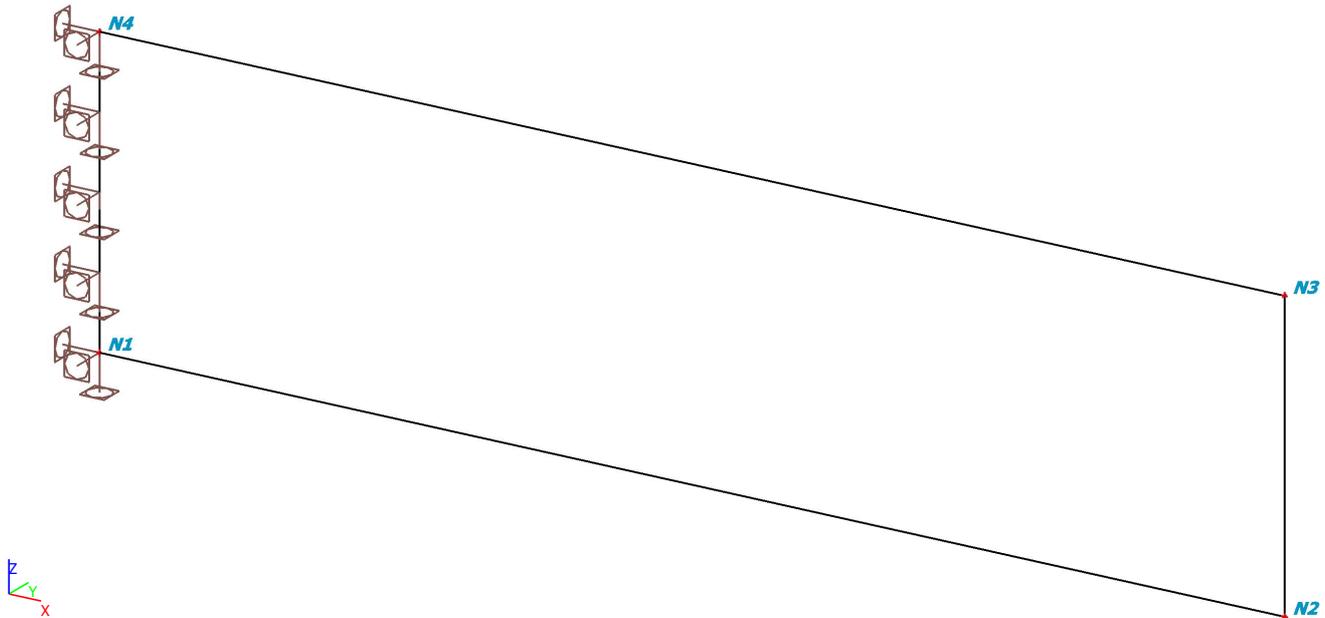
REFERENCE : "Guide de validation des progiciels de calcul de structures" AFNOR, 1990

1. TESTCASE DESCRIPTION

Rectangular membrane under in-plane shear
Specification: Rectangular shell: in-plane bending and shear.

2. MODEL

2.1. Analysis model



2.2. 2D members

| Name | Layer | Type | Element type | Material | Thickness type | Th. [mm] |
|------|---------|------------|--------------|----------|----------------|----------|
| D1 | Calque1 | dalle (90) | Standard | S 235 | constant | 1 |

2.3. Supports on 2D member edge

| Name | 2D member Edge | Orig Coor | Pos x ₁ Pos x ₂ | X | Y | Z | Rx | Ry | Rz |
|------|----------------|--------------------|---------------------------------------|-------|-------|-------|-------|-------|-------|
| Sle1 | D1 4 | From start Rela | 0.000 1.000 | Rigid | Rigid | Rigid | Rigid | Rigid | Rigid |

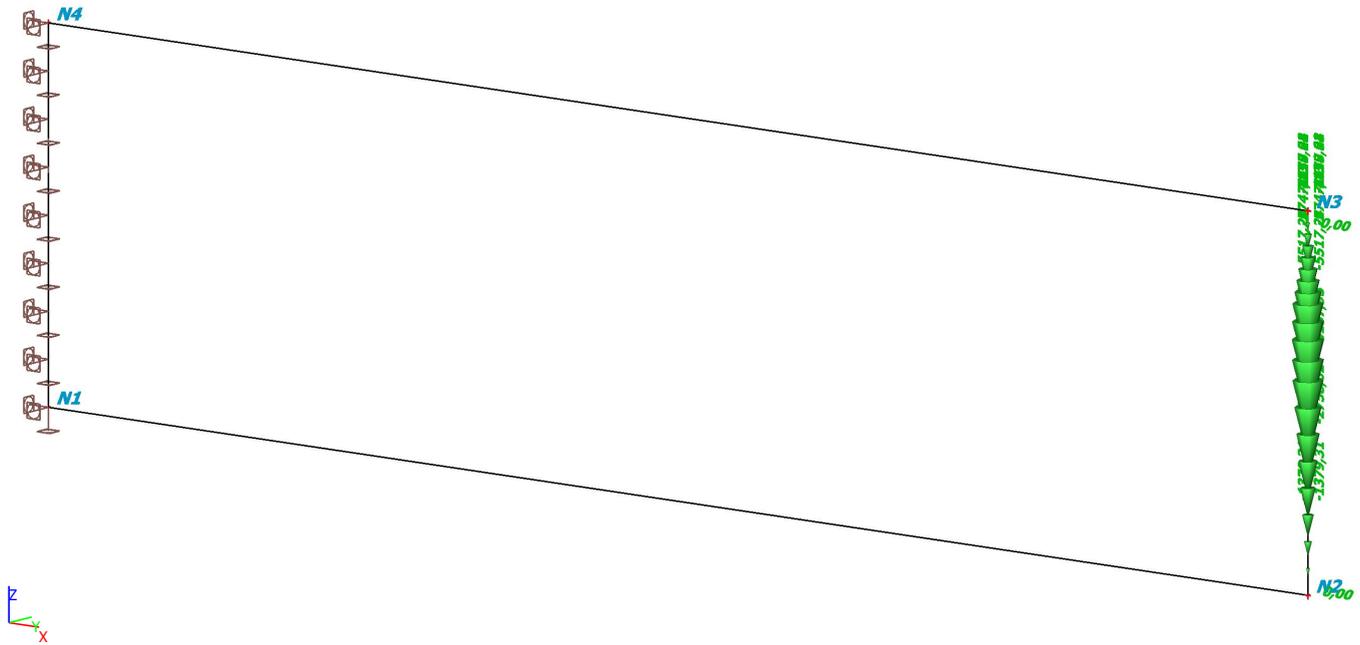
2.4. Materials

Steel EC3

| Name | ρ [kg/m ³] | E_{mod} [MPa] G_{mod} [MPa] | μ α [m/mK] | Limit inférieure [mm] | Limite supérieure [mm] | F_y [MPa] | F_u [MPa] | Colour |
|-------|-----------------------------|------------------------------------|--------------------------|-----------------------|------------------------|----------------|----------------|--------------------------------------|
| S 235 | 7850,00 | 3,0000e+04 1,2000e+04 | 0.25 0,01e-003 | 0 40 | 40 80 | 235,0 215,0 | 360,0 360,0 | ■ |

3. LOAD

3.1. LC1 / Tot. value



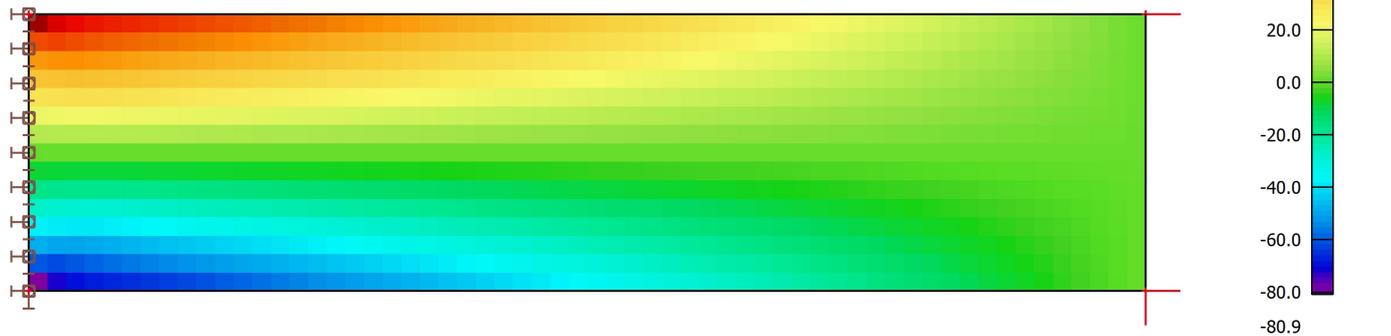
3.2. Line force on 2D member edge

| Name | 2D member | Type | Dir | Value - P ₁ | Pos x ₁ | Loc | Edge |
|-------|-----------------|--------|--------------|------------------------|--------------------|--------|------------|
| | Load case | System | Distribution | Value - P ₂ | Pos x ₂ | Coor | Orig |
| LFS2 | D1 | Force | Z | -1379,31 | 0.100 | Length | 2 |
| | LC2 - Permanent | GCS | Trapez | -2758,62 | 0.200 | Rela | From start |
| LFS3 | D1 | Force | Z | -2758,62 | 0.200 | Length | 2 |
| | LC2 - Permanent | GCS | Trapez | -4137,93 | 0.300 | Rela | From start |
| LFS4 | D1 | Force | Z | -4137,93 | 0.300 | Length | 2 |
| | LC2 - Permanent | GCS | Trapez | -5517,24 | 0.400 | Rela | From start |
| LFS5 | D1 | Force | Z | -5517,24 | 0.400 | Length | 2 |
| | LC2 - Permanent | GCS | Trapez | -5747,13 | 0.500 | Rela | From start |
| LFS7 | D1 | Force | Z | -1379,31 | 0.100 | Length | 2 |
| | LC2 - Permanent | GCS | Trapez | -2758,62 | 0.200 | Rela | From end |
| LFS8 | D1 | Force | Z | -2758,62 | 0.200 | Length | 2 |
| | LC2 - Permanent | GCS | Trapez | -4137,93 | 0.300 | Rela | From end |
| LFS9 | D1 | Force | Z | -4137,93 | 0.300 | Length | 2 |
| | LC2 - Permanent | GCS | Trapez | -5517,24 | 0.400 | Rela | From end |
| LFS10 | D1 | Force | Z | -5517,24 | 0.400 | Length | 2 |
| | LC2 - Permanent | GCS | Trapez | -5747,13 | 0.500 | Rela | From end |
| LFS20 | D1 | Force | Z | 0,00 | 0.000 | Length | 2 |
| | LC2 - Permanent | GCS | Trapez | -1379,31 | 0.100 | Rela | From start |
| LFS21 | D1 | Force | Z | 0,00 | 0.000 | Length | 2 |
| | LC2 - Permanent | GCS | Trapez | -1379,31 | 0.100 | Rela | From end |

4. RESULTS

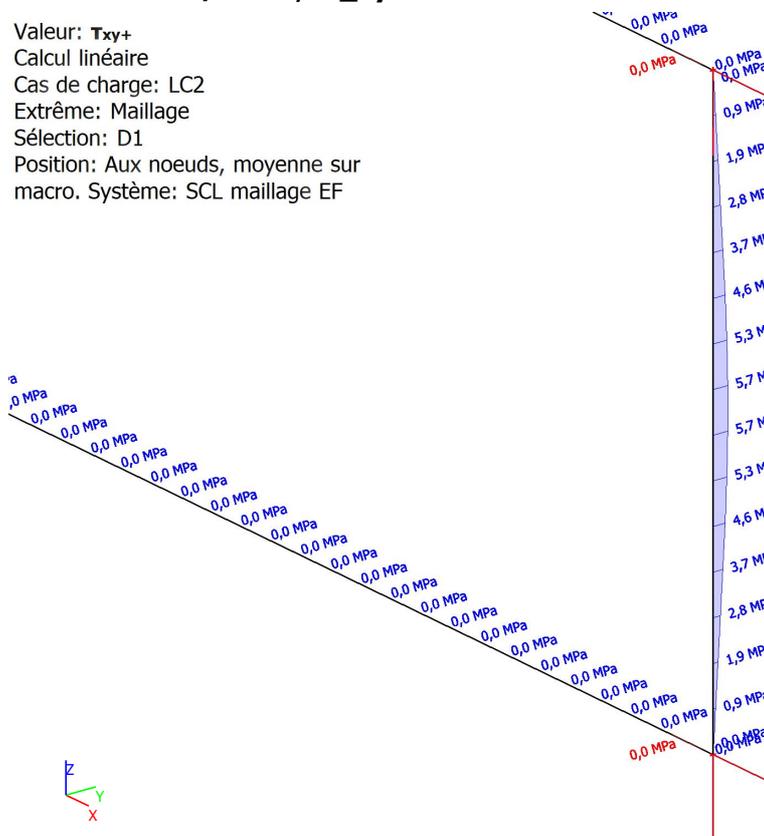
4.1. 2D stress/strain; σ_{x+}

Valeur: σ_{x+}
 Calcul linéaire
 Cas de charge: LC2
 Extrême: Maillage
 Sélection: Tout
 Position: Aux centres. Système: SCL
 maillage EF



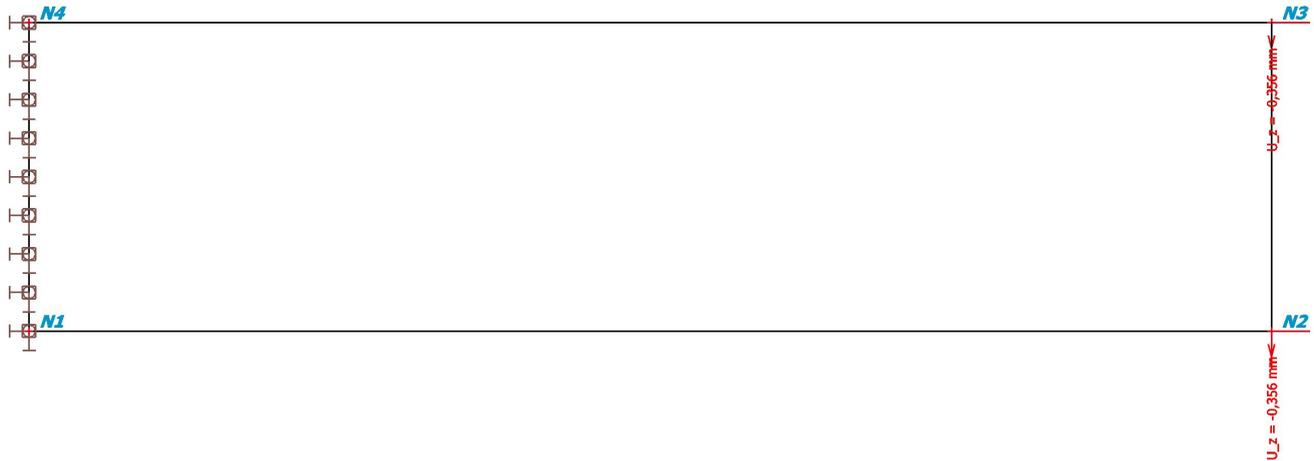
4.2. 2D stress/strain; τ_{xy+}

Valeur: τ_{xy+}
 Calcul linéaire
 Cas de charge: LC2
 Extrême: Maillage
 Sélection: D1
 Position: Aux noeuds, moyenne sur
 macro. Système: SCL maillage EF



4.3. Displacement of nodes; U_z

Valeur: U_z
Calcul linéaire
Cas de charge: LC2
Extrême: Global
Sélection: N2, N3



4.4. Displacement of nodes

Linear calculation
Load case: LC2
Extreme: Global
Selection: N2, N3

| Name | Case | U _x [mm] | U _y [mm] | U _z [mm] | Φ _x [mrad] | Φ _y [mrad] | Φ _z [mrad] | U _{total} [mm] |
|------|------|------------------------|------------------------|------------------------|--------------------------|--------------------------|--------------------------|----------------------------|
| N3 | LC2 | 0,064 | 0,000 | -0,356 | 0,0 | 10,9 | 0,0 | 0,361 |
| N2 | LC2 | -0,064 | 0,000 | -0,356 | 0,0 | 10,9 | 0,0 | 0,361 |

5. EXPECTED AFNOR RESULTS

Max vertical displacement at free end = 0,3573 mm

Max sigmaX stress at fixed end = 80 MPa

Max sigmaXY stress at free end = 5 Mpa

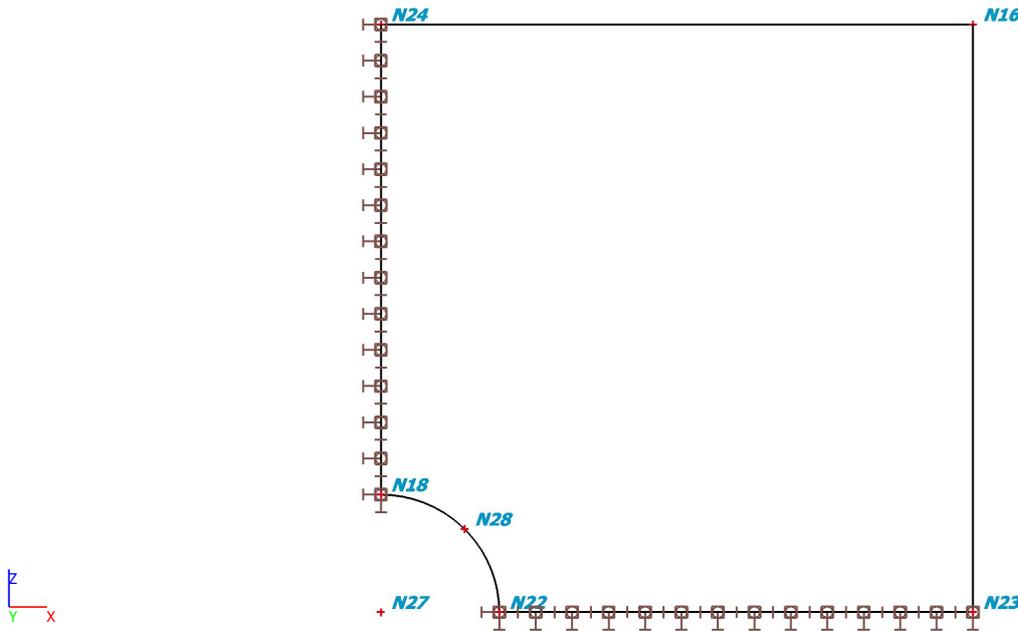
REFERENCE : "Guide de validation des progiciels de calcul de structures" AFNOR, 1990

1. TESTCASE DESCRIPTION

Tension of perforated membrane
Specification: Simple tension of perforated membrane.

2. MODEL

2.1. Analysis model



2.2. 2D members

| Name | Layer | Type | Element type | Material | Thickness type | Th. [mm] |
|------|---------|------------|--------------|----------|----------------|----------|
| D5 | Calque1 | dalle (90) | Standard | S 235 | constant | 1 |

2.3. Supports on 2D member edge

| Name | Edge | Orig Coor | Pos x ₁ Pos x ₂ | X | Y | Z | Rx | Ry | Rz |
|------|------|--------------------|--|-------|-------|-------|-------|-------|-------|
| Sle8 | 1 | From start Rela | 0.000 1.000 | Free | Rigid | Rigid | Rigid | Rigid | Rigid |
| Sle9 | 1 | From start Rela | 0.000 1.000 | Rigid | Rigid | Free | Rigid | Rigid | Rigid |

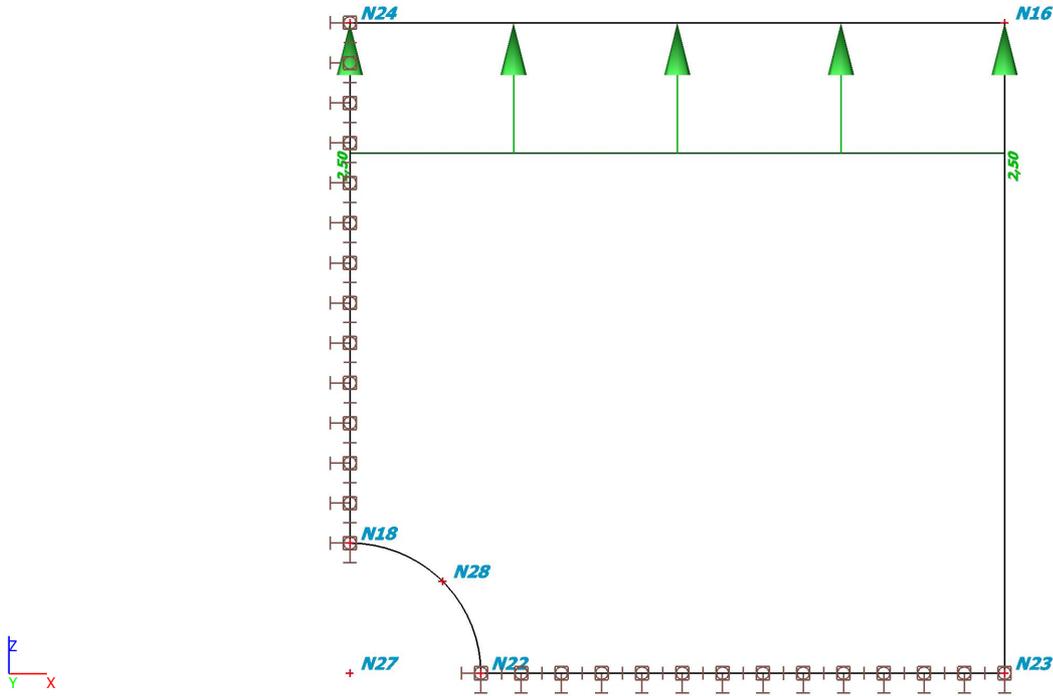
2.4. Materials

Steel EC3

| Name | ρ [kg/m ³] | E_{mod} [MPa] G_{mod} [MPa] | μ α [m/mK] | Limit inférieure [mm] | Limite supérieure [mm] | F_y [N/mm ²] | F_u [N/mm ²] | Colour |
|-------|-----------------------------|------------------------------------|--------------------------|-----------------------|------------------------|----------------------------|----------------------------|--------------------------------------|
| S 235 | 7850,00 | 3,0000e+04 1,2000e+04 | 0,25 0,01e-003 | 0 40 | 40 80 | 235,0 215,0 | 360,0 360,0 | ■ |

3. LOAD

3.1. LC1 / Tot. value



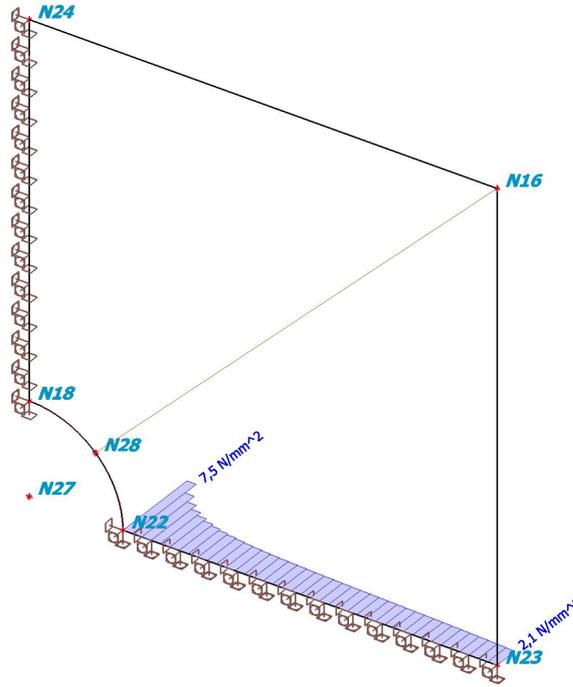
3.2. Line force on 2D member edge

| Name | 2D member | Type | Dir | Value - P ₁ [N/mm] | Pos x ₁ | Loc | Edge |
|------|-----------------|--------|--------------|----------------------------------|--------------------|--------|----------|
| | Load case | System | Distribution | Value - P ₂ [N/mm] | Pos x ₂ | Coor | Orig |
| LFS3 | D5 | Force | Z | 2,50 | 0.000 | Length | 2 |
| | LC2 - Permanent | GCS | Uniform | | 1.000 | Rela | From end |

4. RESULTS

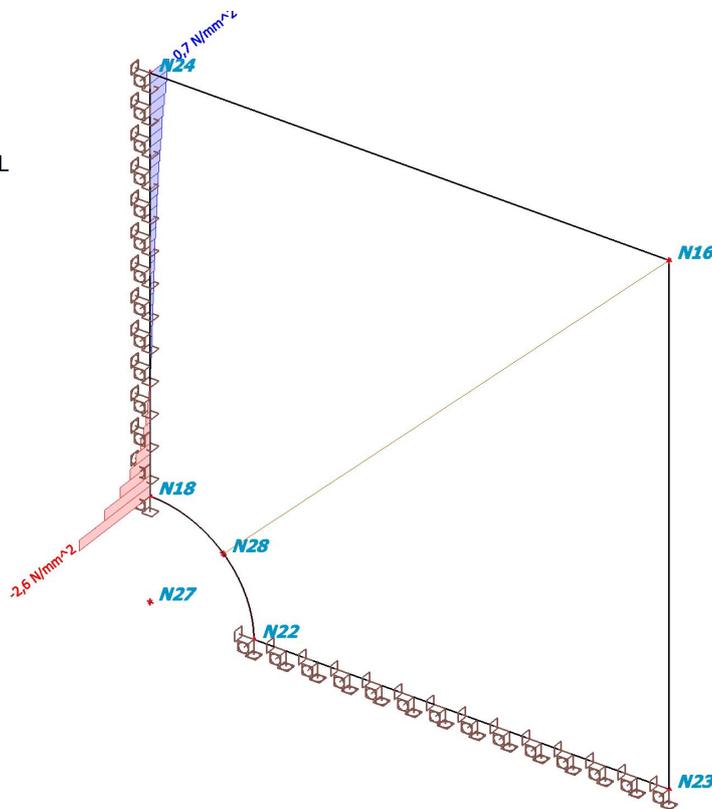
4.1. 3D Stress (a,0)

Valeur: σ_{1+}
 Calcul linéaire
 Cas de charge: LC2
 Extrême: Elément
 Sélection: SE7
 Position: Aux centres. Système: SCL
 maillage EF



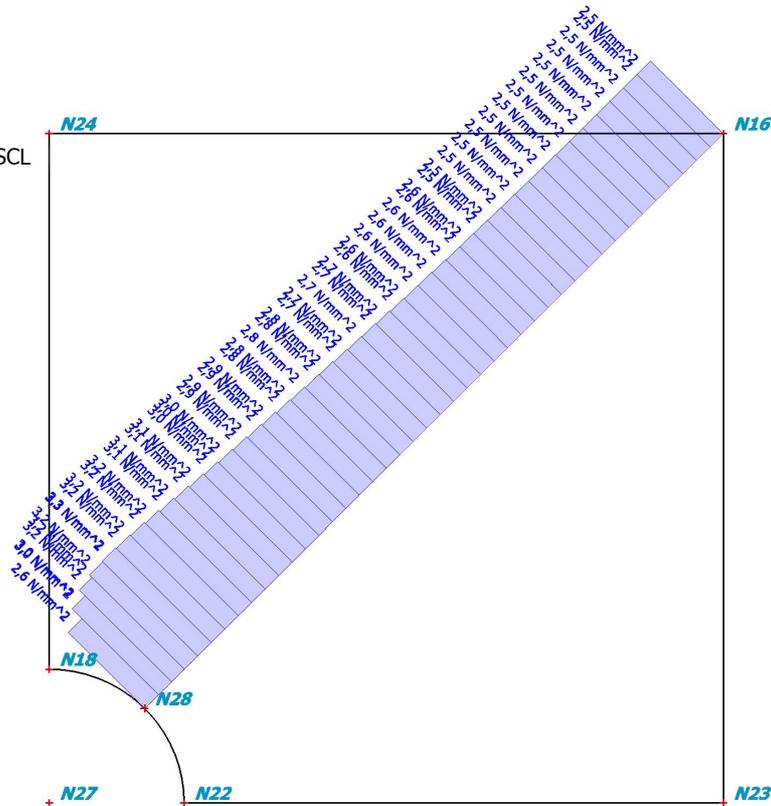
4.2. 3D Stress (a,pi/2)

Valeur: σ_{2+}
 Calcul linéaire
 Cas de charge: LC2
 Extrême: Elément
 Sélection: SE8
 Position: Aux centres. Système: SCL
 maillage EF



4.3. 3D stress (a, pi/4)

Valeur: σ_{1+}
 Calcul linéaire
 Cas de charge: LC2
 Extrême: Maillage
 Sélection: SE6
 Position: Aux centres. Système: SCL
 maillage EF



4.4. 2D stress/strain

Linear calculation
 Load case: LC2
 Extreme: Global
 Selection: SE7, SE8
 Location: In centres. System: LCS mesh element

Principal stress - Results on sections and edges:

| Name | Mesh | Position [mm] | Case | σ_{1+} | σ_{2+} | σ_{E+} | $\alpha+$ | $T_{max,b}$ |
|------|---------------|----------------------------|------|----------------------------|----------------------------|--------------------------|------------------|-------------|
| | | | | [N/mm ²] | [N/mm ²] | [N/mm ²] | [deg] | |
| | | | | σ_{1-} | σ_{2-} | σ_{E-} | $\alpha-$ | |
| | | | | [N/mm ²] | [N/mm ²] | [N/mm ²] | [deg] | |
| SE8 | Element: 54 | 260,631 0,000 61,000 | LC2 | -0,1 -0,1 | -1,7 -1,7 | 1,6 1,6 | 88,74 88,74 | 0,0 |
| SE8 | Element: 30 | 260,631 0,000 60,000 | LC2 | -0,1 -0,1 | -2,6 -2,6 | 2,5 2,5 | -88,31 -88,31 | 0,0 |
| SE7 | Element: 2257 | 273,631 0,000 50,000 | LC2 | 4,7 4,7 | 1,0 1,0 | 4,3 4,3 | 89,86 89,86 | 0,0 |
| SE8 | Element: 2426 | 260,631 0,000 64,000 | LC2 | 0,4 0,4 | -0,5 -0,5 | 0,8 0,8 | 83,63 83,63 | 0,0 |
| SE7 | Element: 50 | 270,631 0,000 50,000 | LC2 | 7,5 7,5 | 0,3 0,3 | 7,3 7,3 | 87,59 87,59 | 0,0 |

5. EXPECTED AFNOR RESULTS

For (a,0) (Node N22):

Sigma = 7,5 Mpa

For (a,PI/4) (Node N18):

Sigma = 2,5 Mpa

For (a,PI/2) (Node N28):

Sigma = -2,5 Mpa

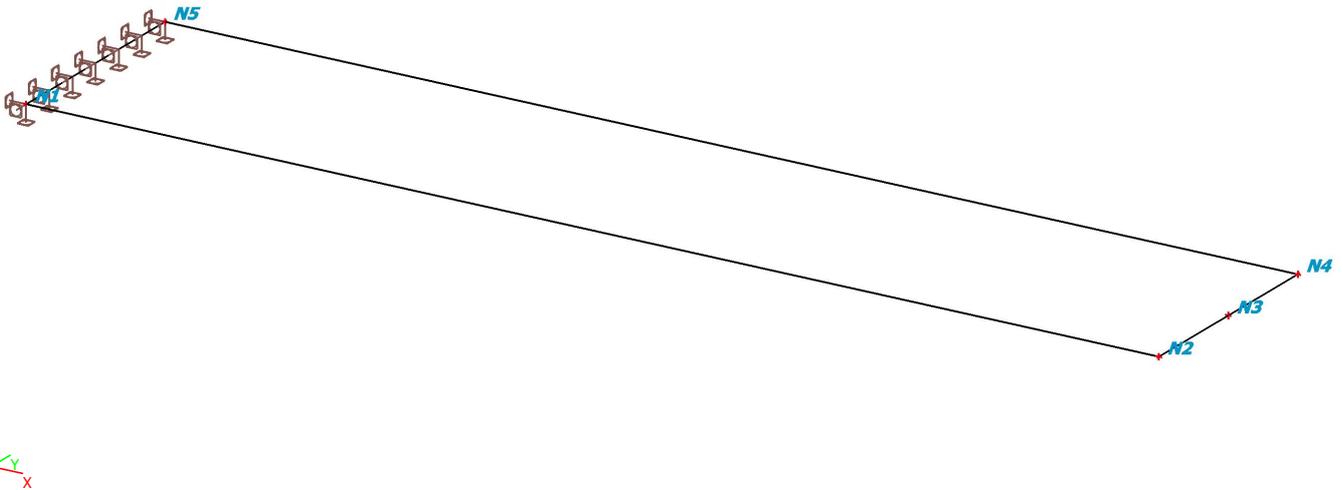
REFERENCE : "Guide de validation des progiciels de calcul de structures" AFNOR, 1990

1. TESTCASE DESCRIPTION

Cantilever slab under uniform pressure

2. MODEL

2.1. Analysis model



2.2. 2D members

| Name | Layer | Type | Element type | Material | Thickness type | Th. [mm] |
|------|---------|------------|--------------|----------|----------------|----------|
| D1 | Calque1 | dalle (90) | Standard | S 235 | constant | 5 |

2.3. Nodes

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] |
|------|-------------|-------------|-------------|
| N1 | 0,000 | 0,000 | 0,000 |
| N2 | 1,000 | 0,000 | 0,000 |

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] |
|------|-------------|-------------|-------------|
| N3 | 1,000 | 0,100 | 0,000 |
| N4 | 1,000 | 0,200 | 0,000 |

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] |
|------|-------------|-------------|-------------|
| N5 | 0,000 | 0,200 | 0,000 |

2.4. Supports on 2D member edge

| Name | 2D member Edge | Orig Coor | Pos x ₁ Pos x ₂ | X | Y | Z | Rx | Ry | Rz |
|------|----------------|------------|---------------------------------------|-------|-------|-------|-------|-------|-------|
| Sle1 | D1 | From start | 0.000 | Rigid | Rigid | Rigid | Rigid | Rigid | Rigid |
| | 5 | Rela | 1.000 | | | | | | |

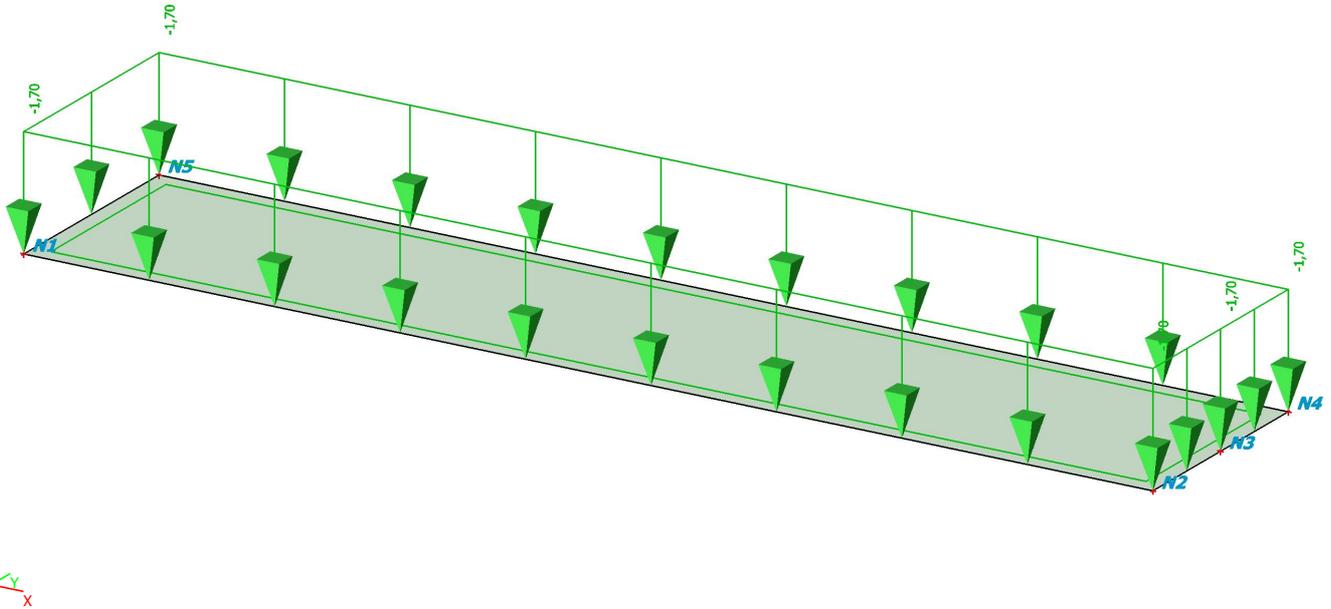
2.5. Materials

Steel EC3

| Name | ρ [kg/m ³] | E_{mod} [MPa] | μ | Limit inférieure [mm] | Limite supérieure [mm] | F_y [MPa] | F_u [MPa] | Colour |
|-------|-----------------------------|-----------------|-----------------|-----------------------|------------------------|-------------|-------------|--------|
| | | G_{mod} [MPa] | α [m/mK] | | | | | |
| S 235 | 7850,00 | 2,1000e+05 | 0.3 | 0 | 40 | 235,0 | 360,0 | ■ |
| | | 8,0769e+04 | 0,01e-003 | 40 | 80 | 215,0 | 360,0 | |

3. LOAD

3.1. LC2 / Tot. value



3.2. Surface load

| Name | Dir | Type | Value [kN/m ²] | 2D member | Load case | System | Loc |
|------|-----|-------|-------------------------------|-----------|-----------------|--------|--------|
| SF1 | Z | Force | -1,70 | D1 | LC2 - permanent | LCS | Length |

4. RESULTS

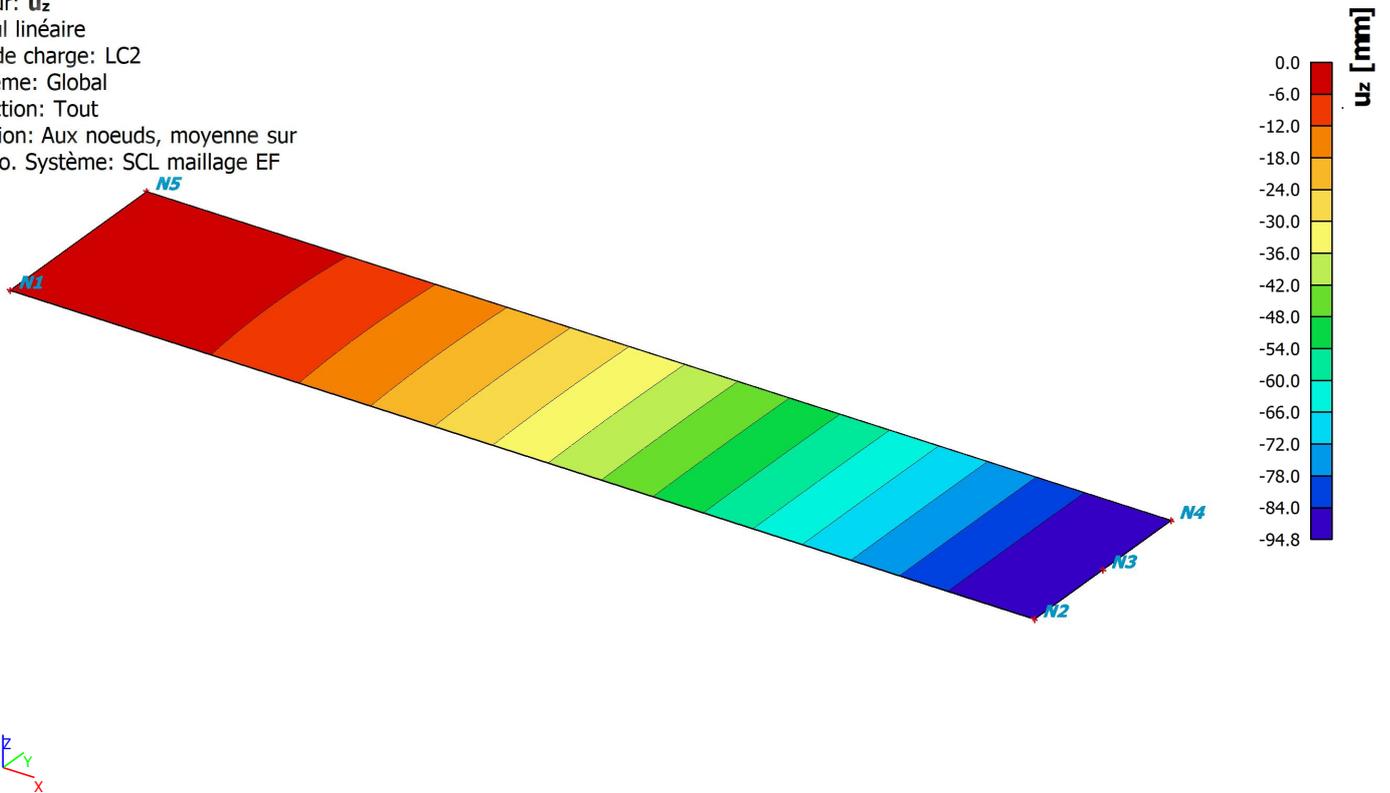
4.1. Displacement of nodes

Linear calculation
Load case: LC2
Extreme: Global
Selection: N2, N4

| Name | Case | U _x [mm] | U _y [mm] | U _z [mm] | Φ _x [mrad] | Φ _y [mrad] | Φ _z [mrad] | U _{total} [mm] |
|------|------|------------------------|------------------------|------------------------|--------------------------|--------------------------|--------------------------|----------------------------|
| N4 | LC2 | 0,0 | 0,0 | -94,8 | 0,1 | 127,1 | 0,0 | 94,8 |
| N2 | LC2 | 0,0 | 0,0 | -94,8 | -0,1 | 127,1 | 0,0 | 94,8 |

4.2. 2D displacement; u_z

Valeur: u_z
Calcul linéaire
Cas de charge: LC2
Extrême: Global
Sélection: Tout
Position: Aux noeuds, moyenne sur macro. Système: SCL maillage EF



5. EXPECTED AFNOR RESULTS

Vertical displacement uz in node N2 &N4 = -97,3 mm

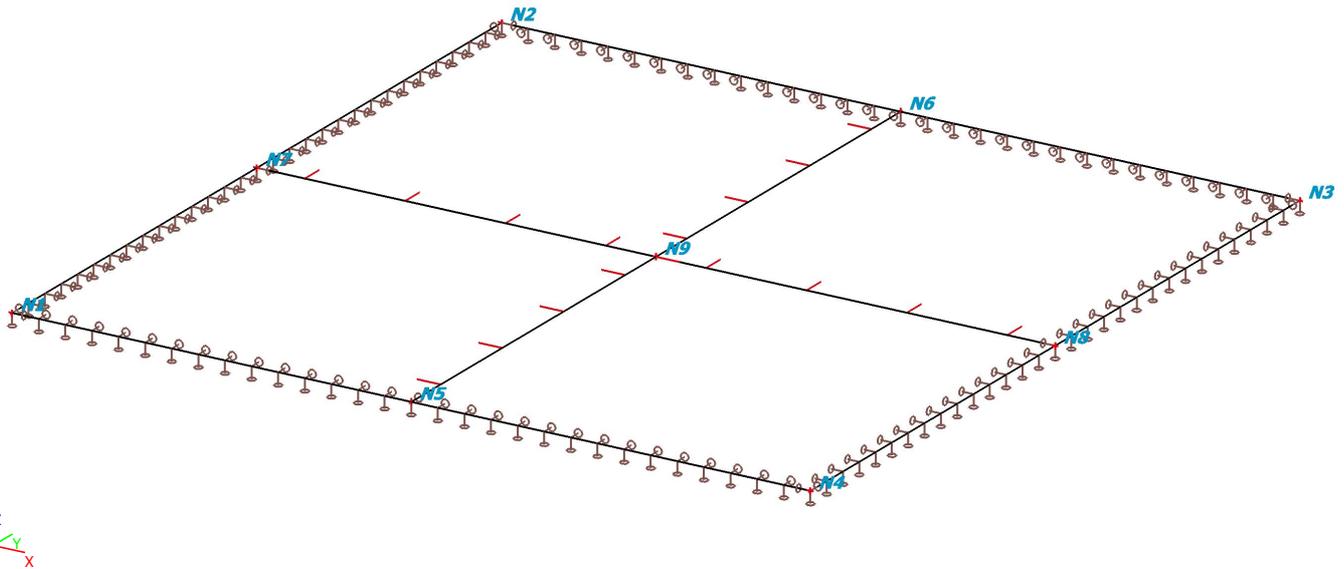
REFERENCE : "Guide de validation des progiciels de calcul de structures" AFNOR, 1990

1. TESTCASE DESCRIPTION

Simply supported square plate under self weight

2. MODEL

2.1. Analysis model



2.2. Nodes

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] |
|------|-------------|-------------|-------------|
| N1 | 0,000 | 0,000 | 0,000 |
| N2 | 0,000 | 1,000 | 0,000 |
| N3 | 1,000 | 1,000 | 0,000 |

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] |
|------|-------------|-------------|-------------|
| N4 | 1,000 | 0,000 | 0,000 |
| N5 | 0,500 | 0,000 | 0,000 |
| N6 | 0,500 | 1,000 | 0,000 |

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] |
|------|-------------|-------------|-------------|
| N7 | 0,000 | 0,500 | 0,000 |
| N8 | 1,000 | 0,500 | 0,000 |
| N9 | 0,500 | 0,500 | 0,000 |

2.3. 2D members

| Name | Layer | Type | Element type | Material | Thickness type | Th. [mm] |
|------|---------|------------|--------------|----------|----------------|----------|
| D1 | Calque1 | dalle (90) | Standard | S 235 | constant | 10 |

2.4. Supports on 2D member edge

| Name | 2D member Edge | Orig Coor | Pos x ₁ | Pos x ₂ | X | Y | Z | Rx | Ry | Rz |
|------|----------------|--------------------|--------------------|--------------------|------|-------|-------|------|------|------|
| Sle1 | D1 1 | From start Rela | 0,000 1,000 | | Free | Rigid | Rigid | Free | Free | Free |
| Sle2 | D1 2 | From start Rela | 0,000 1,000 | | Free | Rigid | Rigid | Free | Free | Free |
| Sle3 | D1 3 | From start Rela | 0,000 1,000 | | Free | Rigid | Rigid | Free | Free | Free |
| Sle4 | D1 4 | From start Rela | 0,000 1,000 | | Free | Rigid | Rigid | Free | Free | Free |

2.5. Materials

Steel EC3

| Name | ρ [kg/m ³] | E_{mod} [MPa] | μ | Limit inférieure [mm] | Limite supérieure [mm] | F_y [MPa] | F_u [MPa] | Colour |
|-------|--------------------------------|--------------------|--------------------|--------------------------|---------------------------|----------------|----------------|--------|
| | | G_{mod} [MPa] | α [m/mK] | | | | | |
| S 235 | 7950,00 | 2,1000e+05 | 0,3 | 0 | 40 | 235,0 | 360,0 | ■ |
| | | 8,0769e+04 | 0,01e-003 | 40 | 80 | 215,0 | 360,0 | |

3. RESULTS

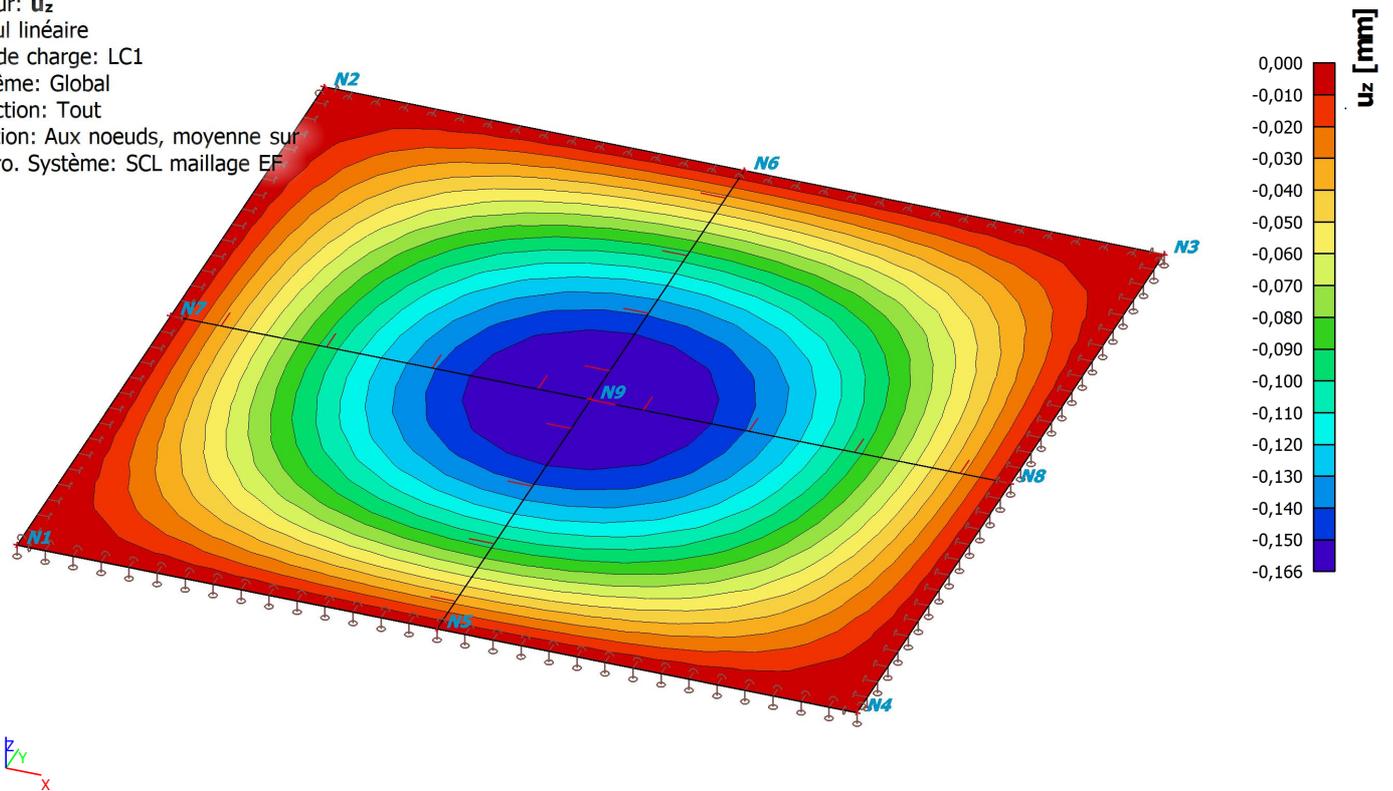
3.1. Displacement of nodes

Linear calculation
Load case: LC1
Extreme: Global
Selection: N9

| Name | Case | U _x [mm] | U _y [mm] | U _z [mm] | Φ _x [mrad] | Φ _y [mrad] | Φ _z [mrad] | U _{total} [mm] |
|------|------|------------------------|------------------------|------------------------|--------------------------|--------------------------|--------------------------|----------------------------|
| N9 | LC1 | 0,000 | 0,000 | -0,166 | 0,0 | 0,0 | 0,0 | 0,166 |

3.2. 2D displacement; u_z

Valeur: u_z
Calcul linéaire
Cas de charge: LC1
Extrême: Global
Sélection: Tout
Position: Aux noeuds, moyenne sur macro. Système: SCL maillage EF



4. EXPECTED AFNOR RESULTS

Vertical displacement uz in node N9= -0,158 mm

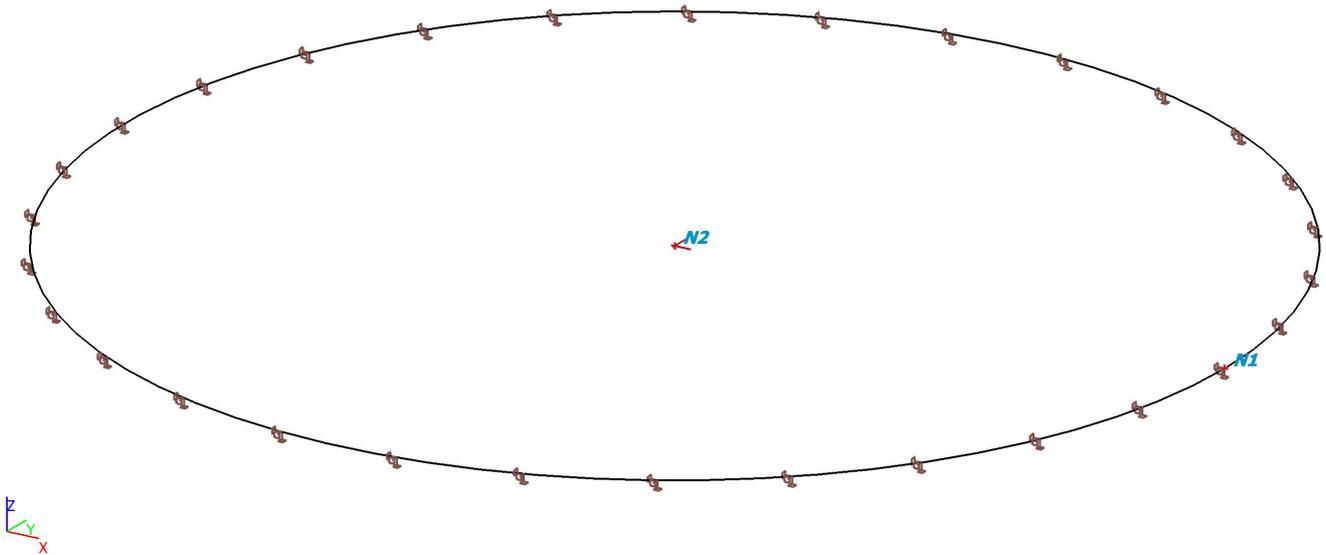
REFERENCE : "Guide de validation des progiciels de calcul de structures" AFNOR, 1990

1. TESTCASE DESCRIPTION

Circular plate with clamped edges under uniform load

2. MODEL

2.1. Analysis model



2.2. 2D members

| Name | Layer | Type | Element type | Material | Thickness type | Th. [mm] |
|------|---------|------------|--------------|----------|----------------|----------|
| D1 | Calque1 | dalle (90) | Standard | S 235 | constant | 5 |

2.3. Supports on 2D member edge

| Name | 2D member Edge | Orig Coor | Pos x ₁ Pos x ₂ | X | Y | Z | Rx | Ry | Rz |
|------|----------------|------------|---------------------------------------|-------|-------|-------|-------|-------|-------|
| Sle1 | D1 | From start | 0.000 | Rigid | Rigid | Rigid | Rigid | Rigid | Rigid |
| | 1 | Rela | 1.000 | | | | | | |

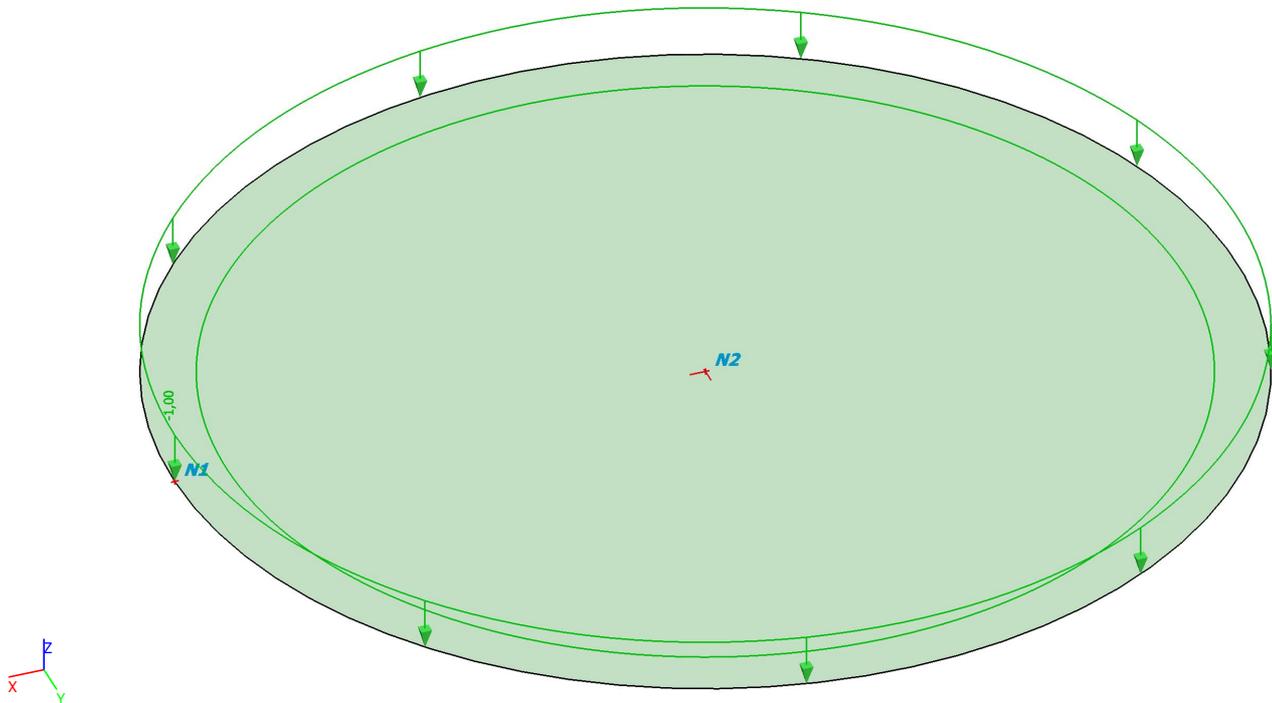
2.4. Materials

Steel EC3

| Name | ρ [kg/m ³] | E_{mod} [MPa] | μ | Limit inférieure [mm] | Limite supérieure [mm] | F_y [MPa] | F_u [MPa] | Colour |
|-------|-----------------------------|-----------------|-----------------|-----------------------|------------------------|-------------|-------------|--------|
| | | G_{mod} [MPa] | α [m/mK] | | | | | |
| S 235 | 7850,00 | 2,1000e+05 | 0.3 | 0 | 40 | 235,0 | 360,0 | ■ |
| | | 8,0769e+04 | 0,01e-003 | 40 | 80 | 215,0 | 360,0 | |

3. LOAD

3.1. LC2 / Tot. value



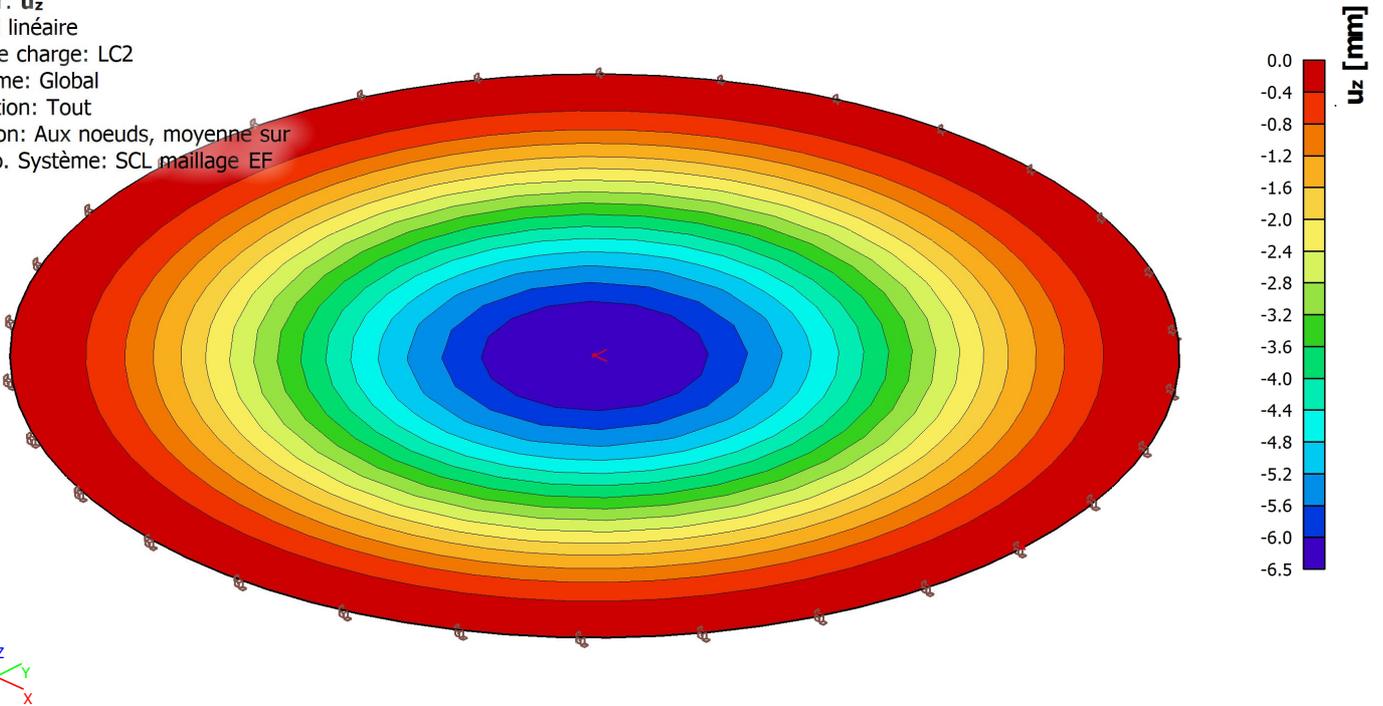
3.2. Surface load

| Name | Dir | Type | Value [kN/m ²] | 2D member | Load case | System | Loc |
|------|-----|-------|-------------------------------|-----------|-----------------|--------|--------|
| SF1 | Z | Force | -1,00 | D1 | LC2 - PERMANENT | LCS | Length |

4. RESULTS

4.1. 2D displacement; u_z

Valeur: u_z
 Calcul linéaire
 Cas de charge: LC2
 Extrême: Global
 Sélection: Tout
 Position: Aux noeuds, moyenne sur macro. Système: SCL maillage EF



4.2. Displacement of nodes

Linear calculation
 Load case: LC2
 Extreme: Global
 Selection: N2

| Name | Case | U_x [mm] | U_y [mm] | U_z [mm] | Φ_x [mrad] | Φ_y [mrad] | Φ_z [mrad] | U_{total} [mm] |
|------|------|---------------|---------------|---------------|--------------------|--------------------|--------------------|---------------------|
| N2 | LC2 | 0,0 | 0,0 | -6,5 | 0,0 | 0,0 | 0,0 | 6,5 |

5. EXPECTED AFNOR RESULTS

Vertical displacement uz in node N2 (the center) = -6,5 mm

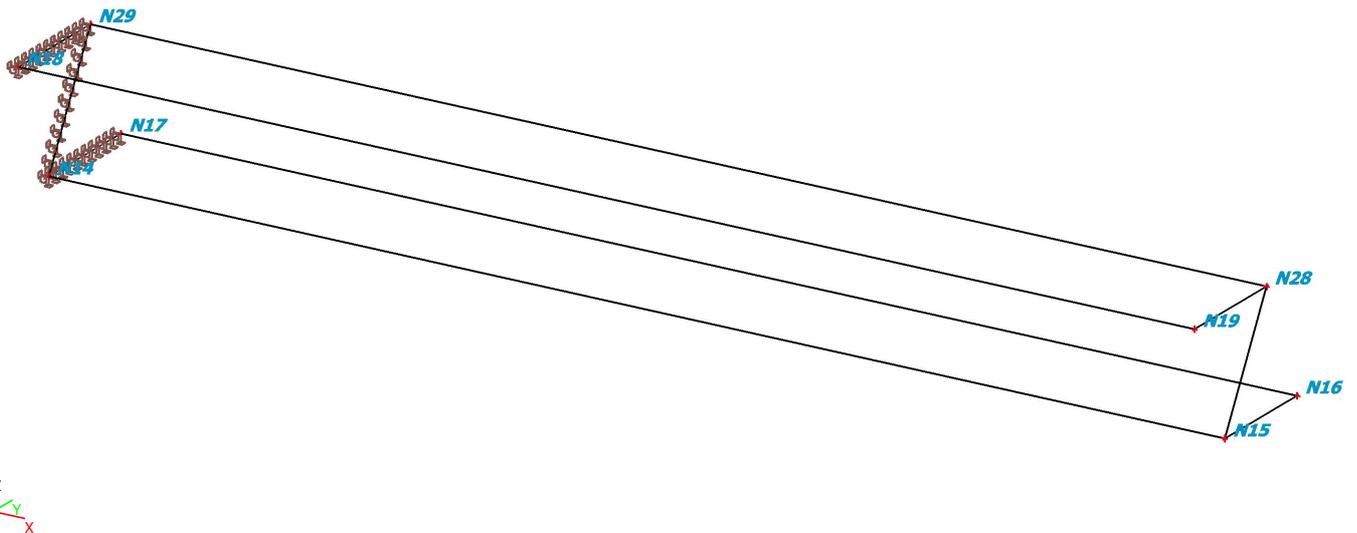
REFERENCE : "Guide de validation des progiciels de calcul de structures" AFNOR, 1990

1. TESTCASE DESCRIPTION

Beam of Z-section

2. MODEL

2.1. Analysis model



2.2. Nodes

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] |
|------|-------------|-------------|-------------|
| N14 | -3,000 | 3,000 | 0,000 |
| N15 | 7,000 | 3,000 | 0,000 |
| N16 | 7,000 | 4,000 | 0,000 |

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] |
|------|-------------|-------------|-------------|
| N17 | -3,000 | 4,000 | 0,000 |
| N18 | -3,000 | 2,577 | 1,000 |
| N19 | 7,000 | 2,577 | 1,000 |

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] |
|------|-------------|-------------|-------------|
| N28 | 7,000 | 3,577 | 1,000 |
| N29 | -3,000 | 3,577 | 1,000 |

2.3. 2D members

| Name | Layer | Type | Element type | Material | Thickness type | Th. [mm] |
|------|---------|------------|--------------|----------|----------------|----------|
| D4 | Calque1 | dalle (90) | Standard | S 235 | constant | 10 |
| D5 | Calque1 | dalle (90) | Standard | S 235 | constant | 10 |
| D6 | Calque1 | dalle (90) | Standard | S 235 | constant | 10 |

2.4. Supports on 2D member edge

| Name | 2D member Edge | Orig Coor | Pos x1 Pos x2 | X | Y | Z | Rx | Ry | Rz |
|-------|----------------|------------|---------------|-------|-------|-------|-------|-------|-------|
| Sle9 | D4 | From start | 0.000 | Rigid | Rigid | Rigid | Rigid | Rigid | Rigid |
| | 4 | Rela | 0.200 | | | | | | |
| Sle10 | D4 | From start | 0.200 | Rigid | Rigid | Rigid | Rigid | Rigid | Rigid |
| | 4 | Rela | 0.400 | | | | | | |
| Sle11 | D4 | From start | 0.400 | Rigid | Rigid | Rigid | Rigid | Rigid | Rigid |
| | 4 | Rela | 0.600 | | | | | | |
| Sle12 | D4 | From start | 0.600 | Rigid | Rigid | Rigid | Rigid | Rigid | Rigid |
| | 4 | Rela | 0.800 | | | | | | |
| Sle13 | D4 | From start | 0.800 | Rigid | Rigid | Rigid | Rigid | Rigid | Rigid |
| | 4 | Rela | 1.000 | | | | | | |
| Sle14 | D5 | From start | 0.000 | Rigid | Rigid | Rigid | Rigid | Rigid | Rigid |
| | 4 | Rela | 0.200 | | | | | | |

| Name | 2D member Edge | Orig Coor | Pos x ₁ Pos x ₂ | X | Y | Z | Rx | Ry | Rz |
|-------|-------------------|--------------------|--|-------|-------|-------|-------|-------|-------|
| Sle15 | D5 4 | From start Rela | 0.200 0.400 | Rigid | Rigid | Rigid | Rigid | Rigid | Rigid |
| Sle16 | D5 4 | From start Rela | 0.400 0.600 | Rigid | Rigid | Rigid | Rigid | Rigid | Rigid |
| Sle17 | D5 4 | From start Rela | 0.600 0.800 | Rigid | Rigid | Rigid | Rigid | Rigid | Rigid |
| Sle18 | D5 4 | From start Rela | 0.800 1.000 | Rigid | Rigid | Rigid | Rigid | Rigid | Rigid |
| Sle19 | D6 1 | From start Rela | 0.800 1.000 | Rigid | Rigid | Rigid | Rigid | Rigid | Rigid |
| Sle20 | D6 1 | From start Rela | 0.600 0.800 | Rigid | Rigid | Rigid | Rigid | Rigid | Rigid |
| Sle21 | D6 1 | From start Rela | 0.400 0.600 | Rigid | Rigid | Rigid | Rigid | Rigid | Rigid |
| Sle22 | D6 1 | From start Rela | 0.200 0.400 | Rigid | Rigid | Rigid | Rigid | Rigid | Rigid |
| Sle23 | D6 1 | From start Rela | 0.000 0.200 | Rigid | Rigid | Rigid | Rigid | Rigid | Rigid |

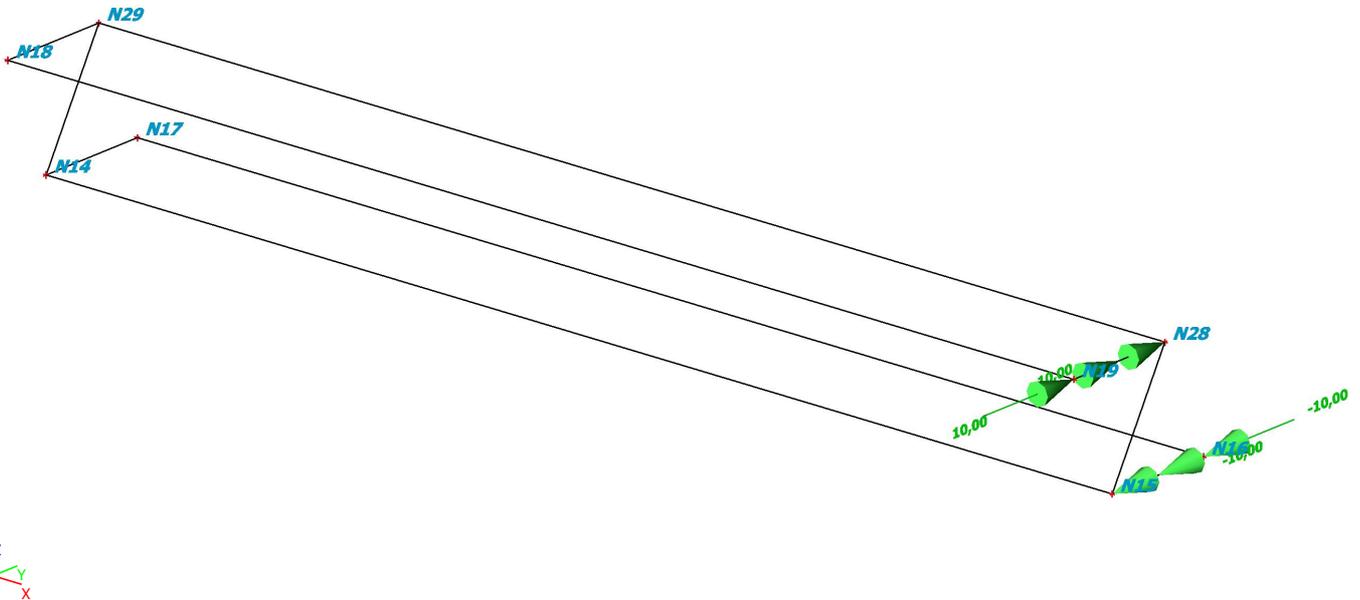
2.5. Materials

Steel EC3

| Name | ρ [kg/m ³] | E _{mod} [MPa] | μ | Limite inférieure [mm] | Limite supérieure [mm] | F _y [MPa] | F _u [MPa] | Colour |
|-------|--------------------------------|---------------------------|--------------------|---------------------------|---------------------------|-------------------------|-------------------------|---|
| | | G _{mod} [MPa] | α [m/mK] | | | | | |
| S 235 | 7850,00 | 2,1000e+05 8,0769e+04 | 0.3 0,01e-003 | 0 40 | 40 80 | 235,0 215,0 | 360,0 360,0 |  |

3. LOAD

3.1. LC2 / Tot. value



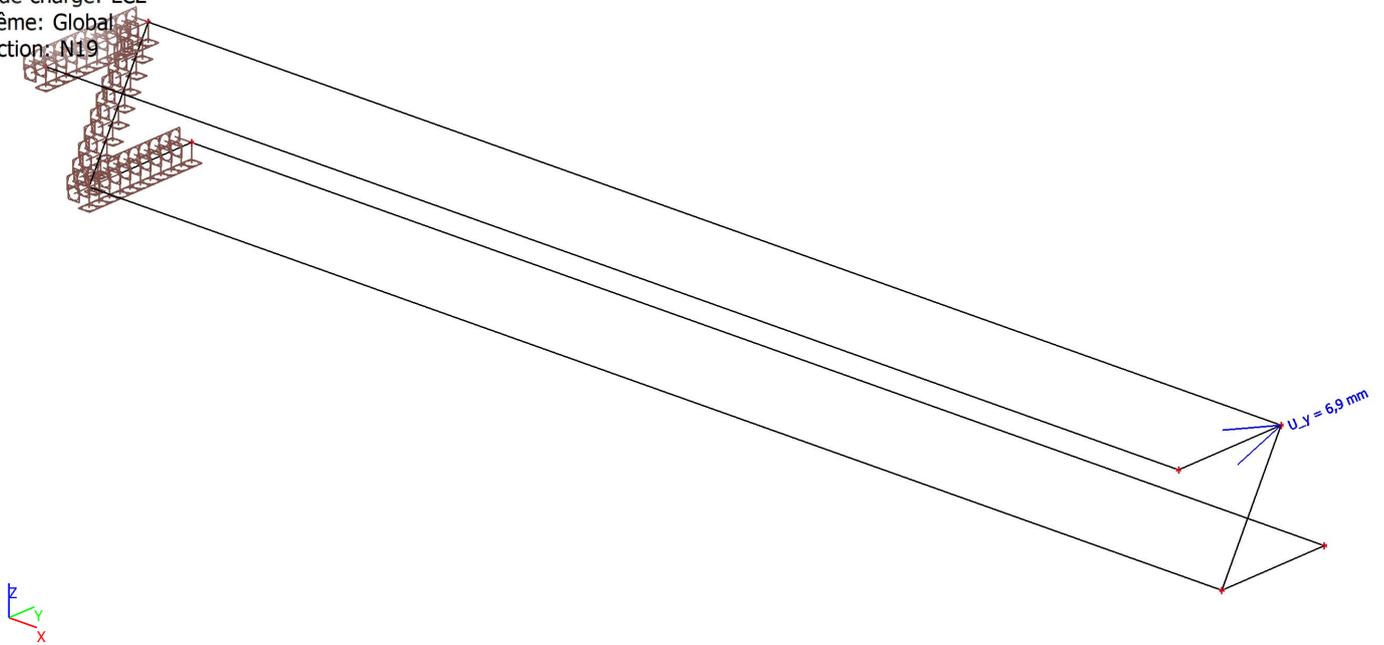
3.2. Line force on 2D member edge

| Name | 2D member | Type | Dir | Value - P ₁ [kN/m] | Pos x ₁ | Loc | Edge |
|------|-----------------|--------|--------------|----------------------------------|--------------------|--------|------------|
| | Load case | System | Distribution | Value - P ₂ [kN/m] | Pos x ₂ | Coor | Orig |
| LFS3 | D4 | Force | Y | -10,00 | 0.000 | Length | 2 |
| | LC2 - Permanent | LCS | Uniform | | 1.000 | Rela | From start |
| LFS4 | D5 | Force | Y | 10,00 | 0.000 | Length | 2 |
| | LC2 - Permanent | LCS | Uniform | | 1.000 | Rela | From start |

4. RESULTS

4.1. Displacement of nodes; U_y

Valeur: U_y
 Calcul linéaire
 Cas de charge: LC2
 Extrême: Global
 Sélection: N19



4.2. Displacement of nodes

Linear calculation
 Load case: LC2
 Extreme: Node
 Selection: N19

| Name | Case | U _y [mm] |
|------|------|------------------------|
| N19 | LC2 | 6,9 |

5. EXPECTED AFNOR RESULTS

Displacement u_y in node N19= -7,15 mm

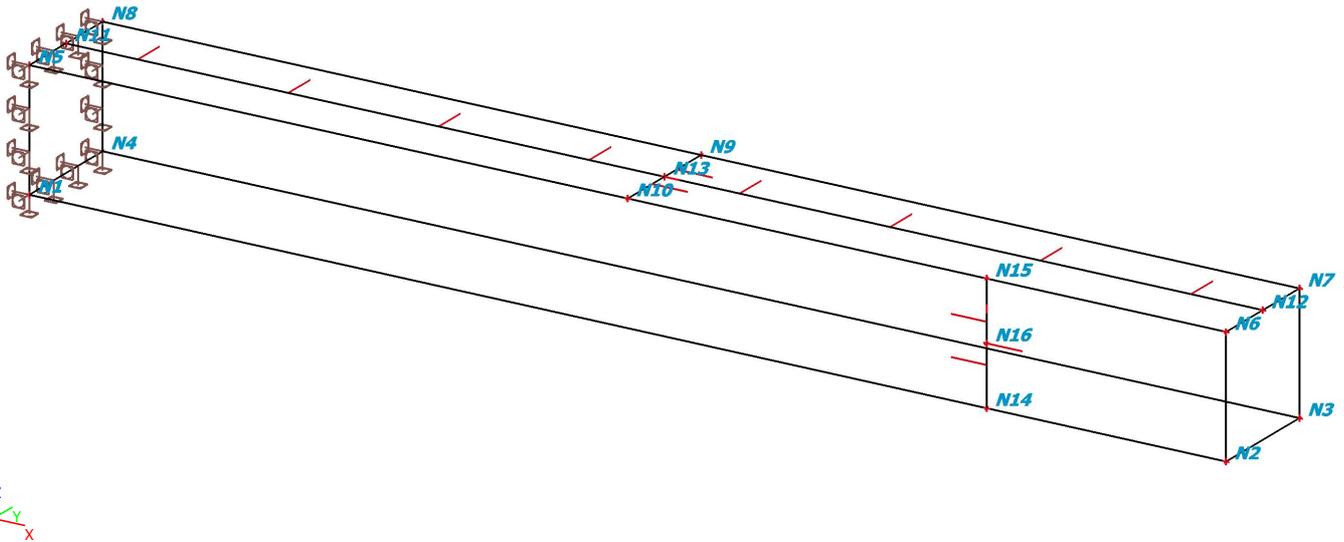
REFERENCE : "Guide de validation des logiciels de calcul de structures" AFNOR, 1990

1. TESTCASE DESCRIPTION

Shell - Box section - Shear - Torsion.

2. MODEL

2.1. Analysis model



2.2. Nodes

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] |
|------|-------------|-------------|-------------|
| N1 | 0,000 | 0,000 | 0,000 |
| N2 | 1,000 | 0,000 | 0,000 |
| N3 | 1,000 | 0,100 | 0,000 |
| N4 | 0,000 | 0,100 | 0,000 |
| N5 | 0,000 | 0,000 | 0,100 |
| N6 | 1,000 | 0,000 | 0,100 |

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] |
|------|-------------|-------------|-------------|
| N7 | 1,000 | 0,100 | 0,100 |
| N8 | 0,000 | 0,100 | 0,100 |
| N9 | 0,500 | 0,100 | 0,100 |
| N10 | 0,500 | 0,000 | 0,100 |
| N11 | 0,000 | 0,050 | 0,100 |
| N12 | 1,000 | 0,050 | 0,100 |

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] |
|------|-------------|-------------|-------------|
| N13 | 0,500 | 0,050 | 0,100 |
| N14 | 0,800 | 0,000 | 0,000 |
| N15 | 0,800 | 0,000 | 0,100 |
| N16 | 0,800 | 0,000 | 0,050 |

2.3. 2D members

| Name | Layer | Type | Element type | Material | Thickness type | Th. [mm] |
|------|---------|------------|--------------|----------|----------------|----------|
| D1 | Calque1 | dalle (90) | Standard | S 235 | constant | 5 |
| D2 | Calque1 | dalle (90) | Standard | S 235 | constant | 5 |
| D3 | Calque1 | dalle (90) | Standard | S 235 | constant | 5 |
| D4 | Calque1 | dalle (90) | Standard | S 235 | constant | 5 |

2.4. Supports on 2D member edge

| Name | 2D member Edge | Orig Coor | Pos x ₁ Pos x ₂ | X | Y | Z | Rx | Ry | Rz |
|------|----------------|--------------------|---------------------------------------|-------|-------|-------|-------|-------|-------|
| Sle1 | D2 4 | From start Rela | 0.000 1.000 | Rigid | Rigid | Rigid | Rigid | Rigid | Rigid |
| Sle2 | D3 1 | From start Rela | 0.000 1.000 | Rigid | Rigid | Rigid | Rigid | Rigid | Rigid |
| Sle3 | D4 1 | From start Rela | 0.000 1.000 | Rigid | Rigid | Rigid | Rigid | Rigid | Rigid |
| Sle4 | D1 4 | From start Rela | 0.000 1.000 | Rigid | Rigid | Rigid | Rigid | Rigid | Rigid |

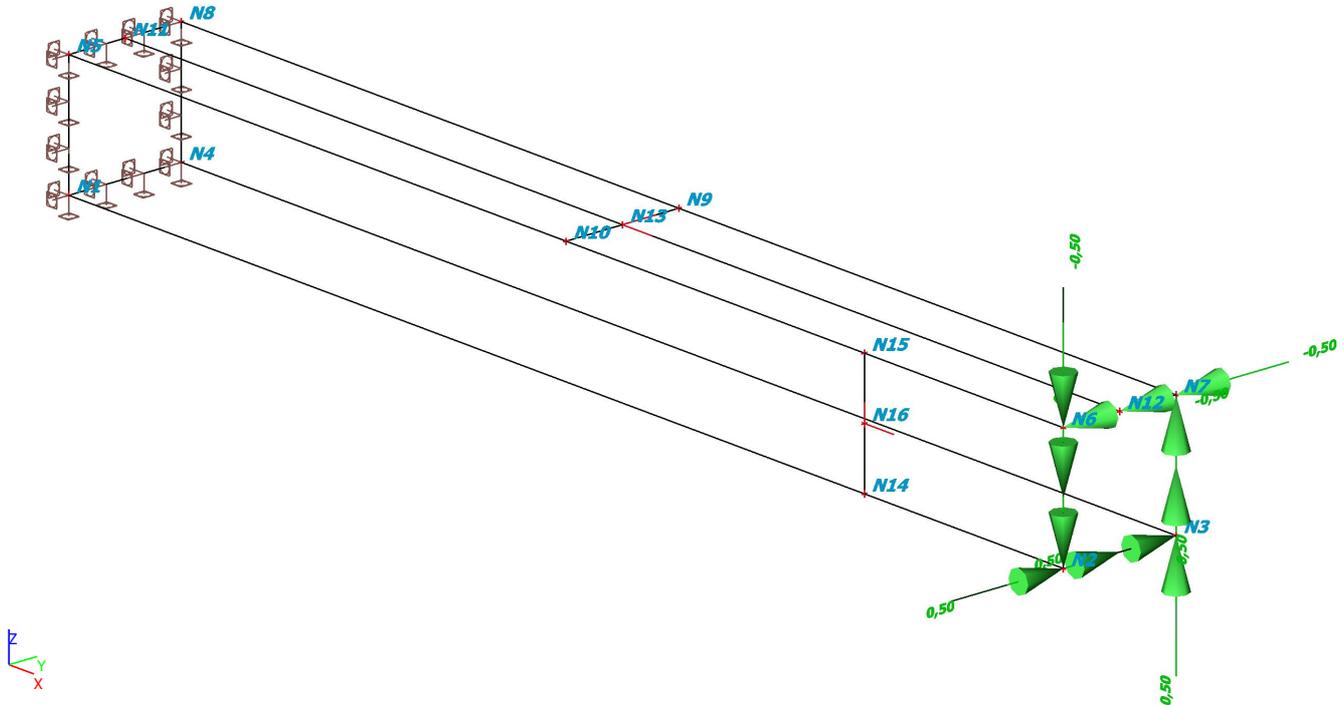
2.5. Materials

Steel EC3

| Name | ρ [kg/m ³] | E_{mod} [MPa] | μ | Limit inférieure [mm] | Limite supérieure [mm] | F_y [MPa] | F_u [MPa] | Colour |
|-------|--------------------------------|--------------------|--------------------|--------------------------|---------------------------|----------------|----------------|--------|
| | | G_{mod} [MPa] | α [m/mK] | | | | | |
| S 235 | 7850,00 | 2,1000e+05 | 0.3 | 0 | 40 | 235,0 | 360,0 | ■ |
| | | 8,0769e+04 | 0,01e-003 | 40 | 80 | 215,0 | 360,0 | |

3. LOAD

3.1. LC1 / Tot. value



3.2. Line force on 2D member edge

| Name | 2D member | Type | Dir | Value - P ₁ [kN/m] | Pos x ₁ | Loc | Edge |
|------|-----------------|--------|--------------|----------------------------------|--------------------|--------|------------|
| | Load case | System | Distribution | Value - P ₂ [kN/m] | Pos x ₂ | Coor | Orig |
| LFS1 | D2 | Force | Y | -0,50 | 0.000 | Length | 2 |
| | LC2 - permanent | GCS | Uniform | | 1.000 | Rela | From start |
| LFS2 | D3 | Force | Z | -0,50 | 0.000 | Length | 3 |
| | LC2 - permanent | GCS | Uniform | | 1.000 | Rela | From start |
| LFS3 | D1 | Force | Y | 0,50 | 0.000 | Length | 2 |
| | LC2 - permanent | GCS | Uniform | | 1.000 | Rela | From start |
| LFS4 | D4 | Force | Z | 0,50 | 0.000 | Length | 3 |
| | LC2 - permanent | GCS | Uniform | | 1.000 | Rela | From start |

4. RESULTS

4.1. Displacement of nodes

Linear calculation

Load case: LC2

Extreme: Node

Selection: N13, N16

| Name | Case | U_y [mm] | U_z [mm] | Φ_x [mrad] |
|------|------|-------------------|-------------------|--------------------|
| N13 | LC2 | -0,0006160 | 0,0000000 | 0,0123250 |
| N16 | LC2 | 0,0000000 | -0,0009860 | 0,0197290 |

5. EXPECTED AFNOR RESULTS

Displacement u_y in node N13= -0,617 e-3 mm

Rotation Φ_x in node N13=0,0123 e-3 rad

Displacement u_z in node N16= -0,987 e-3 mm

Rotation Φ_x in node N13 =0,0197 e-3 rad

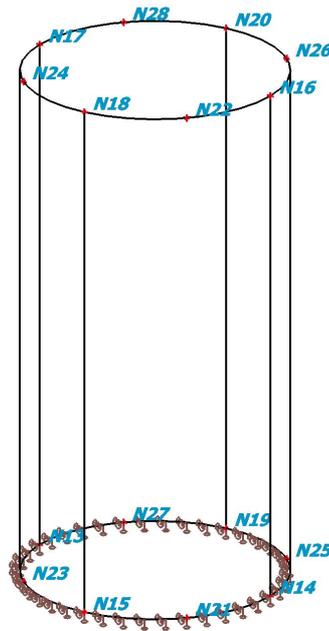
REFERENCE : "Guide de validation des progiciels de calcul de structures" AFNOR, 1990

1. TESTCASE DESCRIPTION

Thin-walled cylinder under uniform radial pressure
Specification: Shell - Cylinder - Material: elastic - Pressure

2. MODEL

2.1. Analysis model



2.2. Noeuds

| Nom | Coord X [m] | Coord Y [m] | Coord Z [m] |
|-----|-------------|-------------|-------------|
| N13 | -0,707 | 0,707 | 0,000 |
| N14 | 1,293 | 0,707 | 0,000 |
| N15 | 0,293 | -0,293 | 0,000 |
| N16 | 1,293 | 0,707 | 4,000 |
| N17 | -0,707 | 0,707 | 4,000 |
| N18 | 0,293 | -0,293 | 4,000 |

| Nom | Coord X [m] | Coord Y [m] | Coord Z [m] |
|-----|-------------|-------------|-------------|
| N19 | 0,293 | 1,707 | 0,000 |
| N20 | 0,293 | 1,707 | 4,000 |
| N21 | 1,000 | 0,000 | 0,000 |
| N22 | 1,000 | 0,000 | 4,000 |
| N23 | -0,414 | 0,000 | 0,000 |
| N24 | -0,414 | 0,000 | 4,000 |

| Nom | Coord X [m] | Coord Y [m] | Coord Z [m] |
|-----|-------------|-------------|-------------|
| N25 | 1,000 | 1,414 | 0,000 |
| N26 | 1,000 | 1,414 | 4,000 |
| N27 | -0,414 | 1,414 | 0,000 |
| N28 | -0,414 | 1,414 | 4,000 |

2.3. Surfaces

| Nom | Calque | Type | Type d'élément | Matériau | Type d'épaisseur | Ep. [mm] |
|-----|---------|------------|----------------|----------|------------------|----------|
| D6 | Calque1 | voile (80) | Standard | S 235 | constante | 20 |
| D7 | Calque1 | voile (80) | Standard | S 235 | constante | 20 |
| D8 | Calque1 | voile (80) | Standard | S 235 | constante | 20 |
| D9 | Calque1 | voile (80) | Standard | S 235 | constante | 20 |

2.4. Appuis aux bords

| Nom | Macro 2D Bord | Orig Coor | Pos x ₁ Pos x ₂ | X | Y | Z | Rx | Ry | Rz |
|-------|---------------|--------------------------|--|----------|----------|--------|-------|-------|-------|
| Sle11 | D6 1 | Depuis le départ Rela | 0.000 1.000 | Flexible | Flexible | Rigide | Libre | Libre | Libre |
| Sle12 | D8 1 | Depuis le départ Rela | 0.000 1.000 | Flexible | Flexible | Rigide | Libre | Libre | Libre |
| Sle13 | D9 1 | Depuis le départ Rela | 0.000 1.000 | Flexible | Flexible | Rigide | Libre | Libre | Libre |
| Sle14 | D7 | Depuis le départ | 0.000 | Flexible | Flexible | Rigide | Libre | Libre | Libre |

| Nom | Macro 2D | Orig | Pos x ₁ | X | Y | Z | Rx | Ry | Rz |
|-----|----------|------|--------------------|---|---|---|----|----|----|
| | Bord | Coor | Pos x ₂ | | | | | | |
| | 1 | Rela | 1.000 | | | | | | |

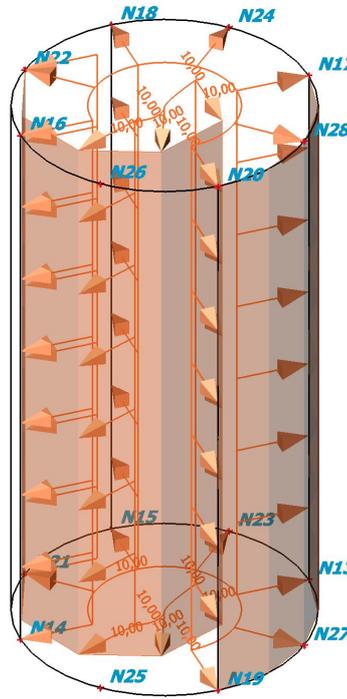
2.5. Matériaux

Acier EC3

| Nom | ρ [kg/m ³] | E_{mod} [MPa] | μ | Limit inférieure [mm] | Limite supérieure [mm] | F_y [kPa] | F_u [kPa] | Couleur |
|-------|--------------------------------|--------------------|--------------------|--------------------------|---------------------------|----------------|----------------|---|
| | | G_{mod} [MPa] | α [m/mK] | | | | | |
| S 235 | 7850,00 | 2,1000e+05 | 0.3 | 0 | 40 | 235000,000 | 360000,000 |  |
| | | 8,0769e+04 | 0,01e-003 | 40 | 80 | 215000,000 | 360000,000 | |

3. LOAD

3.1. LC1 / Tot. value



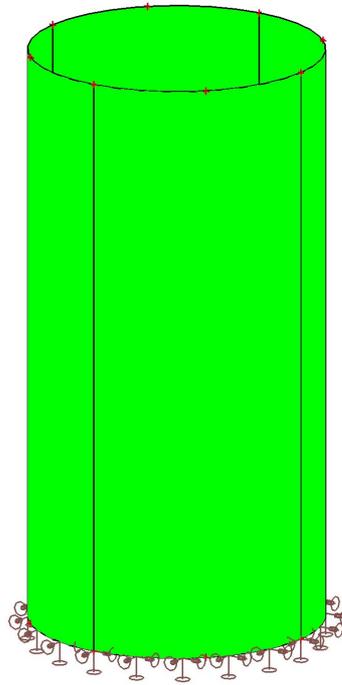
3.2. Charge libre surfacique

| Nom | Cas de charge | Dir | Type | Distribution | q [kN/m ²] | Validité | Sélectionner | Système | Position |
|-----|-----------------|-----|-------|--------------|---------------------------|----------|--------------|-------------|----------|
| FF1 | LC2 - Permanent | Z | Force | Uniforme | 10,00 | Tout | Auto | SCL élément | Longueur |

4. RESULTS

4.1. 2D stress/strain; σ_{x+}

Valeur: σ_{x+}
 Calcul linéaire
 Cas de charge: LC2
 Extrême: Global
 Sélection: Tout
 Position: Aux centres. Système: SCL
 maillage EF

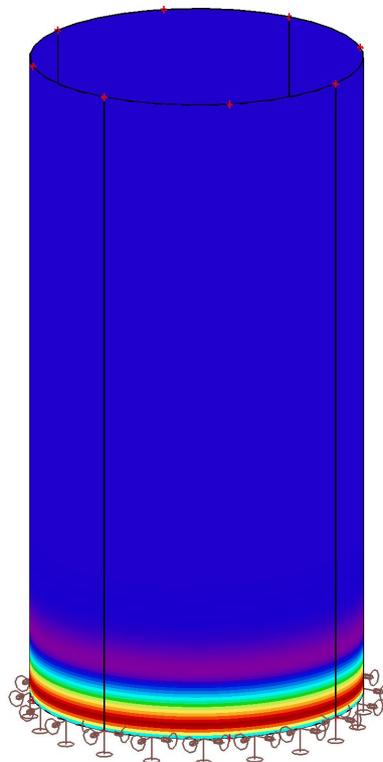


Valeur constante 499.976
 σ_{x+} [kPa]



4.2. 2D stress/strain; σ_{y+}

Valeur: σ_{y+}
 Calcul linéaire
 Cas de charge: LC2
 Extrême: Global
 Sélection: Tout
 Position: Aux centres. Système: SCL
 maillage EF



0.000
 0.000
 0.000
 0.000
 0.000
 0.000
 0.000
 0.000
 -0.000
 σ_{y+} [kPa]



4.3. Contraintes/déformations 2D

Calcul linéaire

Cas de charge: LC2

Extrême: Global

Sélection: Tout

Position: Aux centres. Système: SCL maillage EF

Contrainte de base

| Nom | Maillage | Position [m] | Cas | σ_{x+} | σ_{y+} | T_{xy+} | T_{xz} | T_{yz} |
|-----|----------------|--------------------------|-----|----------------------------------|------------------------------|------------------------------|--------------|--------------|
| | | | | [kPa] | [kPa] | [kPa] | [kPa] | [kPa] |
| | | | | σ_{x-} | σ_{y-} | T_{xy-} | | |
| | | | | [kPa] | [kPa] | [kPa] | | |
| D7 | Elément: 16001 | 0,283 -0,293 0,010 | LC2 | 499,976 499,976 | 0,000 0,000 | 0,000 0,000 | 0,000 | 0,000 |
| D6 | Elément: 1684 | 0,362 -0,290 0,430 | LC2 | 499,976 499,976 | 0,000 0,000 | 0,000 0,000 | 0,000 | 0,000 |
| D6 | Elément: 321 | 0,303 -0,293 0,090 | LC2 | 499,976 499,976 | 0,000 0,000 | 0,000 0,000 | 0,000 | 0,000 |
| D6 | Elément: 1310 | 0,840 -0,130 0,330 | LC2 | 499,976 499,976 | 0,000 0,000 | 0,000 0,000 | 0,000 | 0,000 |
| D6 | Elément: 641 | 0,303 -0,293 0,170 | LC2 | 499,976 499,976 | 0,000 0,000 | 0,000 0,000 | 0,000 | 0,000 |

4.4. Déplacements 2D

Calcul linéaire

Cas de charge: LC2

Extrême: Global

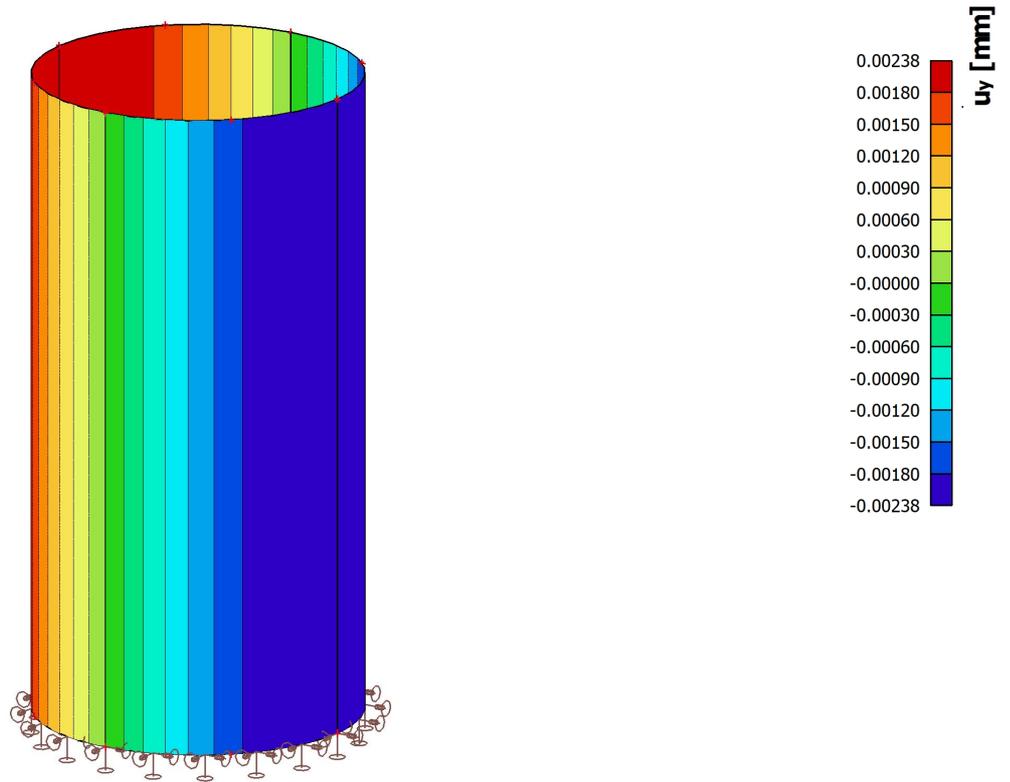
Sélection: Tout

Position: Aux noeuds, moyenne sur macro. Système: SCL maillage EF

| Nom | Maillage | Position [m] | Cas | u_x | u_y | u_z | φ_x | φ_y | φ_z | U_{total} |
|-----|--------------------------------------|--------------------------|-----|----------------|-----------------|----------------|-------------|-------------|-------------|----------------|
| | | | | [mm] | [mm] | [mm] | [mrad] | [mrad] | [mrad] | [mm] |
| D6 | Elément: 15921 Noeud: 16201 | 0,313 -0,293 4,000 | LC2 | 0,00000 | -0,00286 | 0,00238 | 0,0 | 0,0 | 0,0 | 0,00372 |
| D6 | Elément: 1 Noeud: 1 | 0,293 -0,293 0,000 | LC2 | 0,00000 | 0,00000 | 0,00238 | 0,0 | 0,0 | 0,0 | 0,00238 |

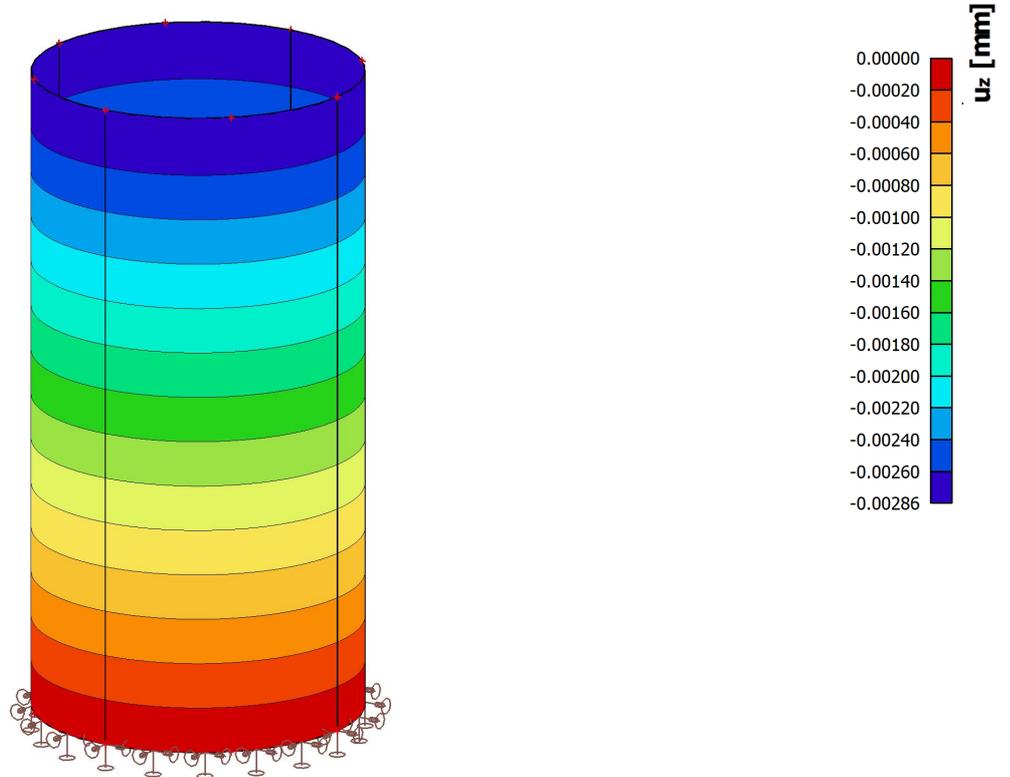
4.5. 2D displacement; u_y

Valeur: u_y
 Calcul linéaire
 Cas de charge: LC2
 Extrême: Global
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



4.6. 2D displacement; u_z

Valeur: u_z
 Calcul linéaire
 Cas de charge: LC2
 Extrême: Global
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



5. EXPECTED AFNOR RESULTS

$\sigma_x = 500 \text{ kPa}$

$\sigma_y = 0 \text{ kPa}$

Radial displacement = $2,38 \cdot 10^{-3} \text{ mm}$

Vertical displacement = $-2,86 \cdot 10^{-3} \text{ mm}$

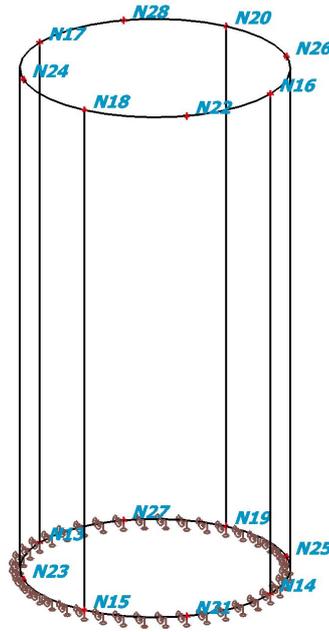
REFERENCE : "Guide de validation des progiciels de calcul de structures" AFNOR, 1990

1. TESTCASE DESCRIPTION

Thin-walled cylinder under uniform axial load
Specification: Shell - Cylinder - Material: elastic - axial load

2. MODEL

2.1. Analysis model



2.2. Noeuds

| Nom | Coord X [m] | Coord Y [m] | Coord Z [m] |
|-----|-------------|-------------|-------------|
| N13 | -0,707 | 0,707 | 0,000 |
| N14 | 1,293 | 0,707 | 0,000 |
| N15 | 0,293 | -0,293 | 0,000 |
| N16 | 1,293 | 0,707 | 4,000 |
| N17 | -0,707 | 0,707 | 4,000 |
| N18 | 0,293 | -0,293 | 4,000 |

| Nom | Coord X [m] | Coord Y [m] | Coord Z [m] |
|-----|-------------|-------------|-------------|
| N19 | 0,293 | 1,707 | 0,000 |
| N20 | 0,293 | 1,707 | 4,000 |
| N21 | 1,000 | 0,000 | 0,000 |
| N22 | 1,000 | 0,000 | 4,000 |
| N23 | -0,414 | 0,000 | 0,000 |
| N24 | -0,414 | 0,000 | 4,000 |

| Nom | Coord X [m] | Coord Y [m] | Coord Z [m] |
|-----|-------------|-------------|-------------|
| N25 | 1,000 | 1,414 | 0,000 |
| N26 | 1,000 | 1,414 | 4,000 |
| N27 | -0,414 | 1,414 | 0,000 |
| N28 | -0,414 | 1,414 | 4,000 |

2.3. Surfaces

| Nom | Calque | Type | Type d'élément | Matériau | Type d'épaisseur | Ep. [mm] |
|-----|---------|------------|----------------|----------|------------------|----------|
| D6 | Calque1 | voile (80) | Standard | S 235 | constante | 20 |
| D7 | Calque1 | voile (80) | Standard | S 235 | constante | 20 |
| D8 | Calque1 | voile (80) | Standard | S 235 | constante | 20 |
| D9 | Calque1 | voile (80) | Standard | S 235 | constante | 20 |

2.4. Appuis aux bords

| Nom | Macro 2D Bord | Orig Coor | Pos x ₁ Pos x ₂ | X | Y | Z | Rx | Ry | Rz |
|-------|---------------|--------------------------|--|----------|----------|--------|-------|-------|-------|
| Sle11 | D6 1 | Depuis le départ Rela | 0.000 1.000 | Flexible | Flexible | Rigide | Libre | Libre | Libre |
| Sle12 | D8 1 | Depuis le départ Rela | 0.000 1.000 | Flexible | Flexible | Rigide | Libre | Libre | Libre |
| Sle13 | D9 1 | Depuis le départ Rela | 0.000 1.000 | Flexible | Flexible | Rigide | Libre | Libre | Libre |
| Sle14 | D7 | Depuis le départ | 0.000 | Flexible | Flexible | Rigide | Libre | Libre | Libre |

| Nom | Macro 2D | Orig | Pos x ₁ | X | Y | Z | Rx | Ry | Rz |
|-----|----------|------|--------------------|---|---|---|----|----|----|
| | Bord | Coor | Pos x ₂ | | | | | | |
| | 1 | Rela | 1.000 | | | | | | |

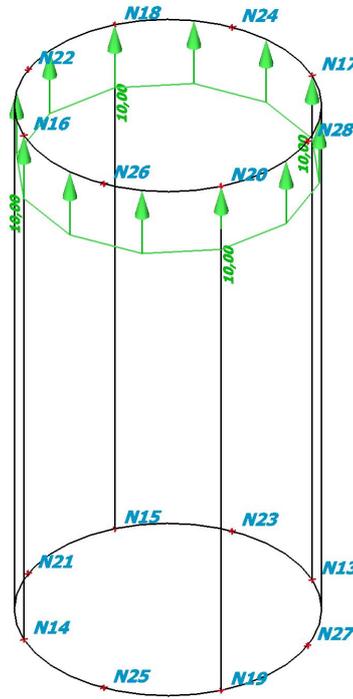
2.5. Matériaux

Acier EC3

| Nom | ρ [kg/m ³] | E_{mod} [MPa] | μ | Limit inférieure [mm] | Limite supérieure [mm] | F_y [kPa] | F_u [kPa] | Couleur |
|-------|--------------------------------|--------------------|--------------------|--------------------------|---------------------------|----------------|----------------|---|
| | | G_{mod} [MPa] | α [m/mK] | | | | | |
| S 235 | 7850,00 | 2,1000e+05 | 0.3 | 0 | 40 | 235000,000 | 360000,000 |  |
| | | 8,0769e+04 | 0,01e-003 | 40 | 80 | 215000,000 | 360000,000 | |

3. LOAD

3.1. LC1 / Tot. value



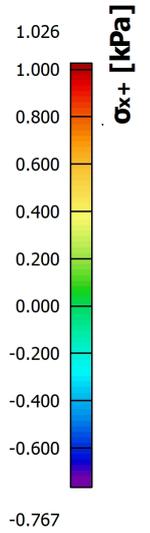
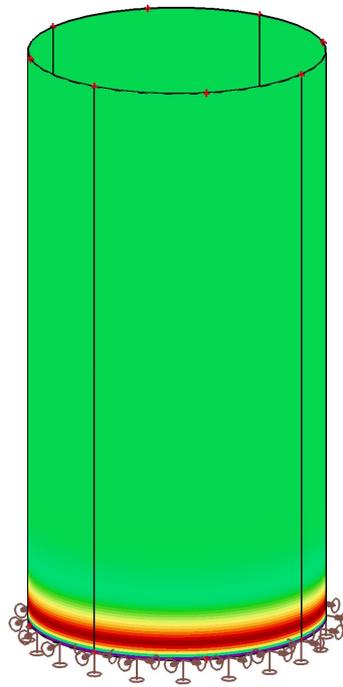
3.2. Charge répartie sur un bord

| Nom | Macro 2D | Type | Dir | Valeur - P ₁ [kN/m] | Pos x ₁ | Pos | Bord |
|------|-----------------|---------|--------------|-----------------------------------|--------------------|----------|------------------|
| | Cas de charge | Système | Distribution | Valeur - P ₂ [kN/m] | Pos x ₂ | Coor | Orig |
| LFS1 | D7 | Force | Z | 10,00 | 0.000 | Longueur | 3 |
| | LC2 - Permanent | SCG | Uniforme | | 1.000 | Rela | Depuis le départ |
| LFS2 | D8 | Force | Z | 10,00 | 0.000 | Longueur | 3 |
| | LC2 - Permanent | SCG | Uniforme | | 1.000 | Rela | Depuis le départ |
| LFS3 | D9 | Force | Z | 10,00 | 0.000 | Longueur | 3 |
| | LC2 - Permanent | SCG | Uniforme | | 1.000 | Rela | Depuis le départ |
| LFS4 | D6 | Force | Z | 10,00 | 0.000 | Longueur | 3 |
| | LC2 - Permanent | SCG | Uniforme | | 1.000 | Rela | Depuis le départ |

4. RESULTS

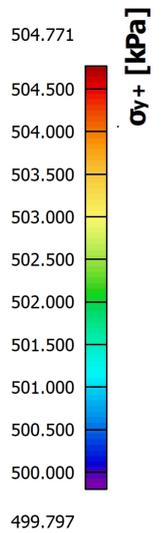
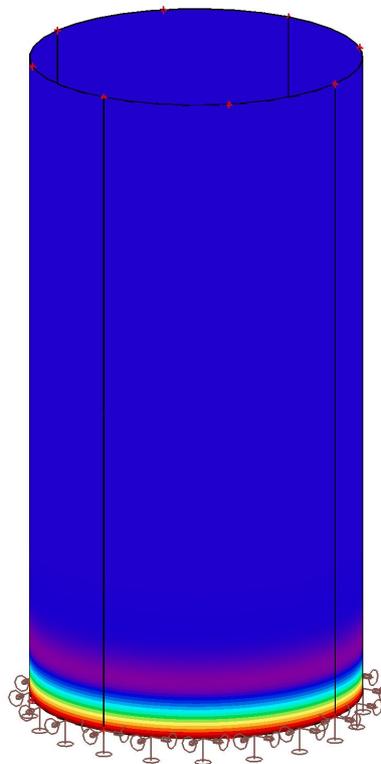
4.1. 2D stress/strain; σ_{x+}

Valeur: σ_{x+}
 Calcul linéaire
 Cas de charge: LC2
 Extrême: Global
 Sélection: Tout
 Position: Aux centres. Système: SCL
 maillage EF



4.2. 2D stress/strain; σ_{y+}

Valeur: σ_{y+}
 Calcul linéaire
 Cas de charge: LC2
 Extrême: Global
 Sélection: Tout
 Position: Aux centres. Système: SCL
 maillage EF



4.3. Contraintes/déformations 2D

Calcul linéaire

Cas de charge: LC2

Extrême: Global

Sélection: Tout

Position: Aux centres. Système: SCL maillage EF

Contrainte de base

| Nom | Maillage | Position [m] | Cas | σ_{x+} | σ_{y+} | τ_{xy+} | τ_{xz} | τ_{yz} | |
|-----|---------------|--------------------------|-----|--------------------------------|----------------------------------|------------------------------|--------------|---------------|-------|
| | | | | [kPa] | [kPa] | [kPa] | | | [kPa] |
| | | | | σ_{x-} | σ_{y-} | τ_{xy-} | | | |
| | | | | [kPa] | [kPa] | [kPa] | | | |
| D6 | Elément: 419 | 0,648 -0,228 0,110 | LC2 | 1,026 -0,446 | 502,454 497,546 | 0,000 0,000 | 0,000 | -0,135 | |
| D6 | Elément: 888 | 0,440 -0,282 0,230 | LC2 | 0,514 0,376 | 500,231 499,769 | 0,000 0,000 | 0,000 | -0,047 | |
| D6 | Elément: 1361 | 0,303 -0,293 0,350 | LC2 | 0,045 0,167 | 499,797 500,203 | 0,000 0,000 | 0,000 | 0,000 | |
| D6 | Elément: 2 | 0,322 -0,292 0,010 | LC2 | -0,767 -3,629 | 504,770 495,230 | 0,000 0,000 | 0,000 | -0,035 | |
| D6 | Elément: 80 | 1,293 0,697 0,010 | LC2 | -0,767 -3,629 | 504,771 495,230 | 0,000 0,000 | 0,000 | -0,035 | |
| D6 | Elément: 1 | 0,303 -0,293 0,010 | LC2 | -0,767 -3,629 | 504,771 495,230 | 0,000 0,000 | 0,000 | -0,035 | |
| D6 | Elément: 326 | 0,401 -0,287 0,090 | LC2 | 0,953 -0,851 | 503,007 496,993 | 0,000 0,000 | 0,000 | -0,140 | |
| D6 | Elément: 1681 | 0,303 -0,293 0,430 | LC2 | -0,038 0,043 | 499,865 500,135 | 0,000 0,000 | 0,000 | 0,006 | |

4.4. Déplacements 2D

Calcul linéaire

Cas de charge: LC2

Extrême: Global

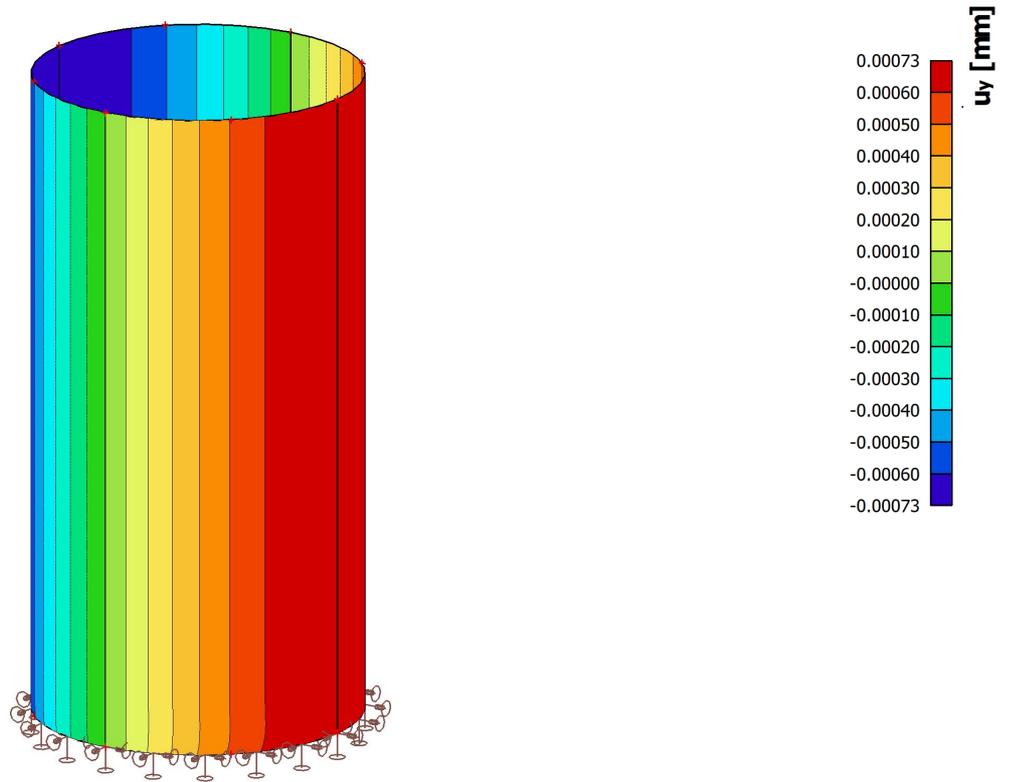
Sélection: Tout

Position: Aux noeuds, moyenne sur macro. Système: SCL maillage EF

| Nom | Maillage | Position [m] | Cas | u_x | u_y | u_z | ϕ_x | ϕ_y | ϕ_z | U_{total} |
|-----|--------------------------------|--------------------------|-----|----------------|----------------|-----------------|------------|------------|------------|----------------|
| | | | | [mm] | [mm] | [mm] | [mrad] | [mrad] | [mrad] | |
| D6 | Elément: 1 Noeud: 161 | 0,313 -0,293 0,020 | LC2 | 0,00000 | 0,00005 | -0,00072 | 0,0 | 0,0 | 0,0 | 0,00072 |
| D6 | Elément: 15921 Noeud: 16201 | 0,313 -0,293 4,000 | LC2 | 0,00000 | 0,00952 | -0,00071 | 0,0 | 0,0 | 0,0 | 0,00955 |

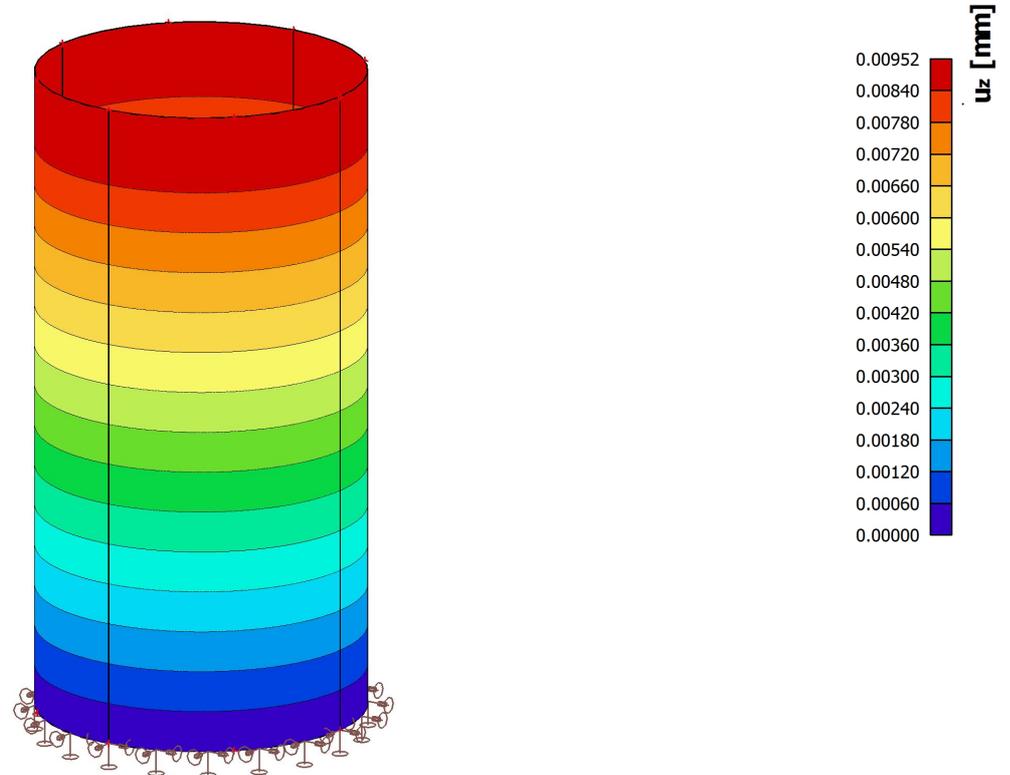
4.5. 2D displacement; u_y

Valeur: u_y
 Calcul linéaire
 Cas de charge: LC2
 Extrême: Global
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



4.6. 2D displacement; u_z

Valeur: u_z
 Calcul linéaire
 Cas de charge: LC2
 Extrême: Global
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



5. EXPECTED AFNOR RESULTS

$\sigma_x = 0$ kPa

$\sigma_y = 500$ kPa

Radial displacement = $-7.14 \cdot 10^{-3}$ mm

Vertical displacement = $9.52 \cdot 10^{-3}$ mm

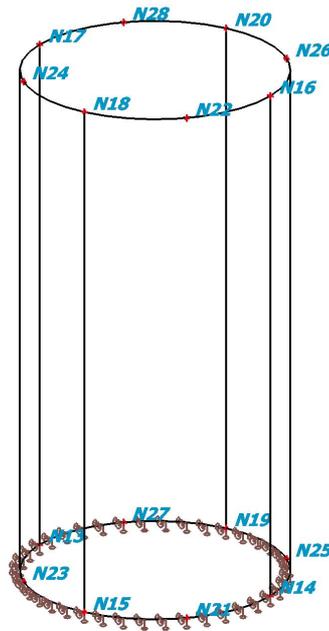
REFERENCE : "Guide de validation des progiciels de calcul de structures" AFNOR, 1990

1. TESTCASE DESCRIPTION

Thin-walled cylinder under hydrostatic pressure
Specification: Shell - Cylinder - Material: elastic - Pressure

2. MODEL

2.1. Analysis model



2.2. Noeuds

| Nom | Coord X [m] | Coord Y [m] | Coord Z [m] |
|-----|-------------|-------------|-------------|
| N13 | -0,707 | 0,707 | 0,000 |
| N14 | 1,293 | 0,707 | 0,000 |
| N15 | 0,293 | -0,293 | 0,000 |
| N16 | 1,293 | 0,707 | 4,000 |
| N17 | -0,707 | 0,707 | 4,000 |
| N18 | 0,293 | -0,293 | 4,000 |

| Nom | Coord X [m] | Coord Y [m] | Coord Z [m] |
|-----|-------------|-------------|-------------|
| N19 | 0,293 | 1,707 | 0,000 |
| N20 | 0,293 | 1,707 | 4,000 |
| N21 | 1,000 | 0,000 | 0,000 |
| N22 | 1,000 | 0,000 | 4,000 |
| N23 | -0,414 | 0,000 | 0,000 |
| N24 | -0,414 | 0,000 | 4,000 |

| Nom | Coord X [m] | Coord Y [m] | Coord Z [m] |
|-----|-------------|-------------|-------------|
| N25 | 1,000 | 1,414 | 0,000 |
| N26 | 1,000 | 1,414 | 4,000 |
| N27 | -0,414 | 1,414 | 0,000 |
| N28 | -0,414 | 1,414 | 4,000 |

2.3. Surfaces

| Nom | Calque | Type | Type d'élément | Matériau | Type d'épaisseur | Ep. [mm] |
|-----|---------|------------|----------------|----------|------------------|----------|
| D6 | Calque1 | voile (80) | Standard | S 235 | constante | 20 |
| D7 | Calque1 | voile (80) | Standard | S 235 | constante | 20 |
| D8 | Calque1 | voile (80) | Standard | S 235 | constante | 20 |
| D9 | Calque1 | voile (80) | Standard | S 235 | constante | 20 |

2.4. Appuis aux bords

| Nom | Macro 2D Bord | Orig Coor | Pos x ₁ Pos x ₂ | X | Y | Z | Rx | Ry | Rz |
|-------|---------------|--------------------------|---------------------------------------|----------|----------|--------|-------|-------|-------|
| Sle11 | D6 1 | Depuis le départ Rela | 0.000 1.000 | Flexible | Flexible | Rigide | Libre | Libre | Libre |
| Sle12 | D8 1 | Depuis le départ Rela | 0.000 1.000 | Flexible | Flexible | Rigide | Libre | Libre | Libre |
| Sle13 | D9 1 | Depuis le départ Rela | 0.000 1.000 | Flexible | Flexible | Rigide | Libre | Libre | Libre |
| Sle14 | D7 | Depuis le départ | 0.000 | Flexible | Flexible | Rigide | Libre | Libre | Libre |

| Nom | Macro 2D | Orig | Pos x ₁ | X | Y | Z | Rx | Ry | Rz |
|-----|----------|------|--------------------|---|---|---|----|----|----|
| | Bord | Coor | Pos x ₂ | | | | | | |
| | 1 | Rela | 1.000 | | | | | | |

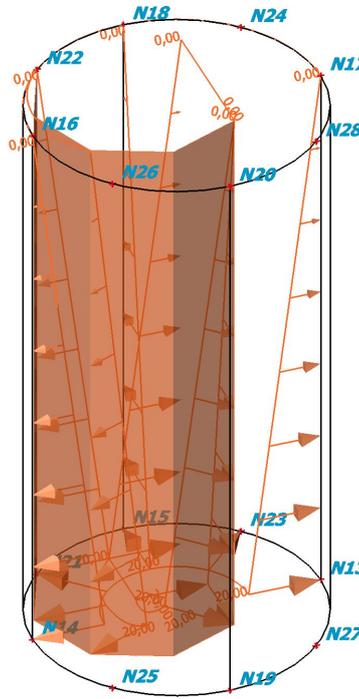
2.5. Matériaux

Acier EC3

| Nom | ρ [kg/m ³] | E_{mod} [MPa] | μ | Limit inférieure [mm] | Limite supérieure [mm] | F_y [kPa] | F_u [kPa] | Couleur |
|-------|--------------------------------|--------------------|--------------------|--------------------------|---------------------------|----------------|----------------|---|
| | | G_{mod} [MPa] | α [m/mK] | | | | | |
| S 235 | 7850,00 | 2,1000e+05 | 0.3 | 0 | 40 | 235000,000 | 360000,000 |  |
| | | 8,0769e+04 | 0,01e-003 | 40 | 80 | 215000,000 | 360000,000 | |

3. LOAD

3.1. LC1 / Tot. value



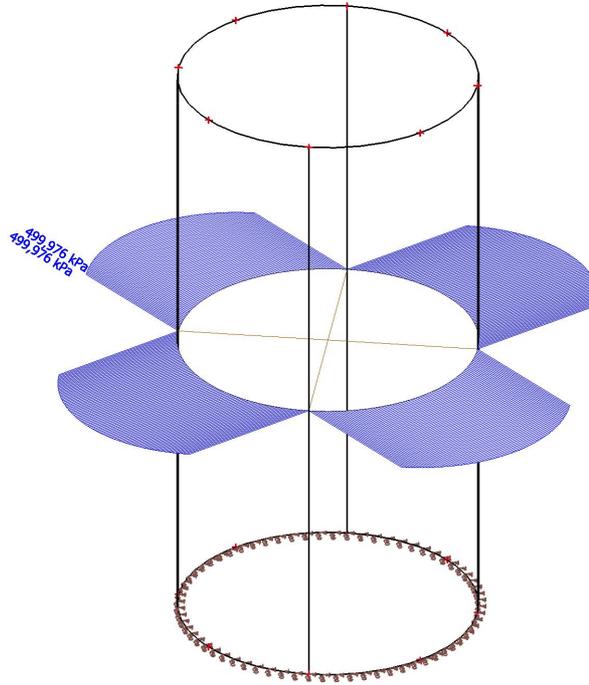
3.2. Charge libre surfacique

| Nom | Cas de charge | Dir | Type | Distribution | q1 [kN/m ²] | q2 [kN/m ²] | Validité | Sélectionner | Système | Position |
|-----|-----------------|-----|-------|--------------|----------------------------|----------------------------|----------|--------------|-------------|----------|
| FF1 | LC2 - Permanent | Z | Force | Dir Y | 0,00 | 20,00 | Tout | Auto | SCL élément | Longueur |

4. RESULTS

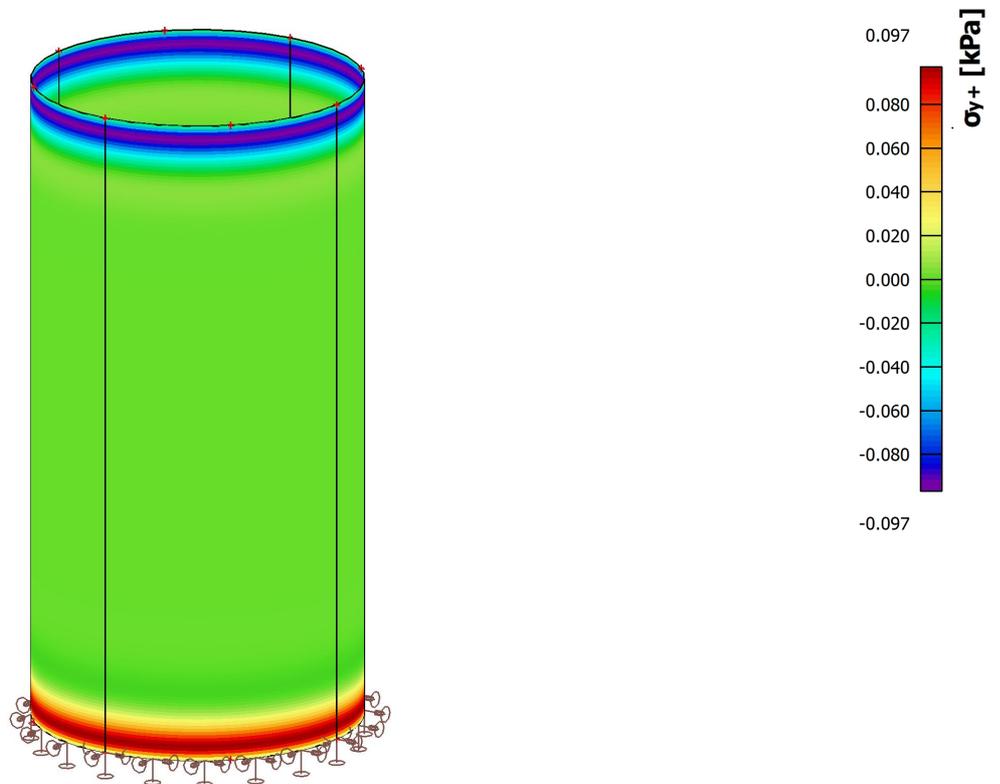
4.1. 2D stress/strain; σ_{x+}

Valeur: σ_{x+}
 Calcul linéaire
 Cas de charge: LC2
 Extrême: Global
 Sélection: Tout
 Position: Aux noeuds, moyenne sur macro. Système: SCL maillage EF



4.2. 2D stress/strain; σ_{y+}

Valeur: σ_{y+}
 Calcul linéaire
 Cas de charge: LC2
 Extrême: Global
 Sélection: Tout
 Position: Aux centres. Système: SCL maillage EF



4.3. Déplacements 2D

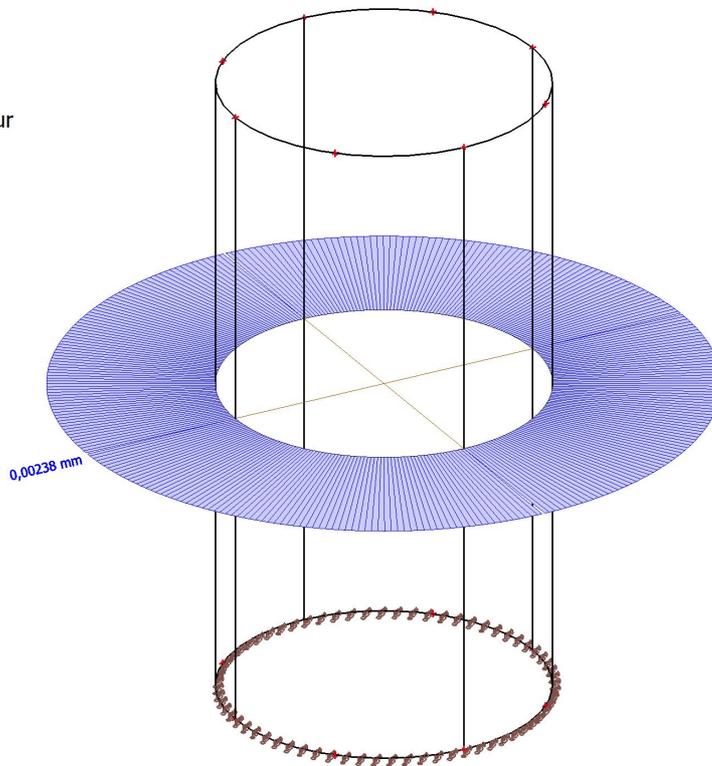
Calcul linéaire
 Cas de charge: LC2
 Extrême: Global
 Sélection: Tout
 Position: Aux noeuds, moyenne sur macro. Système: SCL maillage EF

Résultats dans les coupes:

| Nom | Maillage | Position [m] | Cas | u _z [mm] |
|-----|----------------|-------------------------|-----|---------------------|
| SE1 | Elément: 39921 | 0,293 1,707 2,000 | LC2 | 0,00238 |

4.4. 2D displacement; u_z

Valeur: u_z
 Calcul linéaire
 Cas de charge: LC2
 Extrême: Global
 Sélection: Tout
 Position: Aux noeuds, moyenne sur macro. Système: SCL maillage EF



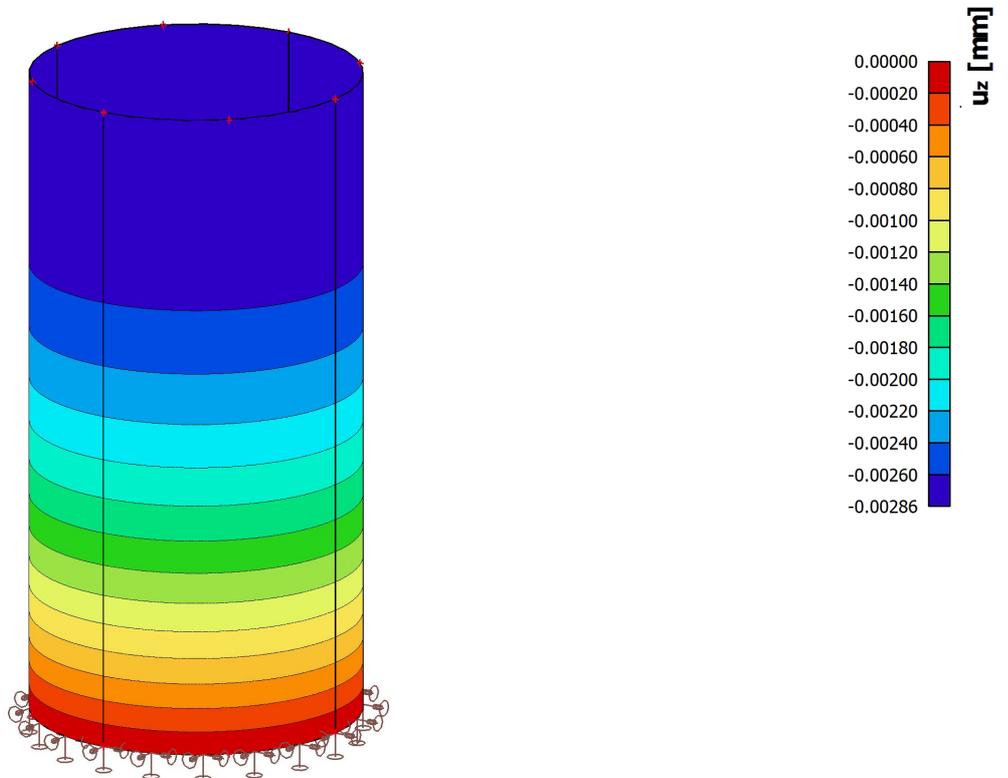
4.5. Déplacements 2D

Calcul linéaire
 Cas de charge: LC2
 Extrême: Global
 Sélection: Tout
 Position: Aux noeuds, moyenne sur macro. Système: SCL maillage EF

| Nom | Maillage | Position [m] | Cas | u_y [mm] |
|-----|--------------------------------|--------------------------|-----|-----------------|
| D6 | Elément: 15761 Noeud: 16039 | 0,313 -0,293 3,960 | LC2 | -0,00286 |
| D6 | Elément: 1 Noeud: 1 | 0,293 -0,293 0,000 | LC2 | 0,00000 |

4.6. 2D displacement; u_z

Valeur: u_z
 Calcul linéaire
 Cas de charge: LC2
 Extrême: Global
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



5. EXPECTED AFNOR RESULTS

σ_x (at mid-height) = 500 kPa

σ_y (on whole height) = 0 kPa

Radial displacement (at mid-height) = $2,38 \cdot 10^{-3}$ mm

Vertical displacement (at top) = $-2,86 \cdot 10^{-3}$ mm

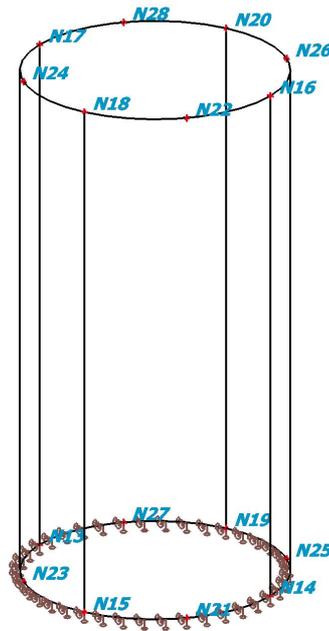
REFERENCE : "Guide de validation des progiciels de calcul de structures" AFNOR, 1990

1. TESTCASE DESCRIPTION

Thin-walled cylinder under selfweight
Specification: Shell - Cylinder - Material: elastic

2. MODEL

2.1. Analysis model



2.2. Nodes

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] |
|------|-------------|-------------|-------------|
| N13 | -0,707 | 0,707 | 0,000 |
| N14 | 1,293 | 0,707 | 0,000 |
| N15 | 0,293 | -0,293 | 0,000 |
| N16 | 1,293 | 0,707 | 4,000 |
| N17 | -0,707 | 0,707 | 4,000 |
| N18 | 0,293 | -0,293 | 4,000 |

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] |
|------|-------------|-------------|-------------|
| N19 | 0,293 | 1,707 | 0,000 |
| N20 | 0,293 | 1,707 | 4,000 |
| N21 | 1,000 | 0,000 | 0,000 |
| N22 | 1,000 | 0,000 | 4,000 |
| N23 | -0,414 | 0,000 | 0,000 |
| N24 | -0,414 | 0,000 | 4,000 |

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] |
|------|-------------|-------------|-------------|
| N25 | 1,000 | 1,414 | 0,000 |
| N26 | 1,000 | 1,414 | 4,000 |
| N27 | -0,414 | 1,414 | 0,000 |
| N28 | -0,414 | 1,414 | 4,000 |

2.3. 2D members

| Name | Layer | Type | Element type | Material | Thickness type | Th. [mm] |
|------|---------|------------|--------------|----------|----------------|----------|
| D6 | Calque1 | voile (80) | Standard | S 235 | constant | 20 |
| D7 | Calque1 | voile (80) | Standard | S 235 | constant | 20 |
| D8 | Calque1 | voile (80) | Standard | S 235 | constant | 20 |
| D9 | Calque1 | voile (80) | Standard | S 235 | constant | 20 |

2.4. Supports on 2D member edge

| Name | 2D member Edge | Orig Coor | Pos x ₁ Pos x ₂ | X | Y | Z | Rx | Ry | Rz |
|-------|----------------|--------------------|---------------------------------------|----------|----------|-------|------|------|------|
| Sle11 | D6 1 | From start Rela | 0,000 1,000 | Flexible | Flexible | Rigid | Free | Free | Free |
| Sle12 | D8 1 | From start Rela | 0,000 1,000 | Flexible | Flexible | Rigid | Free | Free | Free |
| Sle13 | D9 1 | From start Rela | 0,000 1,000 | Flexible | Flexible | Rigid | Free | Free | Free |
| Sle14 | D7 | From start | 0,000 | Flexible | Flexible | Rigid | Free | Free | Free |

| Name | 2D member | Orig | Pos x ₁ | X | Y | Z | Rx | Ry | Rz |
|------|-----------|------|--------------------|---|---|---|----|----|----|
| | Edge | Coor | Pos x ₂ | | | | | | |
| | 1 | Rela | 1,000 | | | | | | |

2.5. Materials

Steel EC3

| Name | ρ [kg/m ³] | E_{mod} [MPa] | μ | Limit inférieure [mm] | Limite supérieure [mm] | F_y [kPa] | F_u [kPa] | Colour |
|-------|--------------------------------|--------------------|--------------------|--------------------------|---------------------------|----------------|----------------|--------|
| | | G_{mod} [MPa] | α [m/mK] | | | | | |
| S 235 | 7850,00 | 2,1000e+05 | 0,3 | 0 | 40 | 235000,000 | 360000,000 | ■ |
| | | 8,0769e+04 | 0,01e-003 | 40 | 80 | 215000,000 | 360000,000 | |

3. LOAD

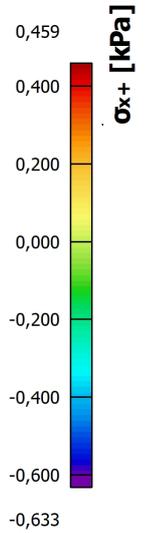
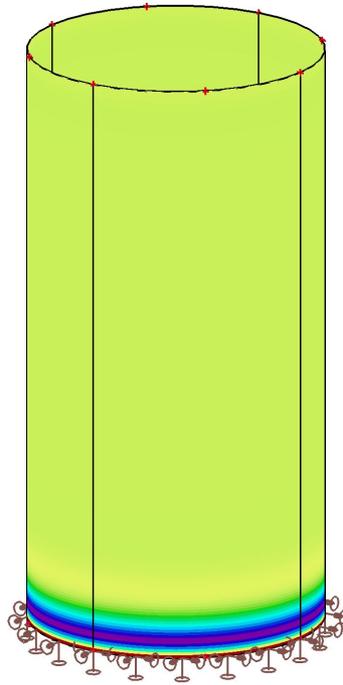
3.1. Load cases

| Name | Description Spec | Action type Load type | Load group | Direction |
|------|---------------------|--------------------------|------------|-----------|
| LC1 | Poids propre | Permanent Self weight | LG1 | -Z |

4. RESULTS

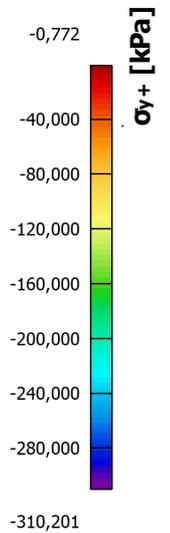
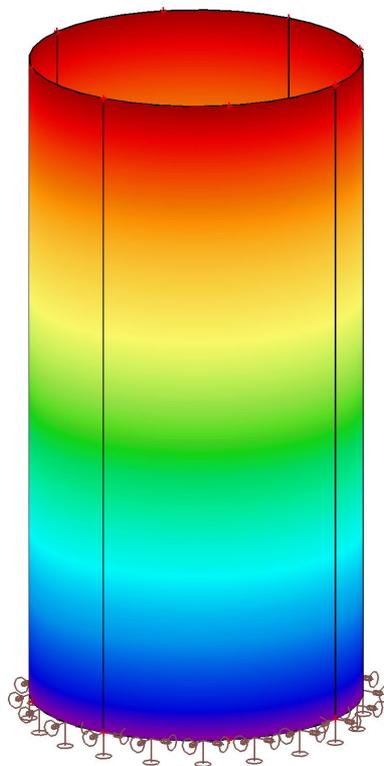
4.1. 2D stress/strain; σ_{x+}

Valeur: σ_{x+}
 Calcul linéaire
 Cas de charge: LC1
 Extrême: Global
 Sélection: Tout
 Position: Aux centres. Système: SCL
 maillage EF



4.2. 2D stress/strain; σ_{y+}

Valeur: σ_{y+}
 Calcul linéaire
 Cas de charge: LC1
 Extrême: Global
 Sélection: Tout
 Position: Aux centres. Système: SCL
 maillage EF



4.3. 2D stress/strain

Linear calculation

Load case: LC1

Extreme: Global

Selection: All

Location: In centres. System: LCS mesh element

Basic stress

| Name | Mesh | Position [m] | Case | σ_{x+} | σ_{y+} | τ_{xy+} | τ_{xz} | τ_{yz} | |
|------|----------------|--------------------------|------|------------------------------|------------------------------------|------------------------------|--------------|---------------|-------|
| | | | | [kPa] | [kPa] | [kPa] | | | [kPa] |
| | | | | σ_{x-} | σ_{y-} | τ_{xy-} | | | |
| | | | | [kPa] | [kPa] | [kPa] | | | |
| D6 | Element: 415 | 0,574 -0,253 0,110 | LC1 | -0,633 0,269 | -301,066 -298,060 | 0,000 0,000 | 0,000 | 0,083 | |
| D6 | Element: 887 | 0,420 -0,285 0,230 | LC1 | -0,315 -0,231 | -290,461 -290,183 | 0,000 0,000 | 0,000 | 0,029 | |
| D6 | Element: 2 | 0,322 -0,292 0,010 | LC1 | 0,459 2,221 | -310,201 -304,327 | 0,000 0,000 | 0,000 | 0,023 | |
| D6 | Element: 15921 | 0,303 -0,293 3,990 | LC1 | 0,013 0,015 | -0,772 -0,768 | 0,000 0,000 | 0,000 | 0,001 | |
| D6 | Element: 1 | 0,303 -0,293 0,010 | LC1 | 0,459 2,221 | -310,201 -304,327 | 0,000 0,000 | 0,000 | 0,023 | |
| D6 | Element: 80 | 1,293 0,697 0,010 | LC1 | 0,459 2,221 | -310,201 -304,327 | 0,000 0,000 | 0,000 | 0,023 | |
| D6 | Element: 1681 | 0,303 -0,293 0,430 | LC1 | 0,024 -0,026 | -274,837 -275,003 | 0,000 0,000 | 0,000 | -0,004 | |
| D6 | Element: 329 | 0,459 -0,279 0,090 | LC1 | -0,589 0,517 | -302,947 -299,260 | 0,000 0,000 | 0,000 | 0,086 | |

4.4. 2D displacement

Linear calculation

Load case: LC1

Extreme: Global

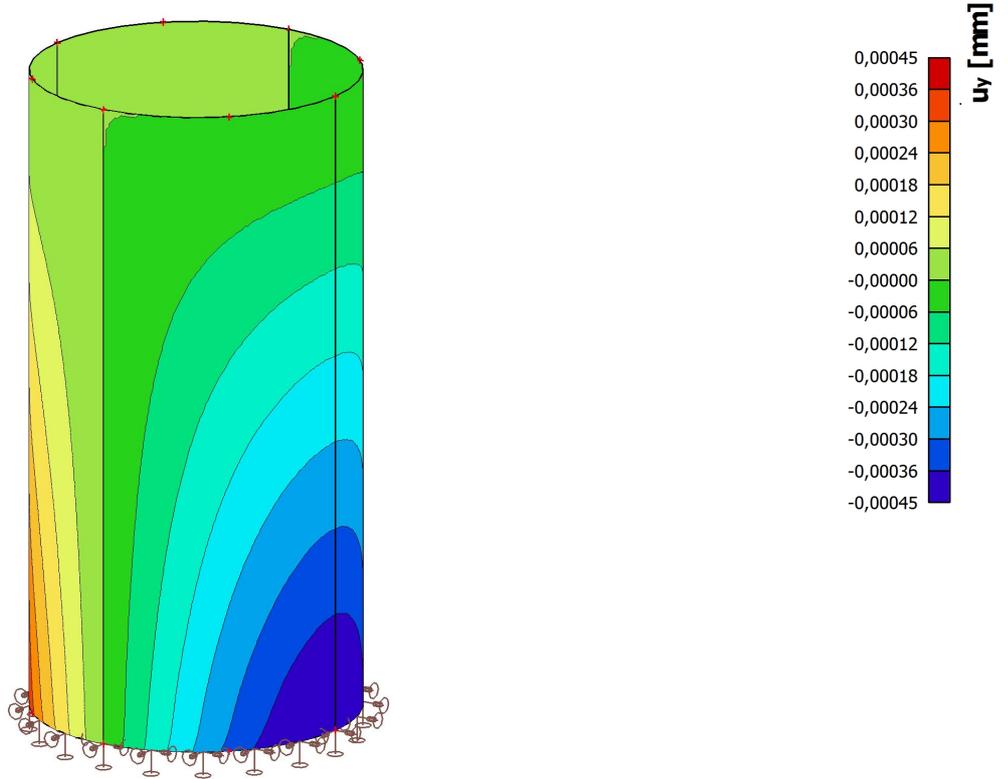
Selection: All

Location: In nodes avg. on macro. System: LCS mesh element

| Name | Mesh | Position [m] | Case | u_x | u_y | u_z | ϕ_x | ϕ_y | ϕ_z | U_{total} |
|------|-------------------------------|--------------------------|------|----------------|-----------------|----------------|------------|------------|------------|----------------|
| | | | | [mm] | [mm] | [mm] | [mrad] | [mrad] | [mrad] | [mm] |
| D6 | Element: 15921 Node: 16201 | 0,313 -0,293 4,000 | LC1 | 0,00000 | -0,00293 | 0,00000 | 0,0 | 0,0 | 0,0 | 0,00293 |
| D6 | Element: 81 Node: 163 | 0,313 -0,293 0,040 | LC1 | 0,00000 | -0,00006 | 0,00044 | 0,0 | 0,0 | 0,0 | 0,00044 |

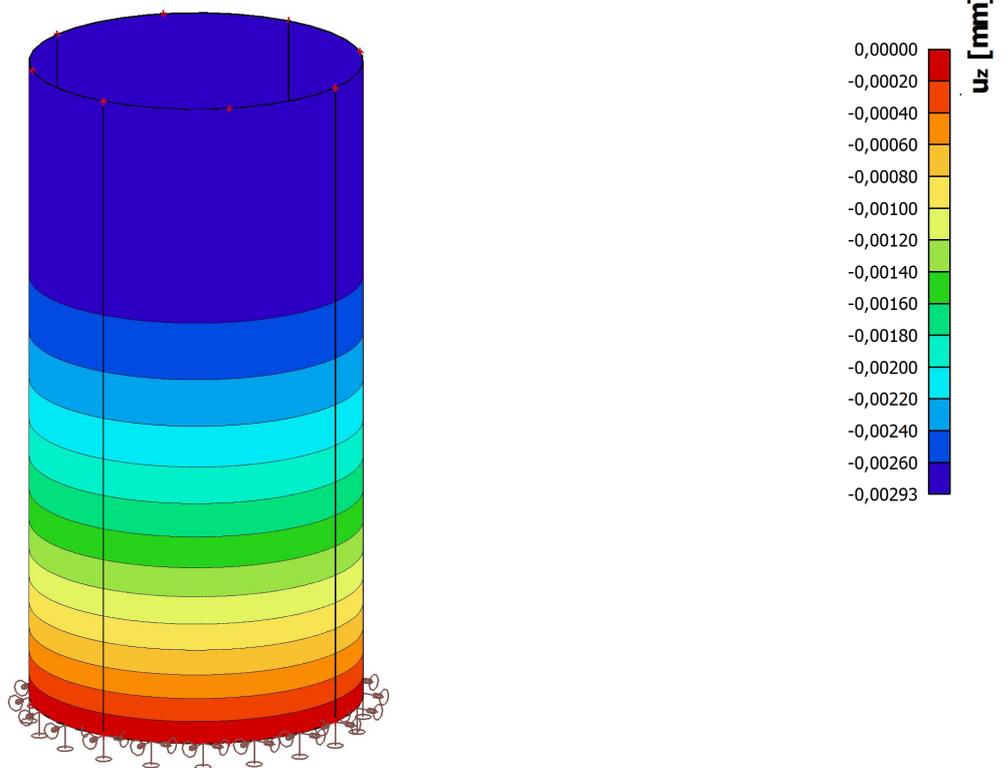
4.5. 2D displacement; u_y

Valeur: u_y
 Calcul linéaire
 Cas de charge: LC1
 Extrême: Global
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



4.6. 2D displacement; u_z

Valeur: u_z
 Calcul linéaire
 Cas de charge: LC1
 Extrême: Global
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



5. EXPECTED AFNOR RESULTS

σ_x (Whole height)= 0 kPa

σ_y (at bottom)= -314 kPa

Radial displacement = $4.49 \cdot 10^{-4}$ mm

Vertical displacement = $-2.99 \cdot 10^{-3}$ mm

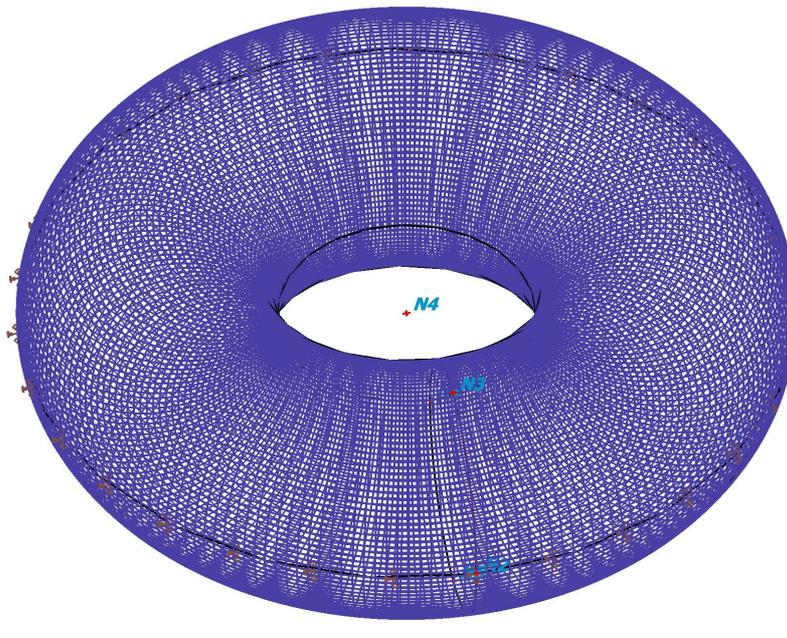
REFERENCE : "Guide de validation des progiciels de calcul de structures" AFNOR, 1990

1. TESTCASE DESCRIPTION

Torus under uniform internal pressure

2. MODEL

2.1. Analysis model



2.2. Nodes

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] |
|------|-------------|-------------|-------------|
| N1 | 1,000 | 0,000 | 0,000 |
| N2 | 3,000 | 0,000 | 0,000 |

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] |
|------|-------------|-------------|-------------|
| N3 | 2,000 | 0,000 | 1,000 |
| N4 | 0,000 | 0,000 | 0,000 |

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] |
|------|-------------|-------------|-------------|
| N5 | 2,000 | 0,000 | -1,000 |

2.3. 2D members

| Name | Layer | Type | Element type | Material | Thickness type | Th. [mm] |
|------|---------|------------|--------------|----------|----------------|----------|
| D1 | Calque1 | coque (98) | Standard | S 235 | constant | 20 |
| D2 | Calque1 | coque (98) | Standard | S 235 | constant | 20 |

2.4. Supports on 2D member edge

| Name | 2D member Edge | Orig Coor | Pos x ₁ Pos x ₂ | X | Y | Z | Rx | Ry | Rz |
|------|----------------|------------|---------------------------------------|----------|----------|-------|------|------|------|
| Sle1 | D1 | From start | 0.000 | Flexible | Flexible | Rigid | Free | Free | Free |
| | D2 | Rela | 1.000 | | | | | | |

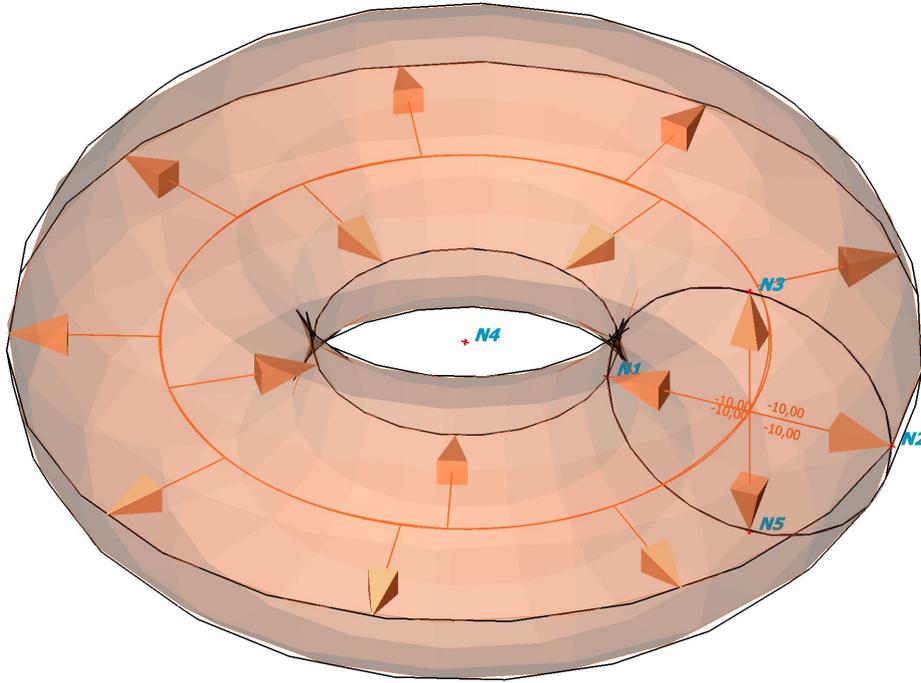
2.5. Materials

Steel EC3

| Name | ρ [kg/m ³] | E _{mod} [MPa] | μ | Limit inférieure [mm] | Limite supérieure [mm] | F _y [MPa] | F _u [MPa] | Colour |
|-------|------------------------|------------------------|-----------|-----------------------|------------------------|----------------------|----------------------|--------|
| | | G _{mod} [MPa] | α [m/mK] | | | | | |
| S 235 | 7850,00 | 2,1000e+05 | 0.3 | 0 | 40 | 235,00 | 360,00 | ■ |
| | | 8,0769e+04 | 0,01e-003 | 40 | 80 | 215,00 | 360,00 | |

3. LOAD

3.1. LC2 / Tot. value



3.2. Load cases

| Name | Description | Action type | Load group |
|------|-------------|-----------------------|------------|
| | Spec | Load type | |
| LC2 | PERMANENT | Permanent Standard | LG1 |

3.3. Generated free loads

| Name | Load case | 2D member | Dir | Type load | Original Load | q [kN/m ²] Value - P [kN/m] | System |
|------|-----------------|-----------|--------------|-----------|---------------|--|----------------------|
| | | | Distribution | Type | | | Location |
| GFF1 | LC2 - PERMANENT | D1 | Z | Surface | FF1 | -10,00 | Member LCS Length |
| GFF2 | LC2 - PERMANENT | D2 | Z | Surface | FF1 | -10,00 | Member LCS Length |

3.4. Free surface load

| Name | Load case | Dir | Type | Distribution | q [kN/m ²] | Validity | Select | System | Location |
|------|-----------------|-----|-------|--------------|---------------------------|----------|--------|------------|----------|
| FF1 | LC2 - PERMANENT | Z | Force | Uniform | -10,00 | All | Auto | Member LCS | Length |

4. RESULTS

4.1. 3D stress; σ_x (1D/2D)

Valeur: σ_x (1D/2D)

Calcul linéaire

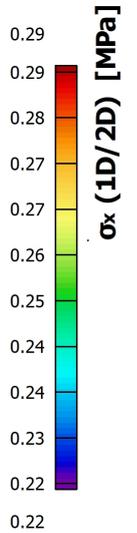
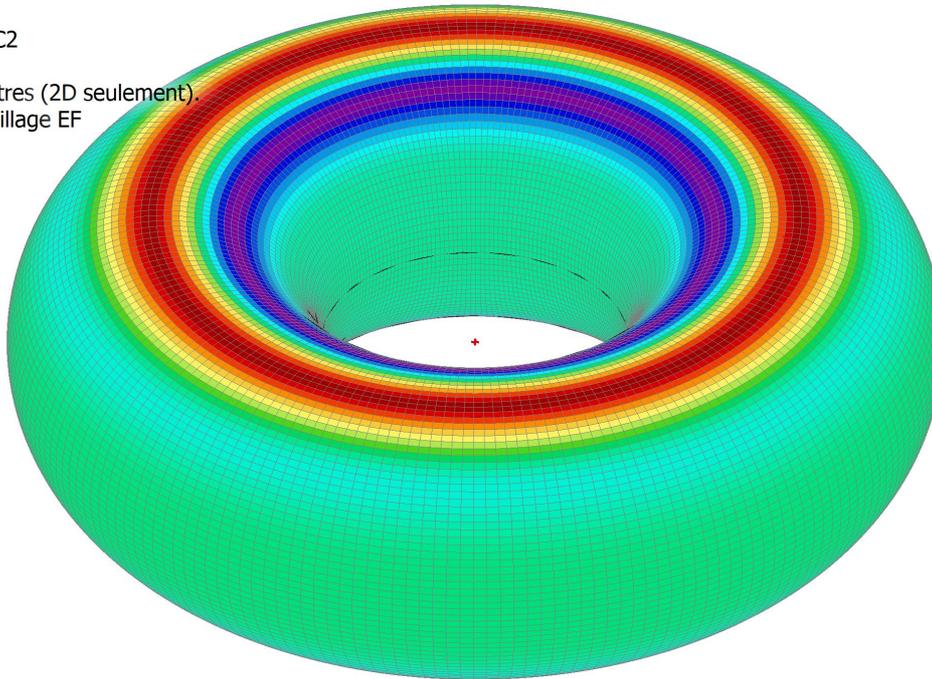
Cas de charge: LC2

Sélection: Tout

Position: Aux centres (2D seulement).

Système: SCL maillage EF

Valeurs de base



4.2. 3D stress; σ_y (2D)

Valeur: σ_y (2D)

Calcul linéaire

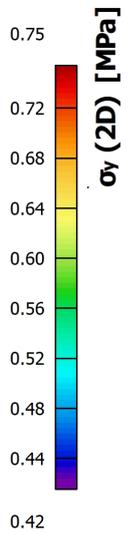
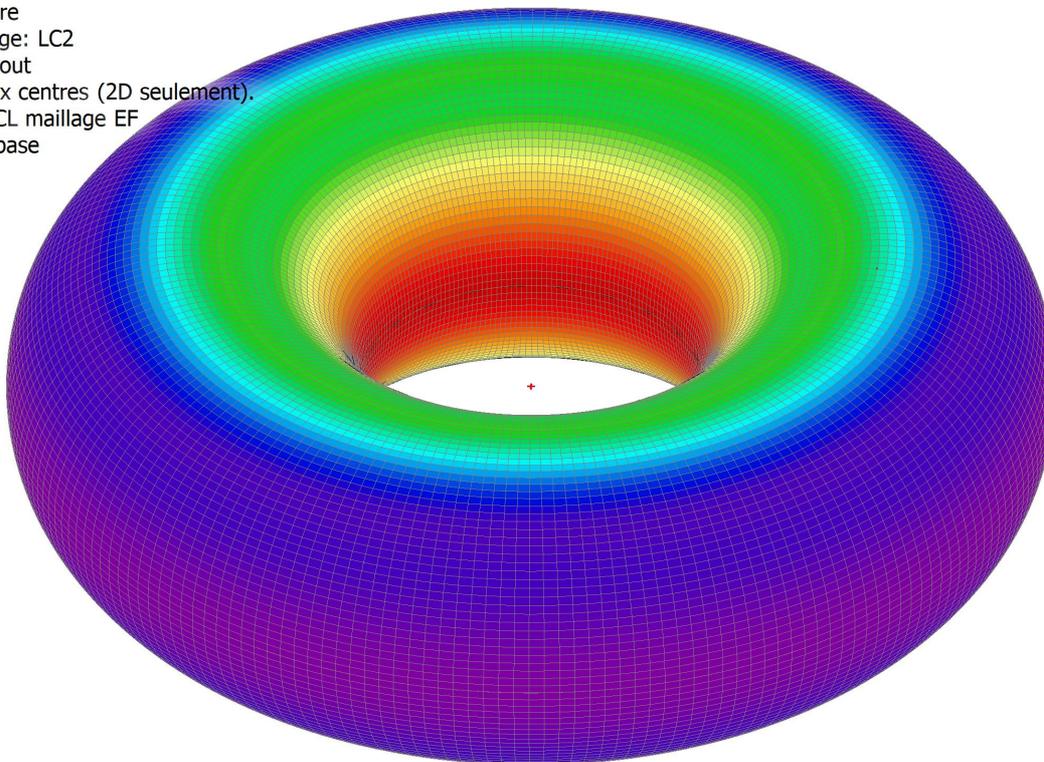
Cas de charge: LC2

Sélection: Tout

Position: Aux centres (2D seulement).

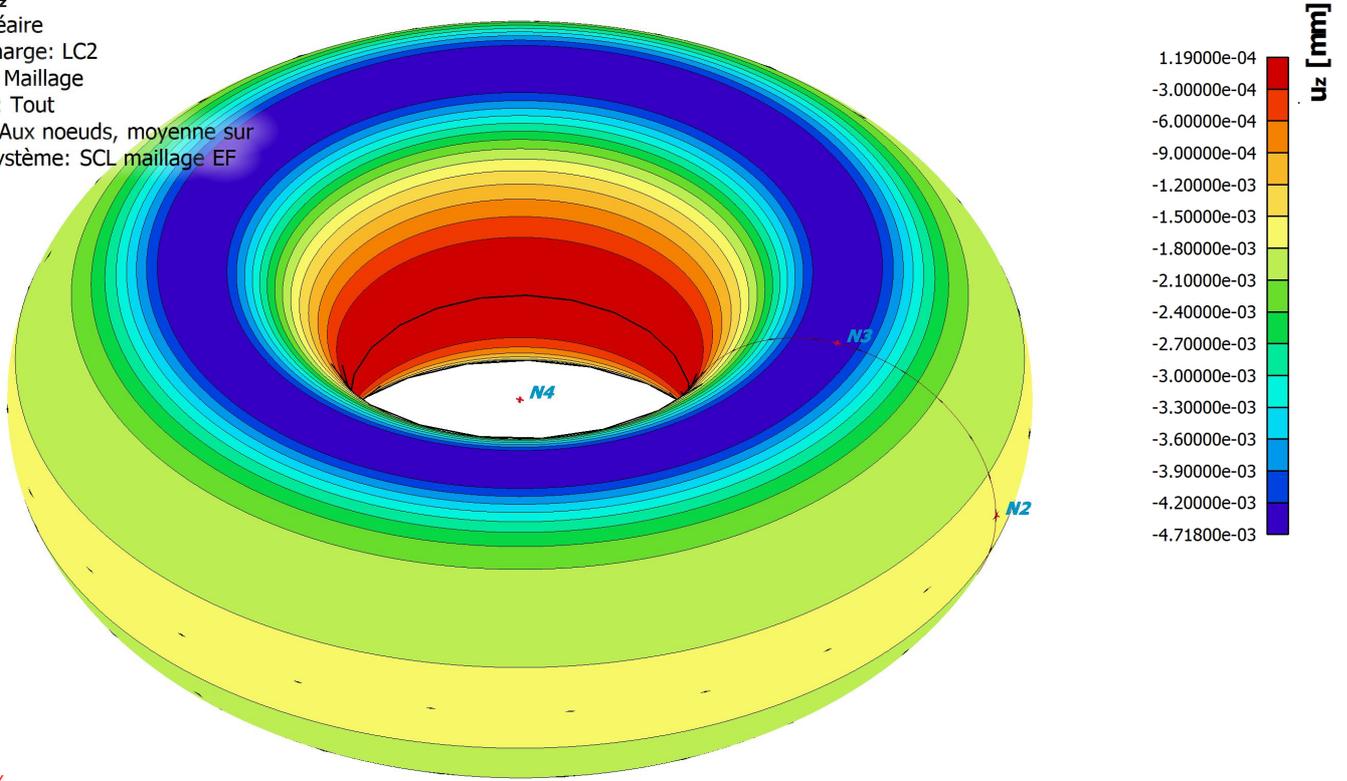
Système: SCL maillage EF

Valeurs de base



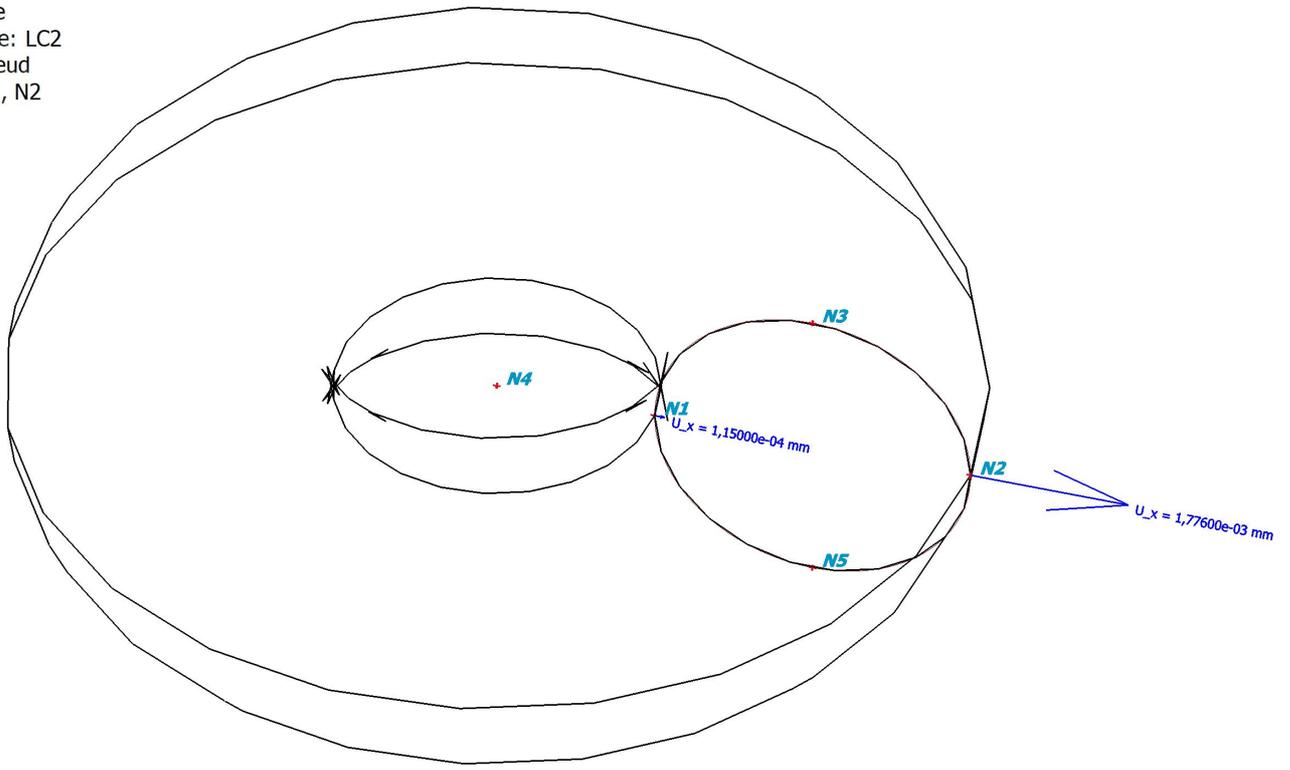
4.3. 2D displacement; u_z

Valeur: u_z
 Calcul linéaire
 Cas de charge: LC2
 Extrême: Maillage
 Sélection: Tout
 Position: Aux noeuds, moyenne sur macro. Système: SCL maillage EF



4.4. Displacement of nodes; U_x

Valeur: U_x
 Calcul linéaire
 Cas de charge: LC2
 Extrême: Noeud
 Sélection: N1, N2



4.5. 3D stress

Linear calculation

Load case: LC2

Selection: All

Location: In centres (for 2D only). System: LCS mesh element

Basic magnitudes

Results on 2D member

Extreme 2D: Global

| Name | Mesh | Position [m] | Case | σ_{x+} | σ_{y+} | τ_{xy+} | τ_{xz} | τ_{yz} |
|------|----------------|---------------------------|------|---------------------|----------------------------|----------------------------|-------------|-------------|
| | | | | [MPa] | [MPa] | [MPa] | | |
| | | | | σ_{x-} | σ_{y-} | τ_{xy-} | | |
| | | | | [MPa] | [MPa] | [MPa] | | |
| D1 | Element: 5617 | 1,733 0,025 0,963 | LC2 | 0,22 0,24 | 0,50 0,57 | 0,00 0,00 | 0,00 | 0,00 |
| D1 | Element: 7993 | 2,266 0,033 0,963 | LC2 | 0,27 0,28 | 0,48 0,46 | 0,00 0,00 | 0,00 | 0,00 |
| D1 | Element: 4753 | 1,550 0,023 0,893 | LC2 | 0,24 0,22 | 0,57 0,57 | 0,00 0,00 | 0,00 | 0,00 |
| D1 | Element: 7129 | 2,073 0,030 0,997 | LC2 | 0,26 0,29 | 0,45 0,52 | 0,00 0,00 | 0,00 | 0,00 |
| D1 | Element: 13609 | 2,999 0,044 0,025 | LC2 | 0,25 0,25 | 0,42 0,42 | 0,00 0,00 | 0,00 | 0,00 |
| D2 | Element: 15029 | -0,919 0,479 -0,267 | LC2 | 0,25 0,25 | 0,74 0,73 | 0,00 0,00 | 0,00 | 0,00 |
| D2 | Element: 13934 | -1,000 0,044 -0,025 | LC2 | 0,25 0,25 | 0,75 0,74 | 0,00 0,00 | 0,00 | 0,00 |
| D1 | Element: 4834 | -1,112 1,080 0,893 | LC2 | 0,24 0,22 | 0,57 0,57 | 0,00 0,00 | 0,00 | 0,00 |
| D1 | Element: 6697 | 1,975 0,029 0,999 | LC2 | 0,24 0,28 | 0,45 0,55 | 0,00 0,00 | 0,00 | 0,00 |
| D1 | Element: 7345 | 2,122 0,031 0,992 | LC2 | 0,26 0,29 | 0,46 0,51 | 0,00 0,00 | 0,00 | 0,00 |

4.6. Displacement of nodes

Linear calculation

Load case: LC2

Extreme: Global

Selection: N1, N2

| Name | Case | U_x [mm] |
|------|------|--------------------|
| N1 | LC2 | 1,15000e-04 |
| N2 | LC2 | 1,77600e-03 |

5. EXPECTED AFNOR RESULTS

σ_x (Whole torus)= 0.25 MPa

σ_y (Max)= 0.75 MPa

σ_y (Min)= 0.42 MPa

Radial (external) displacement (N1 ux)= 1.19*e-4 mm

Radial (internal) displacement (N2 ux)= 1.79*e-3 mm

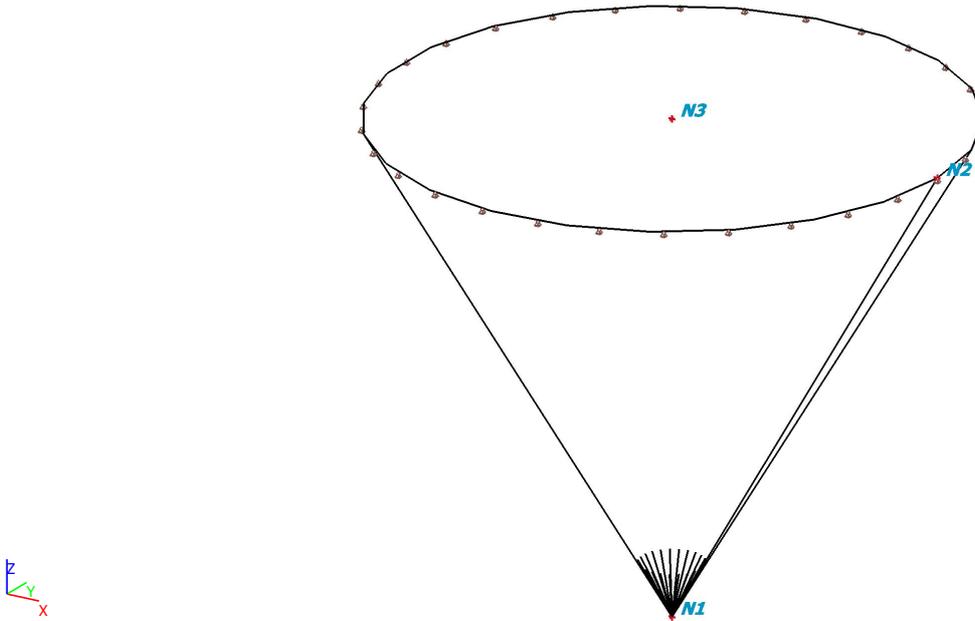
REFERENCE : "Guide de validation des progiciels de calcul de structures" AFNOR, 1990

1. TESTCASE DESCRIPTION

Thin-walled cone subjected to uniform internal pressure
Specification: Shell - Cone - Material: elastic - Pressure.

2. MODEL

2.1. Analysis model



2.2. Nodes

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] |
|------|-------------|-------------|-------------|
| N1 | 0,000 | 0,000 | 0,000 |
| N2 | 1,000 | 0,000 | 1,732 |
| N3 | 0,000 | 0,000 | 1,732 |

2.3. 2D members

| Name | Layer | Type | Element type | Material | Thickness type | Th. [mm] |
|------|---------|------------|--------------|----------|----------------|----------|
| D1 | Calque1 | coque (98) | Standard | S 235 | constant | 20 |

2.4. Supports on 2D member edge

| Name | 2D member Edge | Orig Coor | Pos x ₁ Pos x ₂ | X | Y | Z | Rx | Ry | Rz |
|------|----------------|--------------------|---------------------------------------|-------|-------|-------|------|------|------|
| Sle1 | D1 2 | From start Rela | 0.000 1.000 | Rigid | Rigid | Rigid | Free | Free | Free |

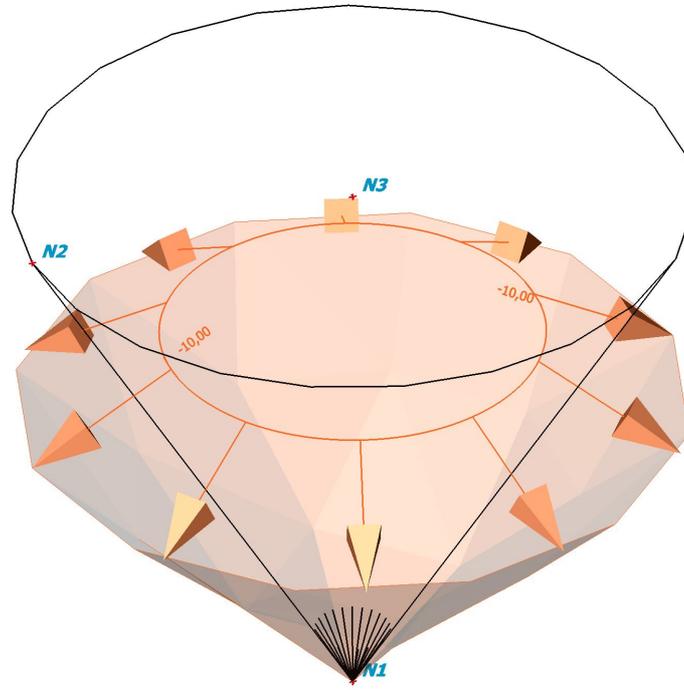
2.5. Materials

Steel EC3

| Name | ρ [kg/m ³] | E _{mod} [MPa] | μ | Limit inférieure [mm] | Limite supérieure [mm] | F _y [MPa] | F _u [MPa] | Colour |
|-------|------------------------|------------------------|-----------|-----------------------|------------------------|----------------------|----------------------|--------|
| | | G _{mod} [MPa] | α [m/mK] | | | | | |
| S 235 | 7850,00 | 2,1000e+05 | 0.3 | 0 | 40 | 235,000 | 360,000 | ■ |
| | | 8,0769e+04 | 0,01e-003 | 40 | 80 | 215,000 | 360,000 | |

3. LOAD

3.1. LC2 / Tot. value



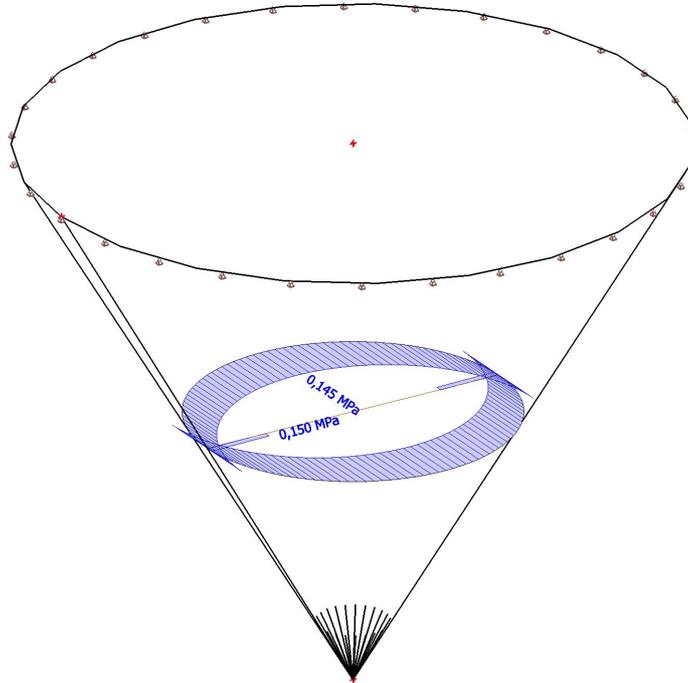
3.2. Free surface load

| Name | Load case | Dir | Type | Distribution | q [kN/m ²] | Validity | Select | System | Location |
|------|-----------------|-----|-------|--------------|---------------------------|----------|--------|------------|----------|
| FF1 | LC2 - Permanent | Z | Force | Uniform | -10,00 | All | Auto | Member LCS | Length |

4. RESULTS

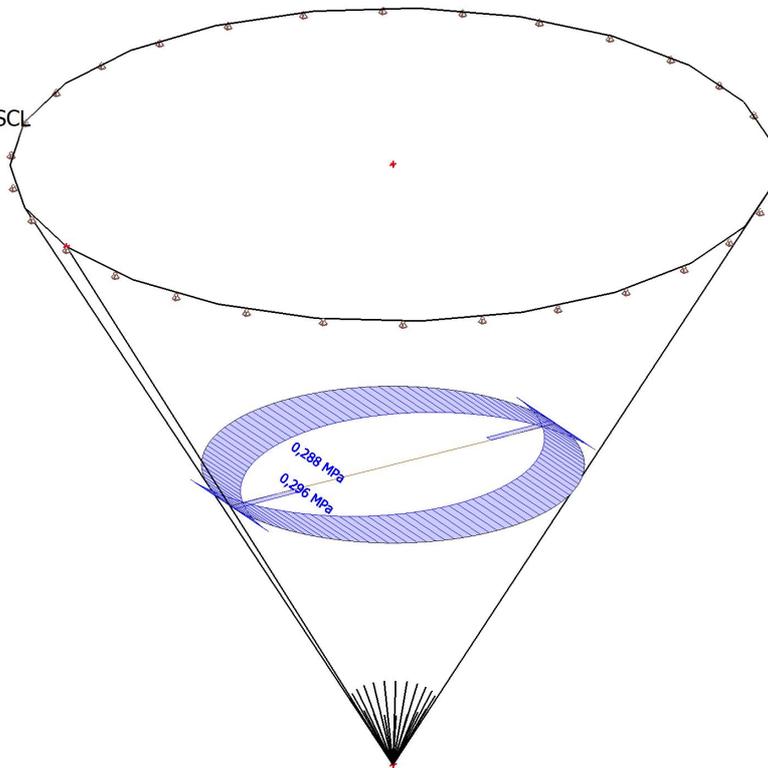
4.1. 2D stress/strain; σ_{y+}

Valeur: σ_{y+}
 Calcul linéaire
 Cas de charge: LC2
 Extrême: Global
 Sélection: Tout
 Position: Aux centres. Système: SCL
 maillage EF



4.2. 2D stress/strain; σ_{x+}

Valeur: σ_{x+}
 Calcul linéaire
 Cas de charge: LC2
 Extrême: Global
 Sélection: Tout
 Position: Aux centres. Système: SCL
 maillage EF



4.3. 2D stress/strain

Linear calculation

Load case: LC2

Extreme: Global

Selection: All

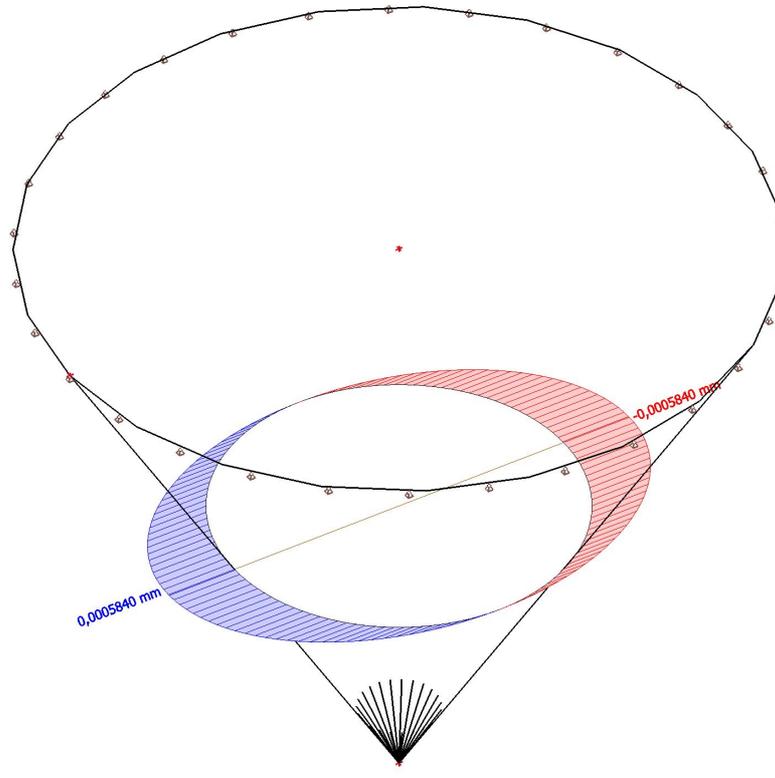
Location: In centres. System: LCS mesh element

Basic stress - Results on sections:

| Name | Mesh | Position [m] | Case | σ_{x+} | σ_{y+} | T_{xy+} | T_{xz} | T_{yz} |
|------|---------------|---------------------------|------|------------------------------|------------------------------|-----------------------|--------------|--------------|
| | | | | [MPa] | [MPa] | [MPa] | | |
| | | | | σ_{x-} | σ_{y-} | T_{xy-} | | |
| | | | | [MPa] | [MPa] | [MPa] | | |
| SE1 | Element: 3377 | -0,478 -0,147 0,866 | LC2 | 0,288 0,282 | 0,145 0,140 | 0,000 0,000 | 0,000 | 0,000 |
| SE1 | Element: 3660 | 0,312 0,391 0,866 | LC2 | 0,296 0,289 | 0,150 0,142 | 0,000 0,000 | 0,000 | 0,000 |
| SE1 | Element: 3351 | 0,012 -0,500 0,866 | LC2 | 0,288 0,282 | 0,145 0,140 | 0,000 0,000 | 0,000 | 0,000 |
| SE1 | Element: 3347 | 0,111 -0,487 0,866 | LC2 | 0,288 0,282 | 0,145 0,140 | 0,000 0,000 | 0,000 | 0,000 |
| SE1 | Element: 3638 | 0,062 0,496 0,866 | LC2 | 0,296 0,289 | 0,150 0,142 | 0,000 0,000 | 0,000 | 0,000 |
| SE1 | Element: 3674 | 0,427 0,261 0,866 | LC2 | 0,296 0,289 | 0,150 0,142 | 0,000 0,000 | 0,000 | 0,000 |
| SE1 | Element: 3331 | 0,427 -0,261 0,866 | LC2 | 0,288 0,282 | 0,145 0,140 | 0,000 0,000 | 0,000 | 0,000 |
| SE1 | Element: 3600 | -0,367 0,340 0,866 | LC2 | 0,296 0,289 | 0,150 0,142 | 0,000 0,000 | 0,000 | 0,000 |
| SE1 | Element: 3367 | -0,349 -0,358 0,866 | LC2 | 0,288 0,282 | 0,145 0,140 | 0,000 0,000 | 0,000 | 0,000 |
| SE1 | Element: 3320 | 0,500 0,000 0,866 | LC2 | 0,288 0,282 | 0,145 0,140 | 0,000 0,000 | 0,000 | 0,000 |
| SE1 | Element: 3696 | 0,500 0,004 0,866 | LC2 | 0,296 0,289 | 0,150 0,142 | 0,000 0,000 | 0,000 | 0,000 |

4.4. 2D displacement; u_x

Valeur: u_x
Calcul linéaire
Cas de charge: LC2
Extrême: Elément
Sélection: Tout
Position: Aux noeuds, moyenne.
Système: Global



4.5. 2D displacement

Linear calculation
Load case: LC2
Extreme: Member
Selection: SE1
Location: In nodes avg.. System: Global

Results on sections:

| Name | Mesh | Position [m] | Case | u_x [mm] | u_y [mm] |
|------|---------------|--------------------------|------|------------------|-------------------|
| SE1 | Element: 3350 | 0,012 -0,500 0,866 | LC2 | 0,0000150 | -0,0005840 |

5. EXPECTED AFNOR RESULTS

Results of the mid-height element:

$\sigma_y = 0.144$ MPa

$\sigma_x = 0.289$ MPa

Displacement radial = 0,5842 e-6 m

REFERENCE : "Guide de validation des progiciels de calcul de structures" AFNOR, 1990

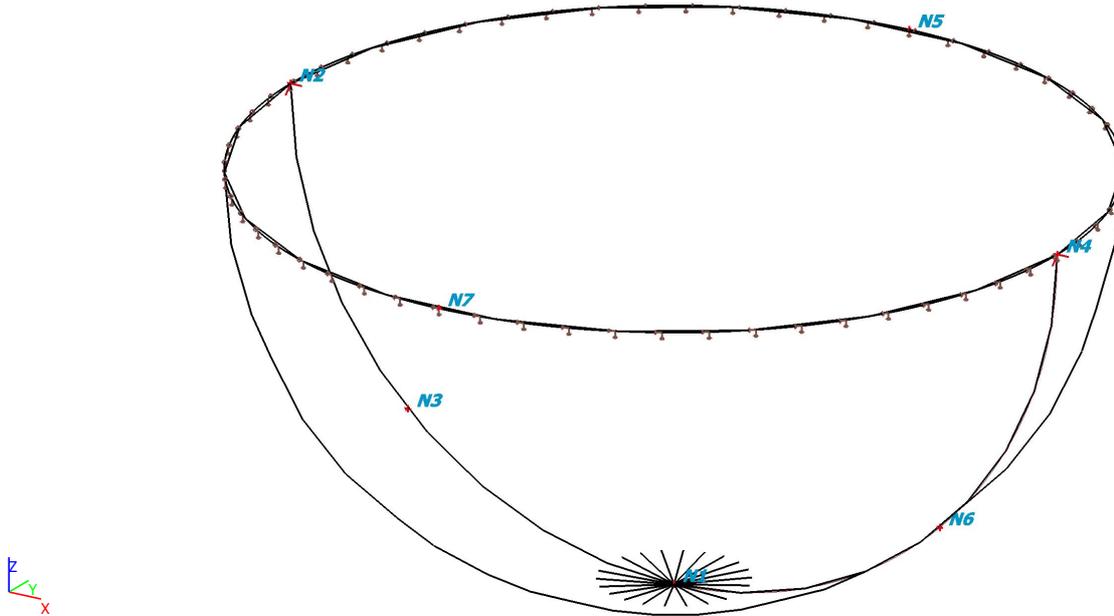
1. TESTCASE DESCRIPTION

Spherical shell subjected to a pressure

Codification: Shell - spherical cup - Material: elastic - Uniform pressure

2. MODEL

2.1. Analysis model



2.2. Nodes

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] |
|------|-------------|-------------|-------------|
| N1 | 0,000 | 0,000 | -1,000 |
| N2 | -1,000 | 0,000 | 0,000 |
| N3 | -0,694 | 0,000 | -0,720 |

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] |
|------|-------------|-------------|-------------|
| N4 | 1,000 | 0,000 | 0,000 |
| N5 | 0,000 | 1,000 | 0,000 |
| N6 | 0,694 | 0,000 | -0,720 |

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] |
|------|-------------|-------------|-------------|
| N7 | 0,000 | -1,000 | 0,000 |

2.3. 2D members

| Name | Layer | Type | Element type | Material | Thickness type | Th. [mm] |
|------|---------|------------|--------------|----------|----------------|----------|
| D1 | Calque1 | coque (98) | Standard | S 235 | constant | 20 |
| D3 | Calque1 | coque (98) | Standard | S 235 | constant | 20 |

2.4. Line supports on member

| Name | Type | Member System | Pos x ₁ Pos x ₂ | Coor Orig | X | Y | Z | Rx | Ry | Rz |
|------|------|---------------|--|--------------------|-------|------|-------|------|------|------|
| Slb1 | Line | B3 LCS | 0.000 1.000 | Rela From start | Rigid | Free | Rigid | Free | Free | Free |
| Slb2 | Line | B1 LCS | 0.000 1.000 | Rela From start | Rigid | Free | Rigid | Free | Free | Free |

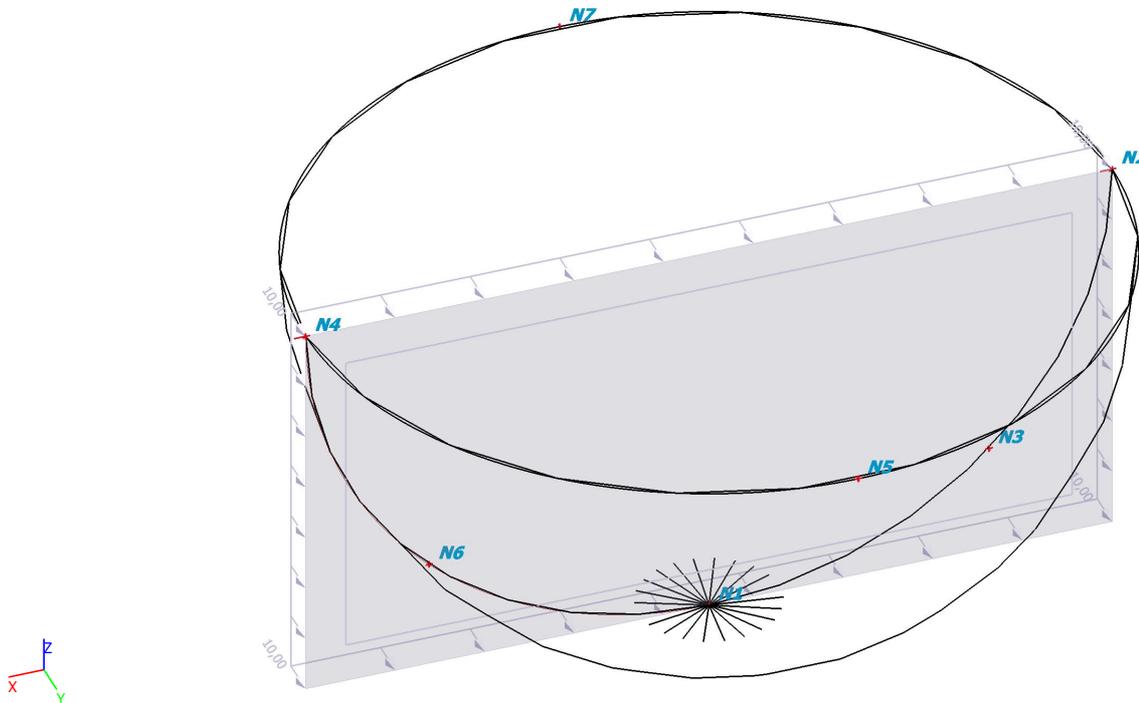
2.5. Materials

Steel EC3

| Name | ρ [kg/m ³] | E_{mod} [MPa] | μ | Limit inférieure [mm] | Limite supérieure [mm] | F_y [MPa] | F_u [MPa] | Colour |
|-------|--------------------------------|--------------------|--------------------|--------------------------|---------------------------|----------------|----------------|--------|
| | | G_{mod} [MPa] | α [m/mK] | | | | | |
| S 235 | 7850,00 | 2,1000e+05 | 0.3 | 0 | 40 | 235,00 | 360,00 | ■ |
| | | 8,0769e+04 | 0,01e-003 | 40 | 80 | 215,00 | 360,00 | |

3. LOAD

3.1. LC1 / Tot. value



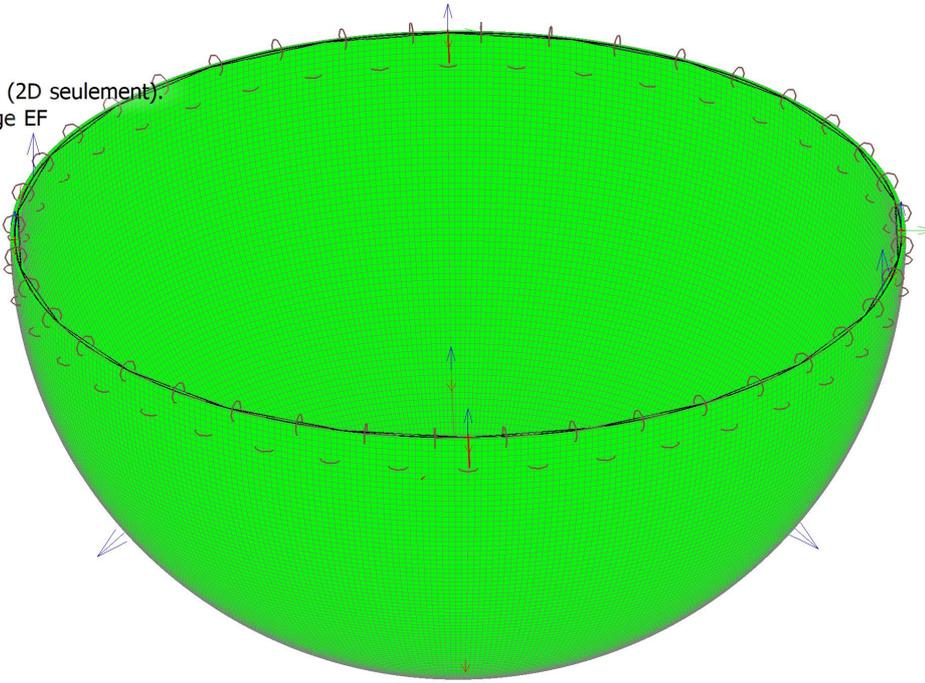
3.2. Free surface load

| Name | Load case | Dir | Type | Distribution | q [kN/m ²] | Validity | Select | System | Location |
|------|-----------------|-----|-------|--------------|---------------------------|----------|--------|------------|----------|
| FF1 | LC2 - Permanent | Z | Force | Uniform | 10,00 | All | Auto | Member LCS | Length |

4. RESULTS

4.1. 3D stress; σ_y (2D)

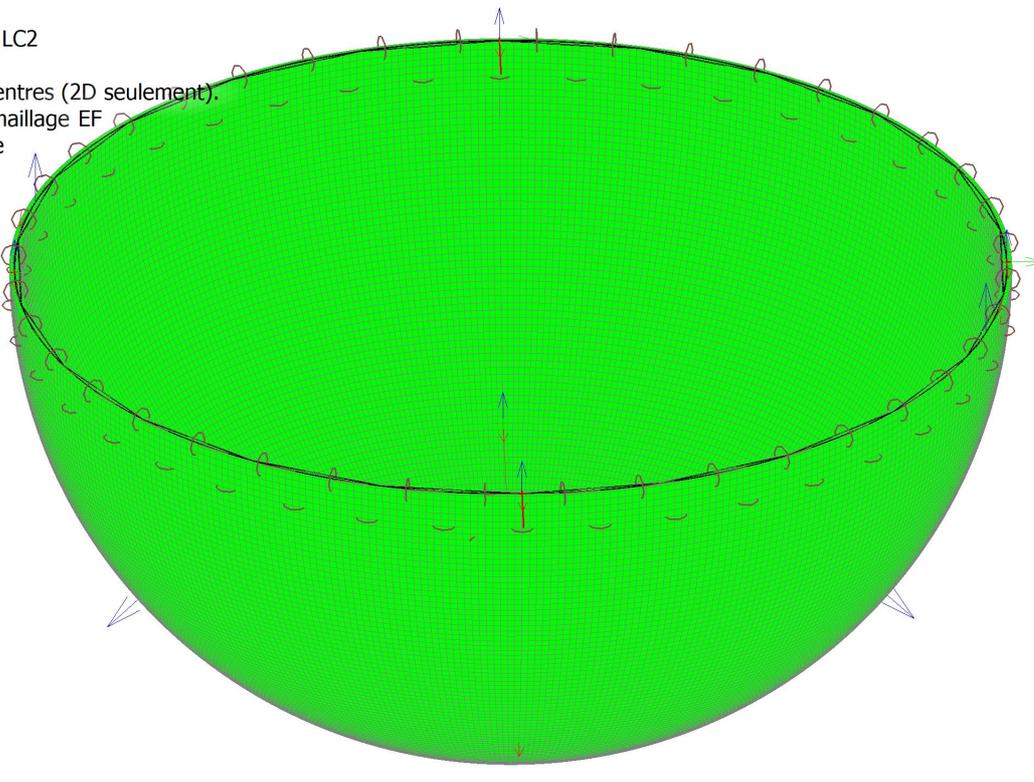
Valeur: σ_y (2D)
 Calcul linéaire
 Cas de charge: LC2
 Sélection: Tout
 Position: Aux centres (2D seulement).
 Système: SCL maillage EF
 Valeurs de base



Valeur constante 0.00
 σ_y (2D) [MPa]

4.2. 3D stress; σ_x (1D/2D)

Valeur: σ_x (1D/2D)
 Calcul linéaire
 Cas de charge: LC2
 Sélection: Tout
 Position: Aux centres (2D seulement).
 Système: SCL maillage EF
 Valeurs de base



Valeur constante 0.00
 σ_x (1D/2D) [MPa]

4.3. 2D stress/strain

Linear calculation

Load case: LC2

Extreme: Global

Selection: All

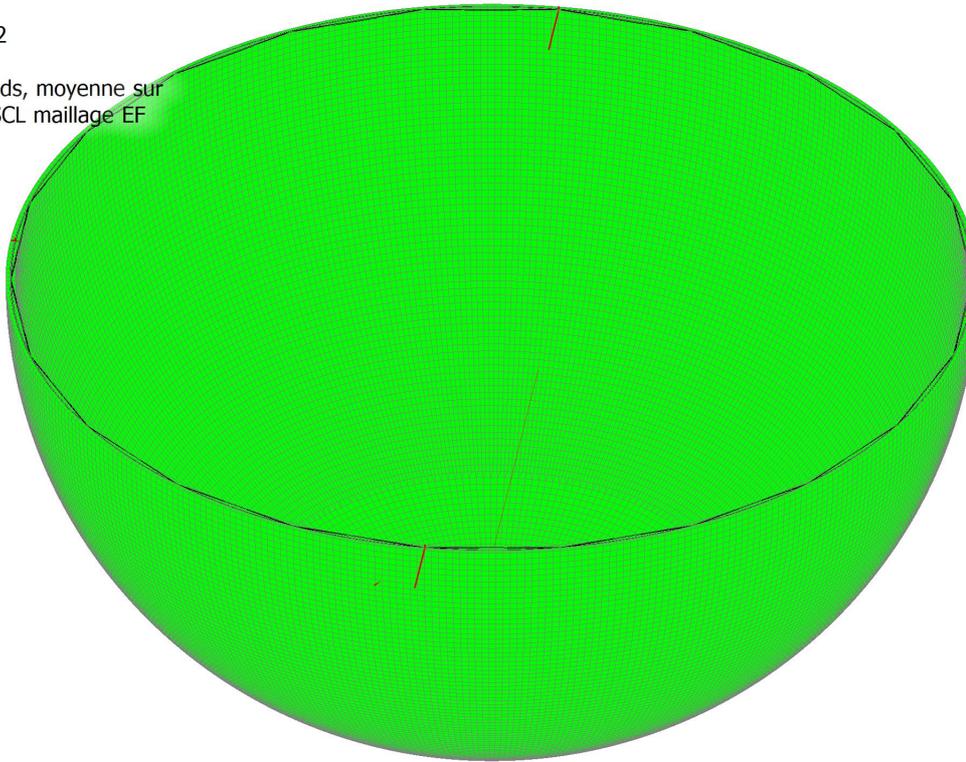
Location: In nodes avg. on macro. System: LCS mesh element

Basic stress - Results on sections:

| Name | Mesh | Position [m] | Case | σ_{x+} | σ_{y+} |
|------|----------------|--------------|------|---------------|---------------|
| | | | | [MPa] | [MPa] |
| | | | | σ_{x-} | σ_{y-} |
| | | | | [MPa] | [MPa] |
| SE1 | Element: 23876 | -0,707 | LC2 | 0,00 | 0,00 |
| | | 0,000 | | 0,00 | 0,00 |
| | | -0,707 | | | |

4.4. 3D displacement; u_z

Valeur: u_z
Calcul linéaire
Cas de charge: LC2
Sélection: Tout
Position: Aux noeuds, moyenne sur macro. Système: SCL maillage EF



Valeur constante 0,00e+00
 u_z [m]

4.5. 3D displacement

Linear calculation
Load case: LC2
Selection: All
Location: In nodes avg. on macro. System: LCS mesh element

Results on 2D member:

Extreme 2D: Global

| Name | Mesh | Position [m] | Case | u_{x+} [m] u_{x-} [m] | u_{y+} [m] u_{y-} [m] | u_{z+} [m] u_{z-} [m] | Φ_x [mrad] | Φ_y [mrad] | Φ_z [mrad] | U total+ [m] U total- [m] |
|------|--------------------------|--------------------------|------|------------------------------|------------------------------|------------------------------|-----------------|-----------------|-----------------|------------------------------|
| D1 | Element: 1 Node: 6055 | 0,007 0,013 -1,000 | LC2 | 0,00e+00 0,00e+00 | 0,00e+00 0,00e+00 | 0,00e+00 0,00e+00 | 0,0 | 0,0 | 0,0 | 0,00e+00 0,00e+00 |

5. EXPECTED AFNOR RESULTS

$\nabla\theta$; $\sigma_x = \sigma_y = 0.25$ MPa

$\theta = 90^\circ$; δR (uz) = 8,33 e-7 m

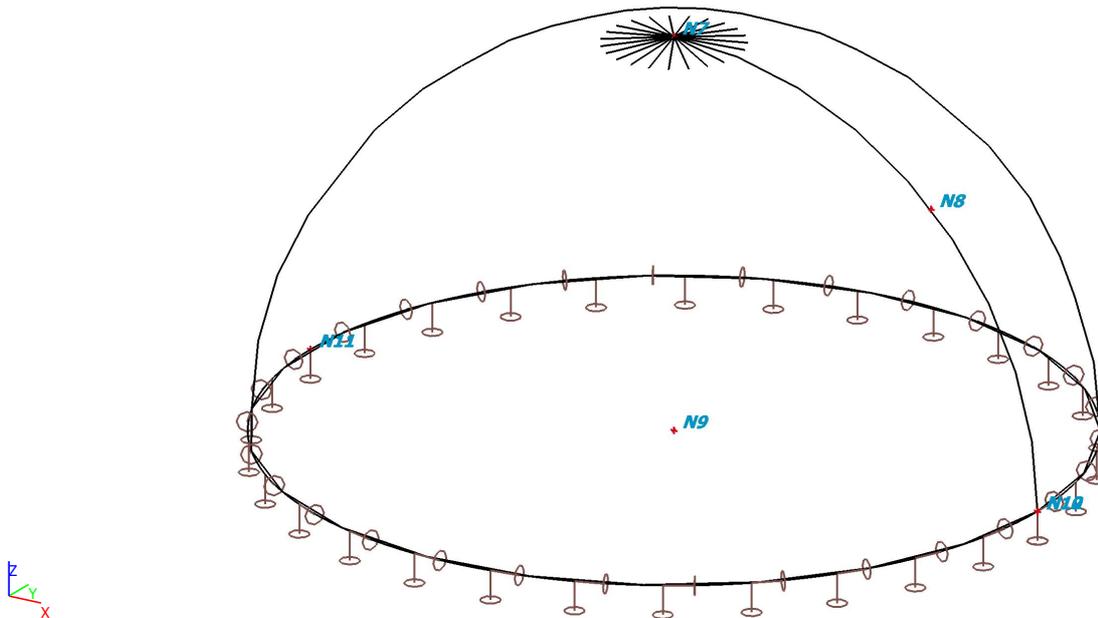
REFERENCE : "Guide de validation des progiciels de calcul de structures" AFNOR, 1990

1. TESTCASE DESCRIPTION

Spherical shell subjected to a moment
Specification: Shell - spherical cup - Material: elastic - Uniform moment.

2. MODEL

2.1. Analysis model



2.2. Nodes

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] |
|------|-------------|-------------|-------------|
| N1 | 1,048 | 0,000 | 0,000 |
| N7 | 0,048 | 0,000 | 1,000 |
| N8 | 0,755 | 0,000 | 0,707 |

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] |
|------|-------------|-------------|-------------|
| N9 | 0,048 | 0,000 | 0,000 |
| N10 | 1,048 | 0,000 | 0,000 |
| N11 | -0,952 | 0,000 | 0,000 |

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] |
|------|-------------|-------------|-------------|
| N12 | 1,048 | 0,001 | 0,000 |

2.3. 2D members

| Name | Layer | Type | Element type | Material | Thickness type | Th. [mm] |
|------|---------|------------|--------------|----------|----------------|----------|
| D2 | Calque1 | coque (98) | Standard | S 235 | constant | 20 |

2.4. Line supports

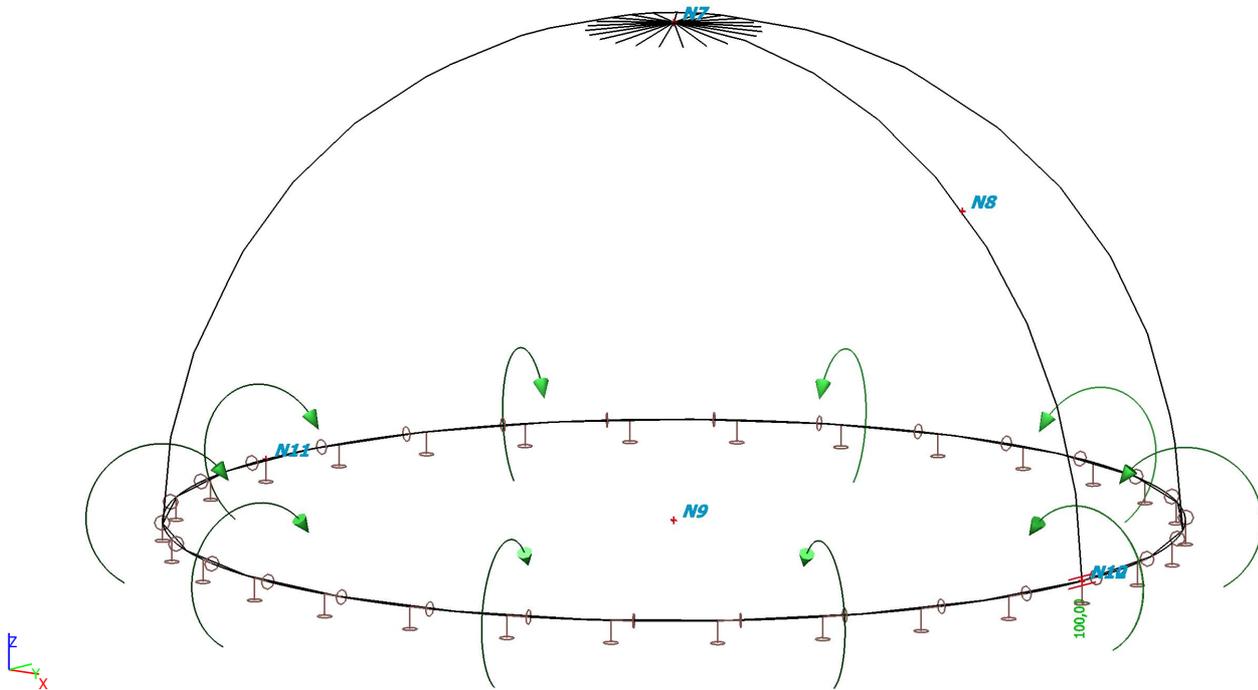
| Name | Type | Pos x ₁ | Pos x ₂ | Coor Orig | X | Y | Z | Rx | Ry | Rz |
|------|------|--------------------|--------------------|-----------------|-------|------|-------|------|------|------|
| Slb1 | Line | 0.000 | 1.000 | Rela From start | Rigid | Free | Rigid | Free | Free | Free |

2.5. Materials

Empty table

3. LOAD

3.1. LC1 / Tot. value

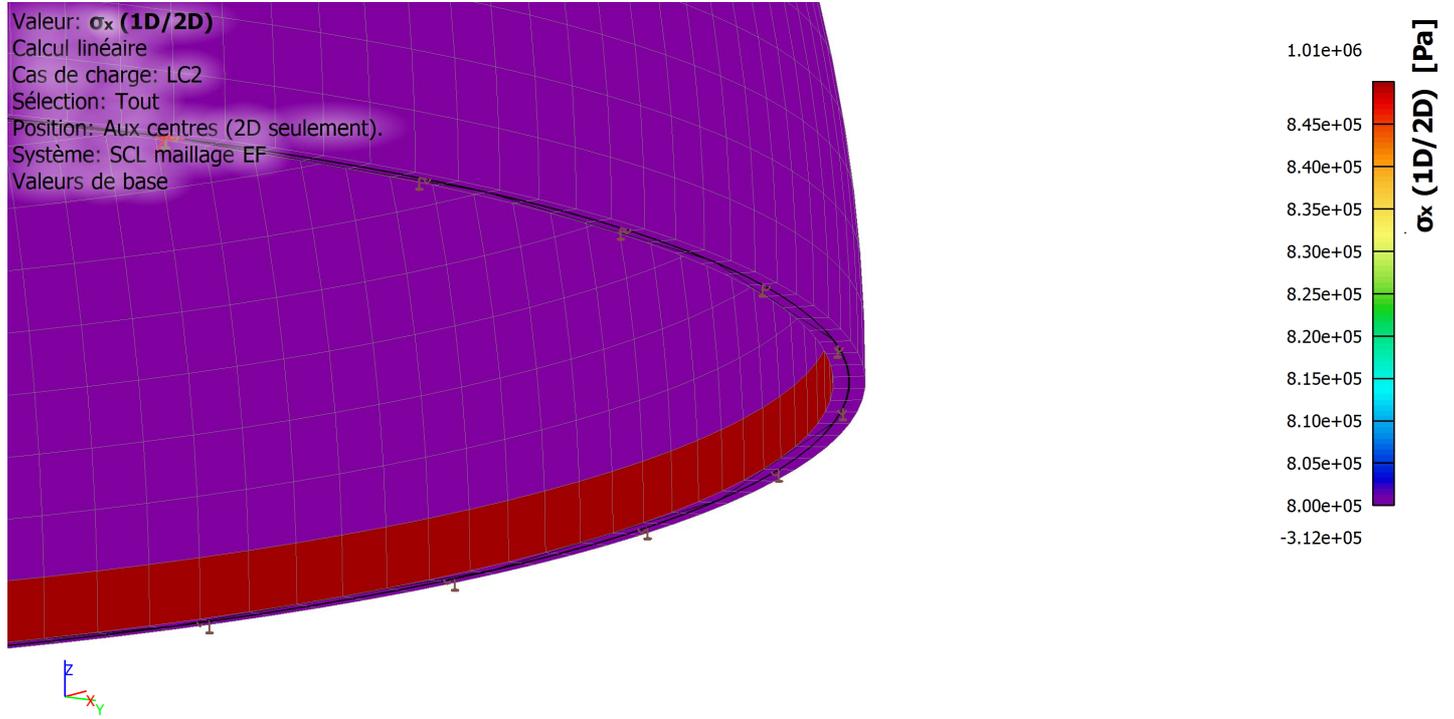


3.2. Line moment

| Name | Type | Dir | Value - M ₁ [Nm/m] | Pos x ₁ | Coor | Orig |
|------|--------|--------------|----------------------------------|--------------------|--------|------------|
| | System | Distribution | Value - M ₂ [Nm/m] | Pos x ₂ | Loc | |
| LM1 | Moment | Mx | 100,00 | 0.000 | Rela | From start |
| | LCS | Uniform | | 1.000 | Length | |

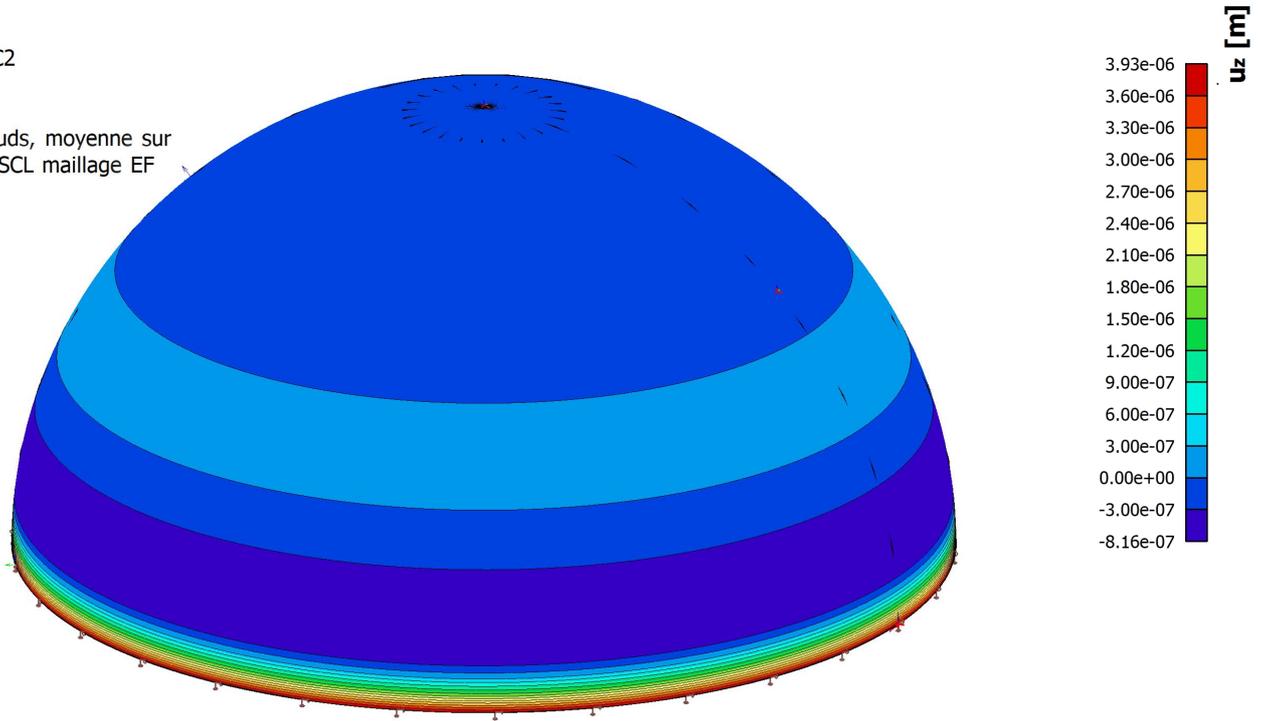
4. RESULTS

4.1. Horizontal stress on edge



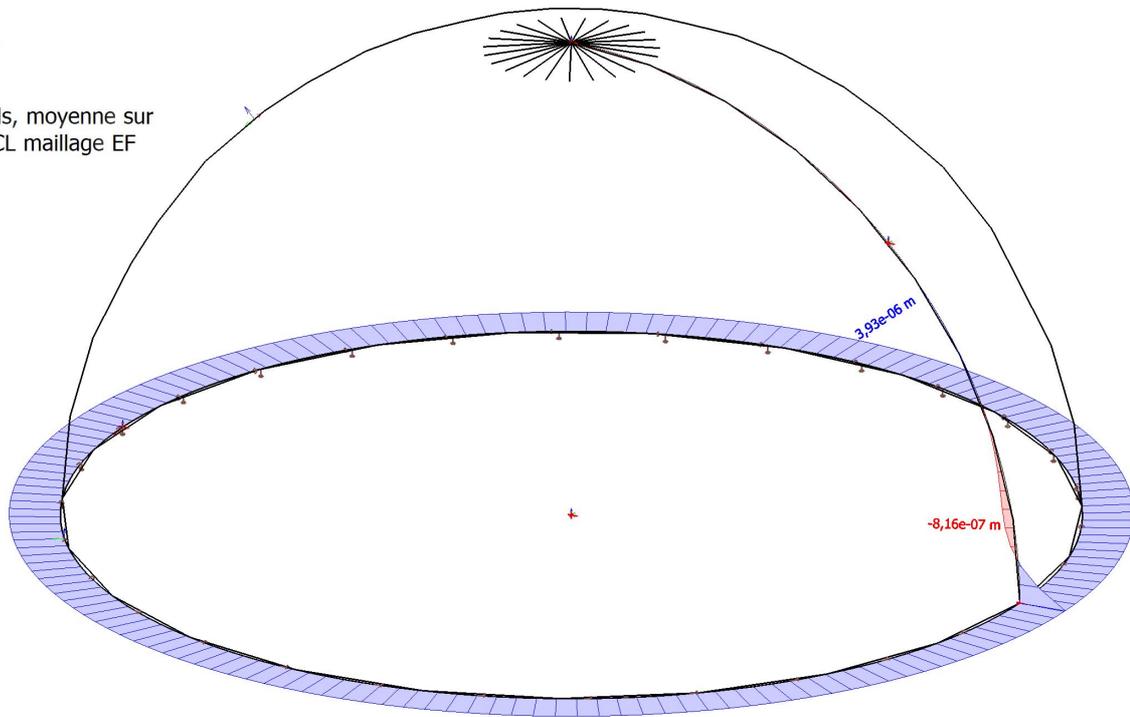
4.2. Displacement δR (m)

Valeur: u_z
Calcul linéaire
Cas de charge: LC2
Extrême: Global
Sélection: Tout
Position: Aux noeuds, moyenne sur macro. Système: SCL maillage EF



4.3. Displacement δR (m) on edge

Valeur: u_z
Calcul linéaire
Cas de charge: LC2
Extrême: Global
Sélection: Tout
Position: Aux noeuds, moyenne sur macro. Système: SCL maillage EF



Linear calculation

Load case: LC2

Extreme: Global

Selection: All

Location: In nodes avg. on macro. System: LCS mesh element

Results on edges:

| Name | Mesh | Position [m] | Case | u _x [m] | u _y [m] | u _z [m] | φ _x [mrad] | φ _y [mrad] | φ _z [mrad] | U _{total} [m] |
|-----------|------------------|-------------------------|------|--------------------|--------------------|--------------------|-----------------------|-----------------------|-----------------------|------------------------|
| D2/Edge 1 | Element: 3660 | 1,010 0,000 0,271 | LC2 | 0,00e+00 | 4,70e-08 | -4,70e-07 | 0,0 | 0,0 | 0,0 | 4,72e-07 |
| D2/Edge 2 | Element: 4820 | 0,048 1,000 0,000 | LC2 | 2,00e-09 | 4,50e-08 | 3,93e-06 | 0,1 | 0,0 | 0,0 | 3,93e-06 |

5. EXPECTED AFNOR RESULTS

Horizontal stress (at the extremity) = 8.26 e5 Pa

Horizontal stress (exterior plane) = 8.11 e5 Pa

RA dial displacement (at the extremity) = 3.93 e-6 m

REFERENCE : "Guide de validation des progiciels de calcul de structures" AFNOR, 1990

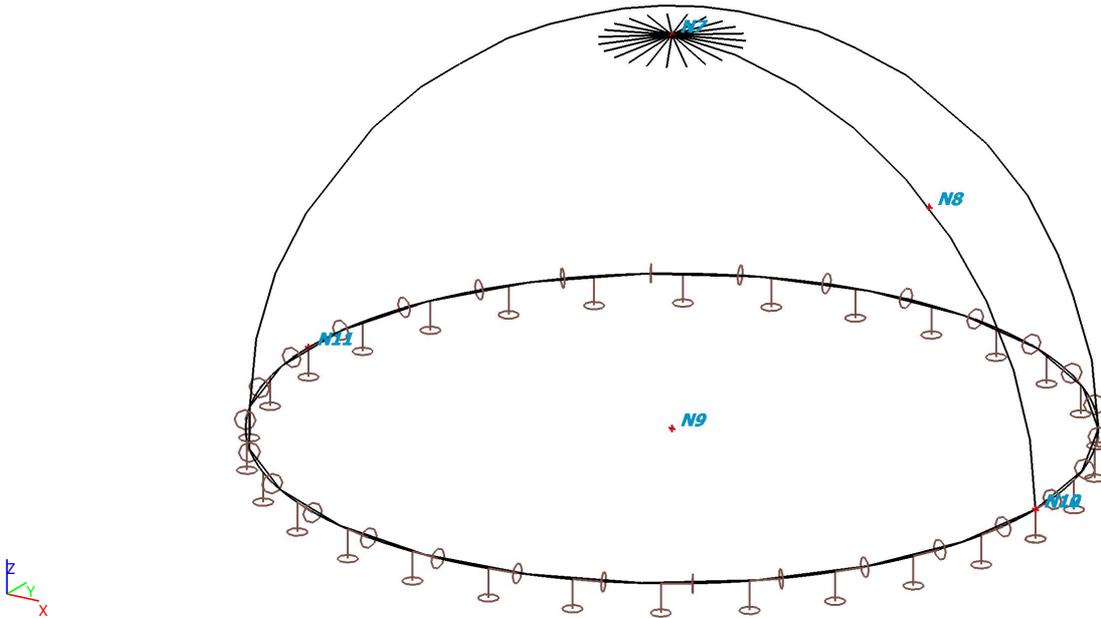
1. TESTCASE DESCRIPTION

Spherical shell

Specification: Shell - spherical cup - Material: elastic – Self weight

2. MODEL

2.1. Analysis model



2.2. 2D members

| Name | Layer | Type | Element type | Material | Thickness type | Th. [mm] |
|------|---------|------------|--------------|----------|----------------|----------|
| D2 | Calque1 | coque (98) | Standard | S 235 | constant | 20 |

2.3. Line supports

| Name | Type | Pos x ₁ | Coor Orig | X | Y | Z | Rx | Ry | Rz |
|------|------|--------------------|------------|-------|------|-------|------|------|------|
| Slb1 | Line | 0,000 | Rela | Rigid | Free | Rigid | Free | Free | Free |
| | | 1,000 | From start | | | | | | |

2.4. Materials

Empty table

3. LOAD

3.1. Load cases

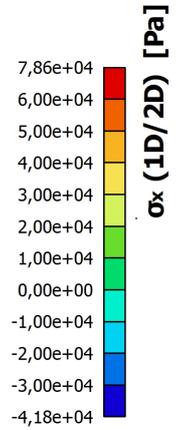
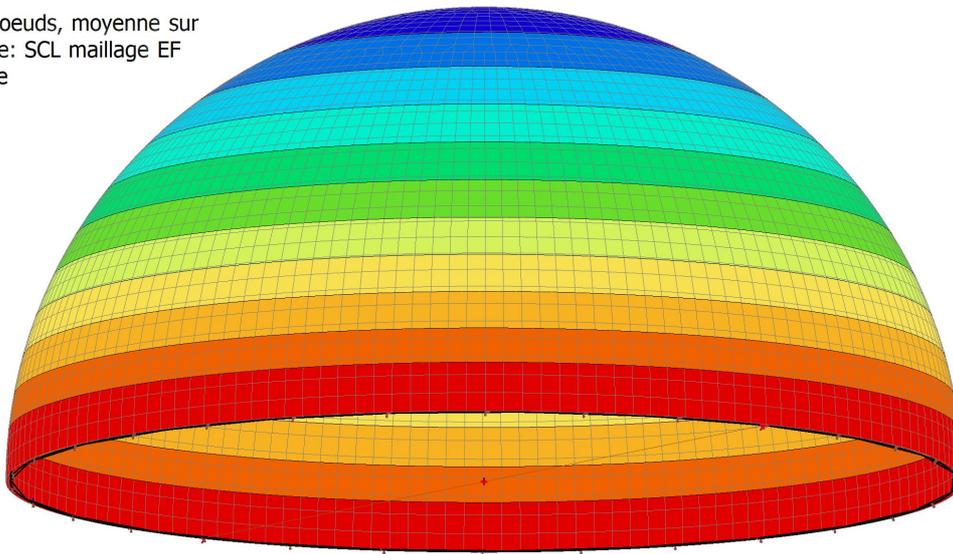
| Name | Description Spec | Action type Load type | Load group | Direction |
|------|---------------------|--------------------------|------------|-----------|
| LC1 | Poids propre | Permanent Self weight | LG1 | -Z |

Shell is subjected to its self-weight

4. RESULTS

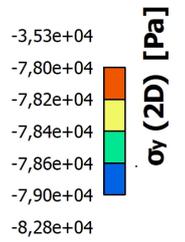
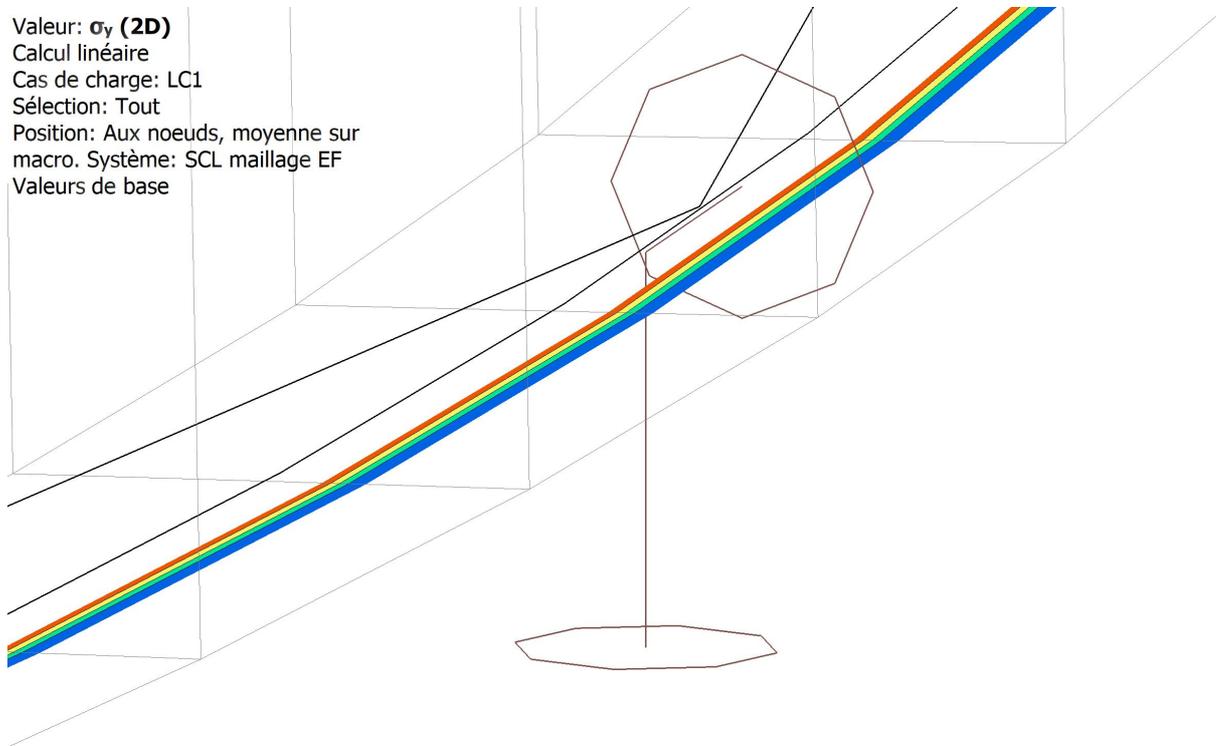
4.1. Horizontal stress

Valeur: σ_x (1D/2D)
 Calcul linéaire
 Cas de charge: LC1
 Sélection: Tout
 Position: Aux noeuds, moyenne sur macro. Système: SCL maillage EF
 Valeurs de base



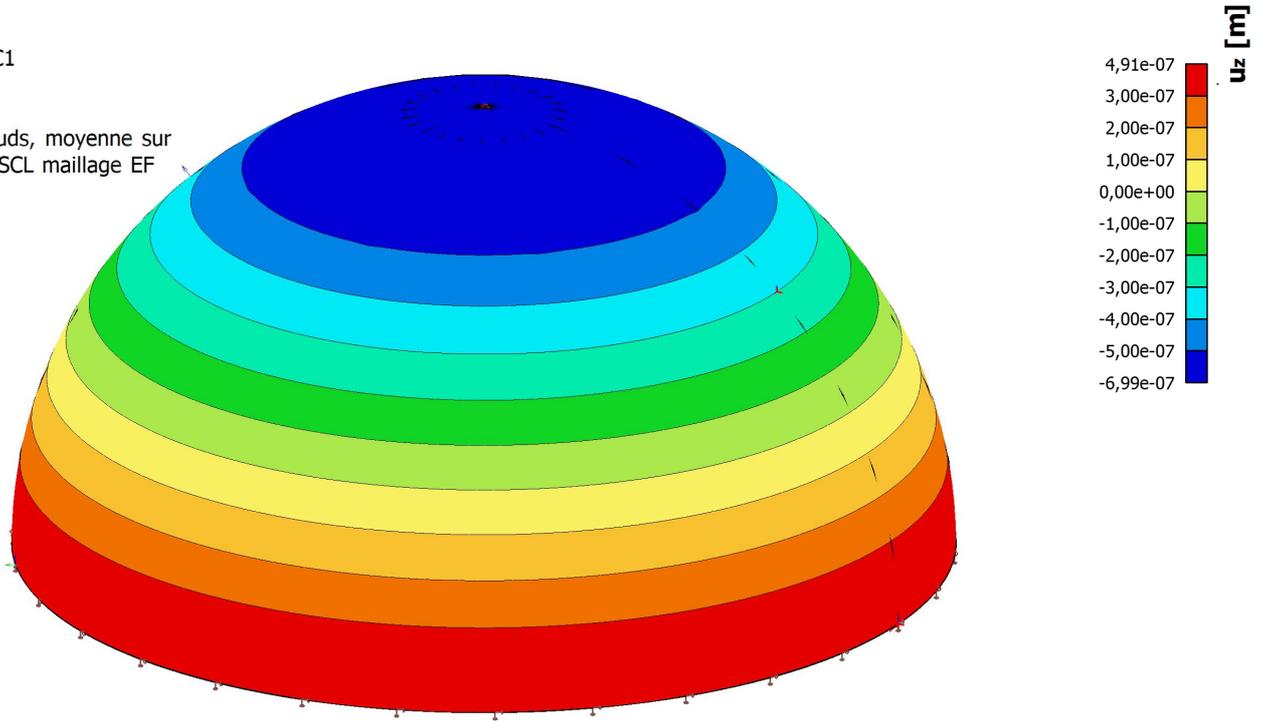
4.2. Vertical stress on edge

Valeur: σ_y (2D)
 Calcul linéaire
 Cas de charge: LC1
 Sélection: Tout
 Position: Aux noeuds, moyenne sur macro. Système: SCL maillage EF
 Valeurs de base



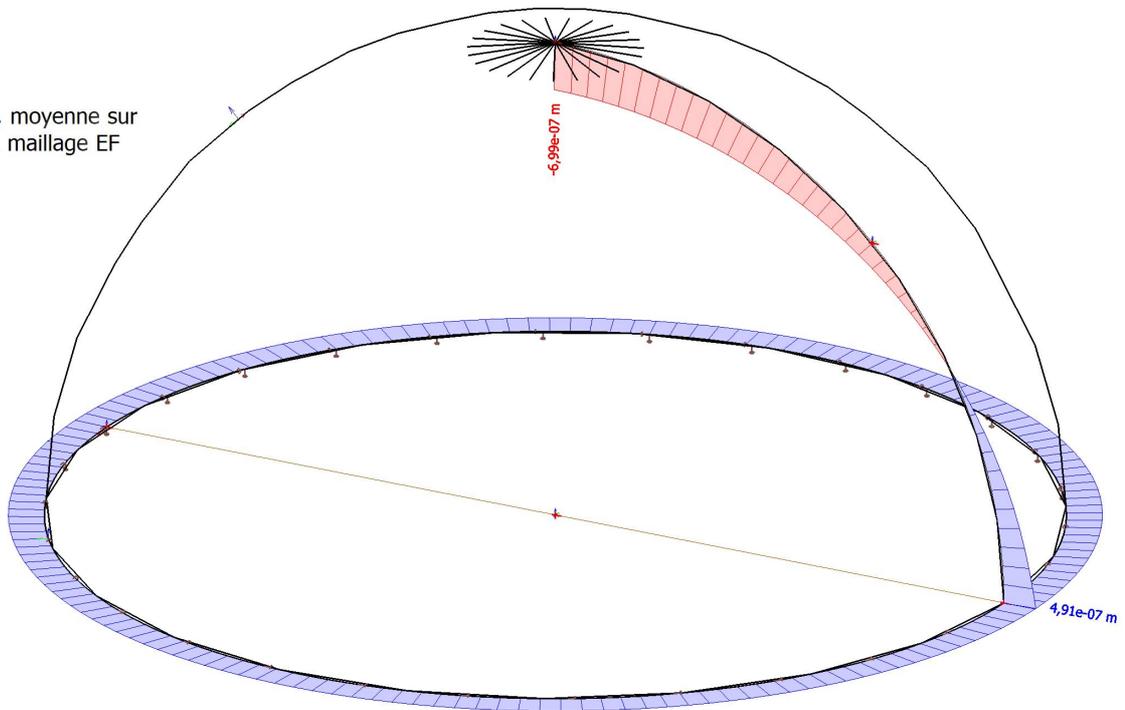
4.3. Displacement δR (m)

Valeur: u_z
Calcul linéaire
Cas de charge: LC1
Extrême: Global
Sélection: Tout
Position: Aux noeuds, moyenne sur macro. Système: SCL maillage EF



4.4. Displacement δR (m) on edge

Valeur: u_z
Calcul linéaire
Cas de charge: LC1
Extrême: Global
Sélection: Tout
Position: Aux noeuds, moyenne sur macro. Système: SCL maillage EF



4.5. 2D displacement

Linear calculation

Load case: LC1

Extreme: Global

Selection: All

Location: In nodes avg. on macro. System: LCS mesh element

Results on sections:

| Name | Mesh | Position [m] | Case | u_x [m] | u_y [m] | u_z [m] | ϕ_x [mrad] | ϕ_y [mrad] | ϕ_z [mrad] | U_{total} [m] |
|------|------------------|-------------------------|------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|
| SE1 | Element: 4780 | 1,048 0,000 0,000 | LC1 | 0,00e+00 | 1,00e-09 | 4,91e-07 | 0,0 | 0,0 | 0,0 | 4,91e-07 |

5. EXPECTED AFNOR RESULTS

At the extremity :

Horizontal stress : 7.85 e4 Pa

Vertical stress: -7.85 e4 Pa

Radial displacement: 4.86 e-7 m

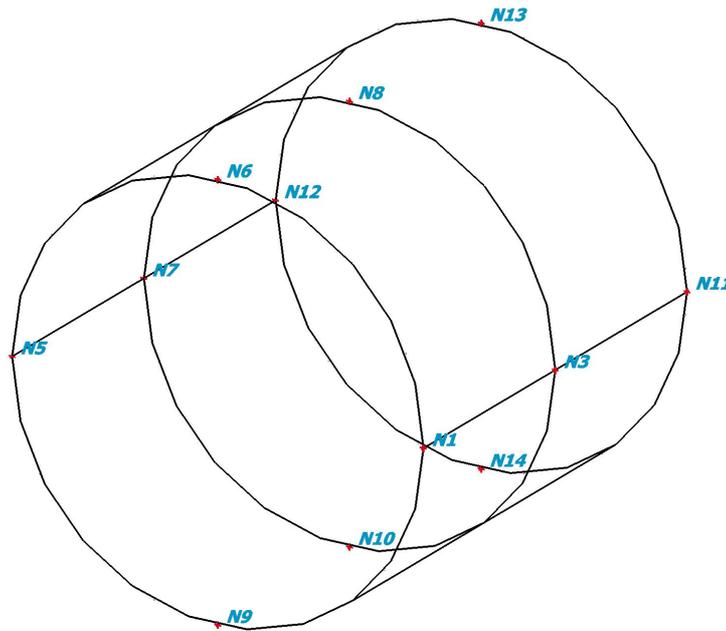
REFERENCE : "Guide de validation des progiciels de calcul de structures" AFNOR, 1990

1. TESTCASE DESCRIPTION

Cylindrical shell subjected to concentrated force -
Codification: Cylindrical shell - Material: elastic - Concentrated forces.

2. MODEL

2.1. Analysis model



2.2. Nodes

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] |
|------|-------------|-------------|-------------|
| N1 | 4,953 | 0,000 | 0,000 |
| N3 | 4,953 | 5,175 | 0,000 |
| N5 | -4,953 | 0,000 | 0,000 |
| N6 | 0,000 | 0,000 | 4,953 |

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] |
|------|-------------|-------------|-------------|
| N7 | -4,953 | 5,175 | 0,000 |
| N8 | 0,000 | 5,175 | 4,953 |
| N9 | 0,000 | 0,000 | -4,953 |
| N10 | 0,000 | 5,175 | -4,953 |

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] |
|------|-------------|-------------|-------------|
| N11 | 4,953 | 10,350 | 0,000 |
| N12 | -4,953 | 10,350 | 0,000 |
| N13 | 0,000 | 10,350 | 4,953 |
| N14 | 0,000 | 10,350 | -4,953 |

2.3. 2D members

| Name | Layer | Type | Element type | Material | Thickness type | Th. [mm] |
|------|---------|------------|--------------|----------|----------------|----------|
| S3 | Calque1 | coque (98) | Standard | Material | constant | 94 |
| S4 | Calque1 | coque (98) | Standard | Material | constant | 94 |
| S5 | Calque1 | coque (98) | Standard | Material | constant | 94 |
| S6 | Calque1 | coque (98) | Standard | Material | constant | 94 |

2.4. Supports on 2D member edge

| Name | 2D member Edge | Orig Coor | Pos x1 Pos x2 | X | Y | Z | Rx | Ry | Rz |
|------|----------------|--------------------|----------------|----------|----------|----------|------|------|------|
| Sle1 | S3 1 | From start Rela | 0.000 1.000 | Flexible | Flexible | Flexible | Free | Free | Free |
| Sle2 | S5 3 | From start Rela | 0.000 1.000 | Flexible | Flexible | Flexible | Free | Free | Free |
| Sle3 | S6 3 | From start Rela | 0.000 1.000 | Flexible | Flexible | Flexible | Free | Free | Free |
| Sle4 | S4 1 | From start Rela | 0.000 1.000 | Flexible | Flexible | Flexible | Free | Free | Free |

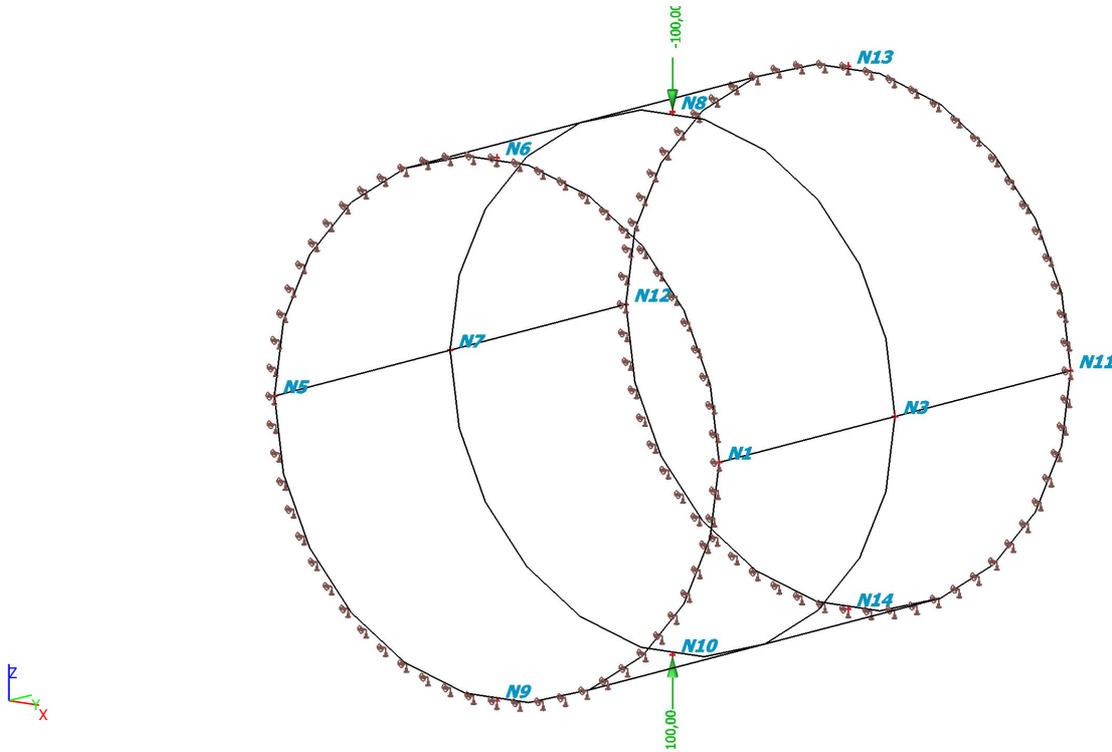
2.5. Materials

Steel EC3

| Name | ρ [kg/m ³] | E_{mod} [MPa] | μ | Limit inférieure [mm] | Limite supérieure [mm] | F_y [MPa] | F_u [MPa] | Colour |
|----------|--------------------------------|--------------------|--------------------|--------------------------|---------------------------|----------------|----------------|--------|
| | | G_{mod} [MPa] | α [m/mK] | | | | | |
| Material | 7850,00 | 1,0500e+01 | 0.3125 | 0 | 40 | 235,0 | 360,0 | ■ |
| | | 4,0000e+00 | 0,01e-003 | 40 | 80 | 215,0 | 360,0 | |

3. LOAD

3.1. LC1 / Tot. value



3.2. Point force in node

| Name | Node | Load case | System | Dir | Type | Value - F [N] |
|------|------|-----------|--------|-----|-------|---------------|
| F1 | N8 | LC1 | GCS | Z | Force | -100,00 |
| F2 | N10 | LC1 | GCS | Z | Force | 100,00 |

4. RESULTS

4.1. Displacement of nodes

Linear calculation

Load case: LC1

Extreme: Global

Selection: N8

| Name | Case | U_z [mm] |
|------|------|-----------------|
| N8 | LC1 | -113,770 |

5. EXPECTED AFNOR RESULTS

Displacement uz in N8 = -113,9 e-3 m

REFERENCE : "Guide de validation des progiciels de calcul de structures" AFNOR, 1990

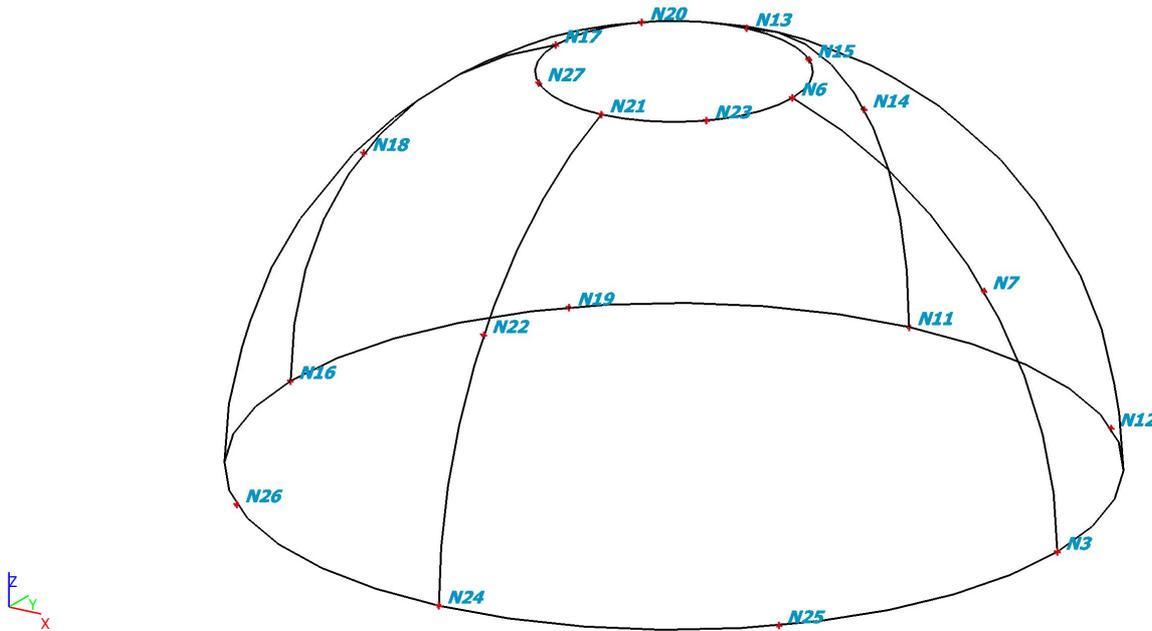
1. TESTCASE DESCRIPTION

Spherical shell with an opening

Codification: Spherical shell - Material: elastic - Concentrated forces

2. MODEL

2.1. Analysis model



2.2. Nodes

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] |
|------|-------------|-------------|-------------|
| N3 | 10,000 | 0,000 | 0,000 |
| N6 | 3,091 | 0,000 | 9,510 |
| N7 | 8,090 | 0,000 | 5,878 |
| N11 | 0,000 | 10,000 | 0,000 |
| N12 | 7,071 | 7,071 | 0,000 |
| N13 | 0,000 | 3,091 | 9,510 |
| N14 | 0,000 | 8,090 | 5,878 |

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] |
|------|-------------|-------------|-------------|
| N15 | 2,186 | 2,186 | 9,510 |
| N16 | -10,000 | 0,000 | 0,000 |
| N17 | -3,091 | 0,000 | 9,510 |
| N18 | -8,090 | 0,000 | 5,878 |
| N19 | -7,071 | 7,071 | 0,000 |
| N20 | -2,186 | 2,186 | 9,510 |
| N21 | 0,000 | -3,091 | 9,510 |

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] |
|------|-------------|-------------|-------------|
| N22 | 0,000 | -8,090 | 5,878 |
| N23 | 2,186 | -2,186 | 9,510 |
| N24 | 0,000 | -10,000 | 0,000 |
| N25 | 7,071 | -7,071 | 0,000 |
| N26 | -7,071 | -7,071 | 0,000 |
| N27 | -2,186 | -2,186 | 9,510 |

2.3. 2D members

| Name | Layer | Type | Element type | Material | Thickness type | Th. [mm] |
|------|---------|------------|--------------|----------|----------------|----------|
| S3 | Calque1 | coque (98) | Standard | Material | constant | 40 |
| S4 | Calque1 | coque (98) | Standard | Material | constant | 40 |
| S5 | Calque1 | coque (98) | Standard | Material | constant | 40 |
| S6 | Calque1 | coque (98) | Standard | Material | constant | 40 |

2.4. Supports on 2D member edge

| Name | 2D member Edge | Orig Coor | Pos x ₁ Pos x ₂ | X | Y | Z | Rx | Ry | Rz |
|------|----------------|--------------------|---------------------------------------|----------|----------|----------|------|------|------|
| Sle5 | S4 3 | From start Rela | 0.000 1.000 | Flexible | Flexible | Flexible | Free | Free | Free |
| Sle6 | S6 3 | From start Rela | 0.000 1.000 | Flexible | Flexible | Flexible | Free | Free | Free |
| Sle7 | S3 3 | From start Rela | 0.000 1.000 | Flexible | Flexible | Flexible | Free | Free | Free |

| Name | 2D member | Orig | Pos x ₁ | X | Y | Z | Rx | Ry | Rz |
|------|-----------|------------|--------------------|----------|----------|----------|------|------|------|
| | Edge | Coor | Pos x ₂ | | | | | | |
| Sle8 | S5 | From start | 0.000 | Flexible | Flexible | Flexible | Free | Free | Free |
| | 3 | Rela | 1.000 | | | | | | |

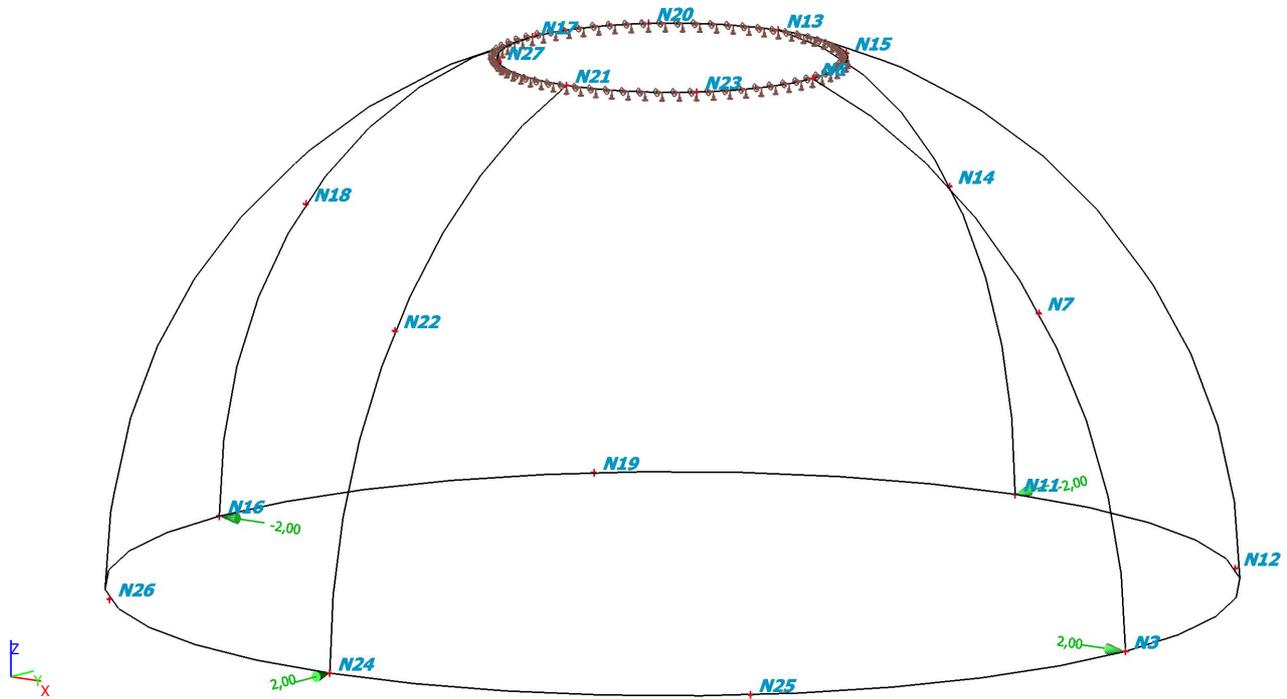
2.5. Materials

Steel EC3

| Name | ρ [kg/m ³] | E_{mod} [MPa] | μ | Limit inférieure [mm] | Limite supérieure [mm] | F_y [Pa] | F_u [Pa] | Colour |
|----------|--------------------------------|--------------------|--------------------|--------------------------|---------------------------|---------------|---------------|--------|
| | | G_{mod} [MPa] | α [m/mK] | | | | | |
| Material | 7850,00 | 6,2850e+01 | 0.3 | 0 | 40 | 235000000,0 | 360000000,0 | ■ |
| | | 2,4173e+01 | 0,01e-003 | 40 | 80 | 215000000,0 | 360000000,0 | |

3. LOAD

3.1. LC1 / Tot. value



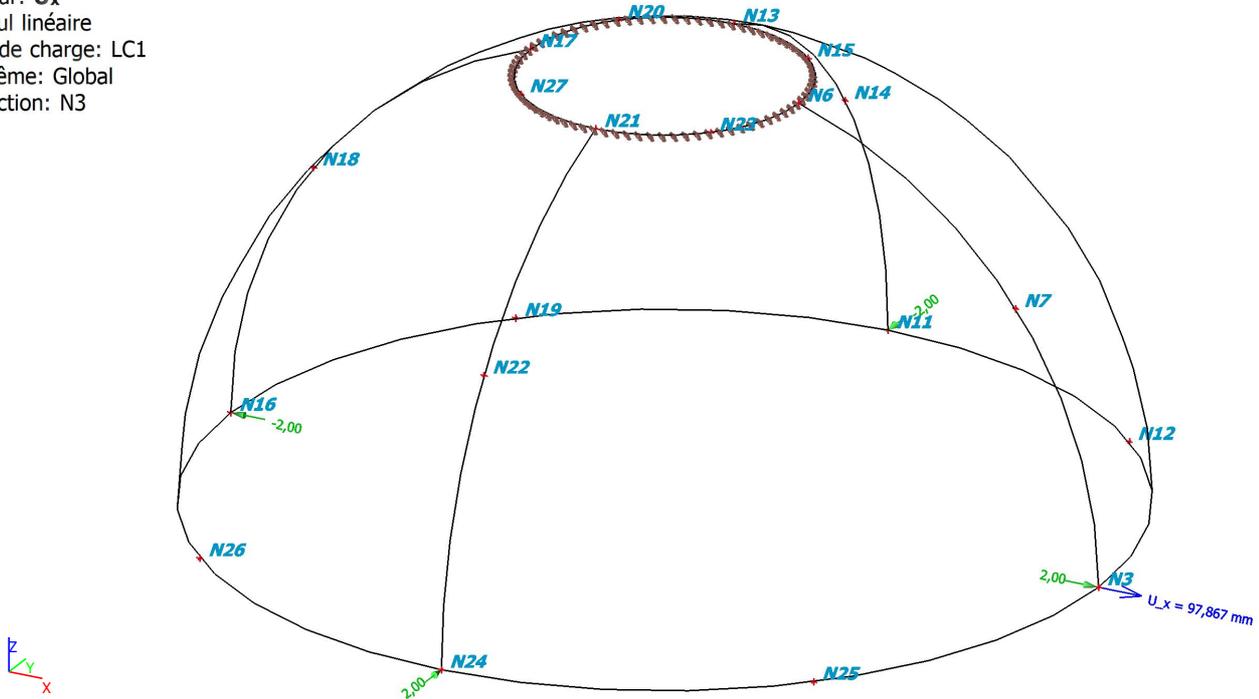
3.2. Point force in node

| Name | Node | Load case | System | Dir | Type | Value - F [N] |
|------|------|-----------|--------|-----|-------|---------------|
| F3 | N11 | LC1 | GCS | Y | Force | -2,00 |
| F4 | N3 | LC1 | GCS | X | Force | 2,00 |
| F5 | N16 | LC1 | GCS | X | Force | -2,00 |
| F6 | N24 | LC1 | GCS | Y | Force | 2,00 |

4. RESULTS

4.1. Displacement of nodes; U_x

Valeur: U_x
 Calcul linéaire
 Cas de charge: LC1
 Extrême: Global
 Sélection: N3



4.2. Displacement of nodes

Linear calculation
 Load case: LC1
 Extreme: Global
 Selection: N3

| Name | Case | U _x [mm] |
|------|------|------------------------|
| N3 | LC1 | 97,867 |

5. EXPECTED AFNOR RESULTS

Displacement u_x in N3 = 94 e-3 m

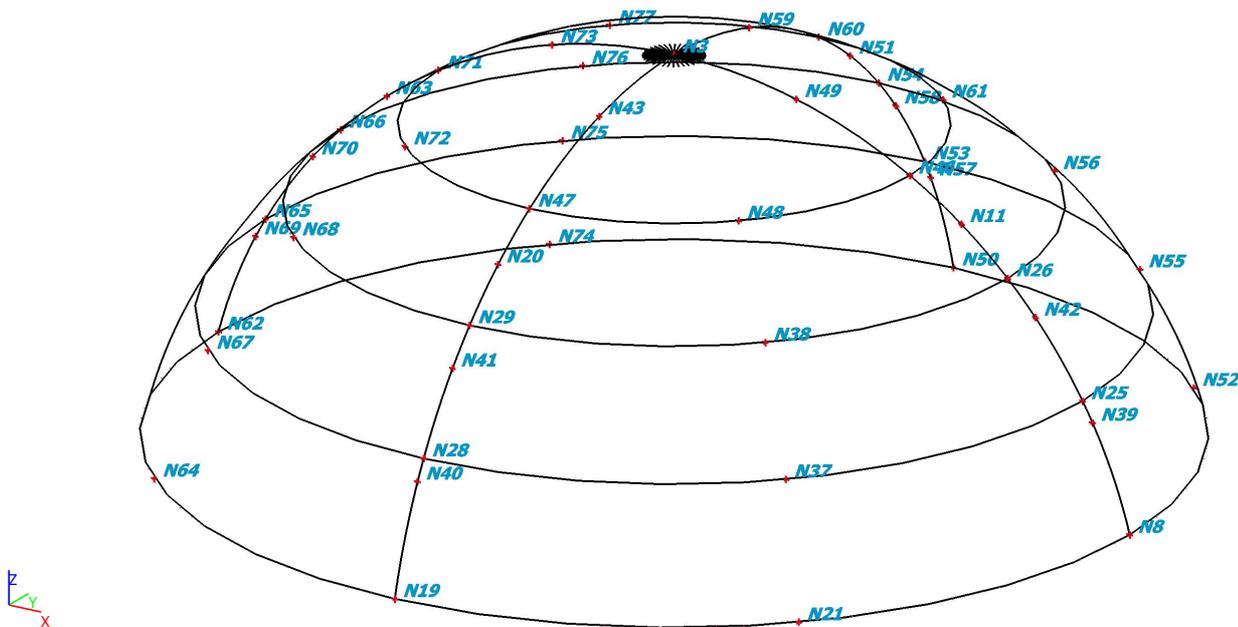
REFERENCE : "Guide de validation des progiciels de calcul de structures" AFNOR, 1990

1. TESTCASE DESCRIPTION

Spherical dome subjected to uniform external pressure
Specification: Spherical shell - Material: elastic - pressure

2. MODEL

2.1. Analysis model



2.2. Nodes

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] |
|------|-------------|-------------|-------------|
| N3 | 0,000 | 0,000 | 2,540 |
| N8 | 2,453 | 0,000 | 0,657 |
| N11 | 1,546 | 0,000 | 2,015 |
| N19 | 0,000 | -2,453 | 0,657 |
| N20 | 0,000 | -1,546 | 2,015 |
| N21 | 1,735 | -1,735 | 0,657 |
| N25 | 2,200 | 0,000 | 1,270 |
| N26 | 1,796 | 0,000 | 1,796 |
| N28 | 0,000 | -2,200 | 1,270 |
| N29 | 0,000 | -1,796 | 1,796 |
| N37 | 1,555 | -1,555 | 1,270 |
| N38 | 1,270 | -1,270 | 1,796 |
| N39 | 2,253 | 0,000 | 1,173 |
| N40 | 0,000 | -2,253 | 1,173 |
| N41 | 0,000 | -1,946 | 1,633 |
| N42 | 1,946 | 0,000 | 1,633 |
| N43 | 0,000 | -0,657 | 2,453 |

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] |
|------|-------------|-------------|-------------|
| N46 | 1,270 | 0,000 | 2,200 |
| N47 | 0,000 | -1,270 | 2,200 |
| N48 | 0,898 | -0,898 | 2,200 |
| N49 | 0,657 | 0,000 | 2,453 |
| N50 | 0,000 | 2,453 | 0,657 |
| N51 | 0,000 | 1,546 | 2,015 |
| N52 | 1,735 | 1,735 | 0,657 |
| N53 | 0,000 | 2,200 | 1,270 |
| N54 | 0,000 | 1,796 | 1,796 |
| N55 | 1,555 | 1,555 | 1,270 |
| N56 | 1,270 | 1,270 | 1,796 |
| N57 | 0,000 | 2,253 | 1,173 |
| N58 | 0,000 | 1,946 | 1,633 |
| N59 | 0,000 | 0,657 | 2,453 |
| N60 | 0,000 | 1,270 | 2,200 |
| N61 | 0,898 | 0,898 | 2,200 |
| N62 | -2,453 | 0,000 | 0,657 |

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] |
|------|-------------|-------------|-------------|
| N63 | -1,546 | 0,000 | 2,015 |
| N64 | -1,735 | -1,735 | 0,657 |
| N65 | -2,200 | 0,000 | 1,270 |
| N66 | -1,796 | 0,000 | 1,796 |
| N67 | -1,555 | -1,555 | 1,270 |
| N68 | -1,270 | -1,270 | 1,796 |
| N69 | -2,253 | 0,000 | 1,173 |
| N70 | -1,946 | 0,000 | 1,633 |
| N71 | -1,270 | 0,000 | 2,200 |
| N72 | -0,898 | -0,898 | 2,200 |
| N73 | -0,657 | 0,000 | 2,453 |
| N74 | -1,735 | 1,735 | 0,657 |
| N75 | -1,555 | 1,555 | 1,270 |
| N76 | -1,270 | 1,270 | 1,796 |
| N77 | -0,898 | 0,898 | 2,200 |

2.3. 2D members

| Name | Layer | Type | Element type | Material | Thickness type | Th. [mm] |
|------|---------|------------|--------------|----------|----------------|----------|
| S1 | Calque1 | coque (98) | Standard | Material | constant | 13 |
| S3 | Calque1 | coque (98) | Standard | Material | constant | 13 |
| S5 | Calque1 | coque (98) | Standard | Material | constant | 13 |
| S6 | Calque1 | coque (98) | Standard | Material | constant | 13 |
| S7 | Calque1 | coque (98) | Standard | Material | constant | 13 |

| Name | Layer | Type | Element type | Material | Thickness type | Th. [mm] |
|------|---------|------------|--------------|----------|----------------|----------|
| S8 | Calque1 | coque (98) | Standard | Material | constant | 13 |
| S9 | Calque1 | coque (98) | Standard | Material | constant | 13 |
| S10 | Calque1 | coque (98) | Standard | Material | constant | 13 |
| S11 | Calque1 | coque (98) | Standard | Material | constant | 13 |
| S12 | Calque1 | coque (98) | Standard | Material | constant | 13 |
| S13 | Calque1 | coque (98) | Standard | Material | constant | 13 |
| S14 | Calque1 | coque (98) | Standard | Material | constant | 13 |
| S15 | Calque1 | coque (98) | Standard | Material | constant | 13 |
| S16 | Calque1 | coque (98) | Standard | Material | constant | 13 |
| S17 | Calque1 | coque (98) | Standard | Material | constant | 13 |
| S18 | Calque1 | coque (98) | Standard | Material | constant | 13 |

2.4. Supports on 2D member edge

| Name | 2D member Edge | Orig Coor | Pos x ₁ Pos x ₂ | X | Y | Z | Rx | Ry | Rz |
|------|----------------|------------|--|-------|-------|-------|-------|-------|-------|
| Sle1 | S15 | From start | 0.000 | Rigid | Rigid | Rigid | Rigid | Rigid | Rigid |
| | 3 | Rela | 1.000 | | | | | | |
| Sle2 | S11 | From start | 0.000 | Rigid | Rigid | Rigid | Rigid | Rigid | Rigid |
| | 3 | Rela | 1.000 | | | | | | |
| Sle3 | S1 | From start | 0.000 | Rigid | Rigid | Rigid | Rigid | Rigid | Rigid |
| | 3 | Rela | 1.000 | | | | | | |
| Sle4 | S7 | From start | 0.000 | Rigid | Rigid | Rigid | Rigid | Rigid | Rigid |
| | 3 | Rela | 1.000 | | | | | | |

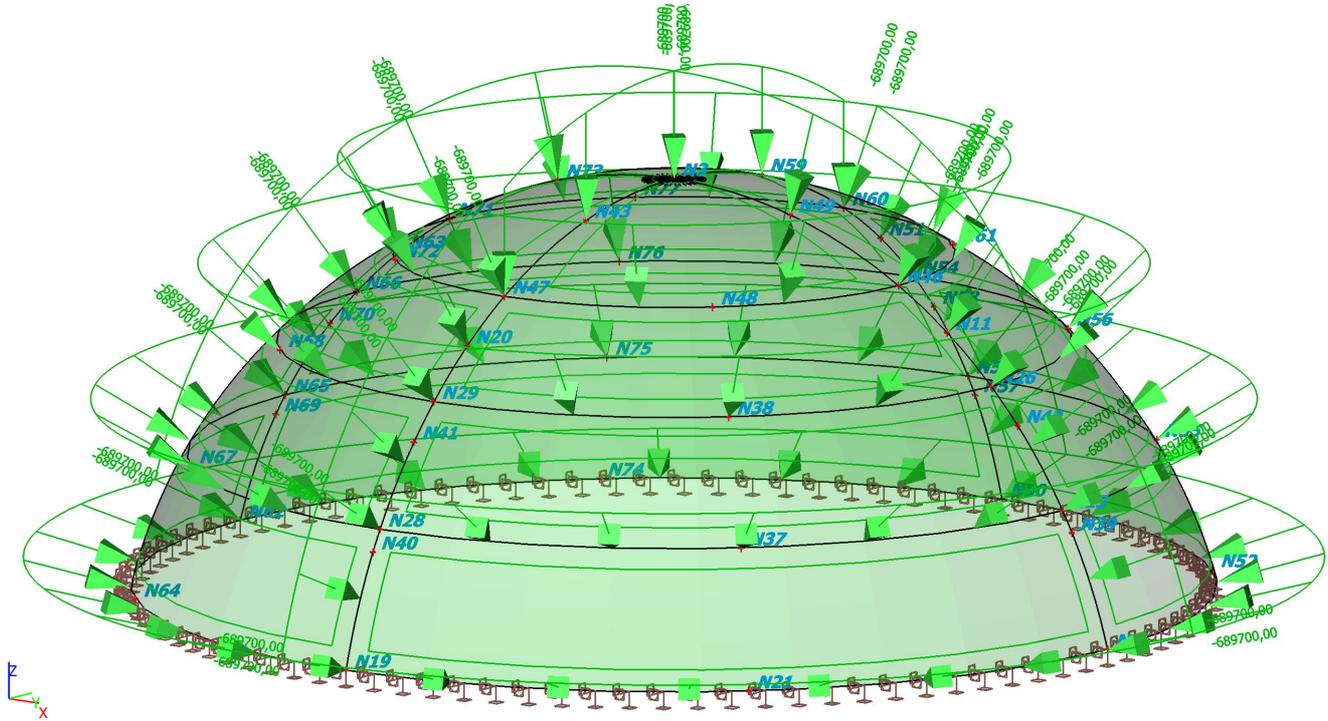
2.5. Materials

Steel EC3

| Name | ρ [kg/m ³] | E_{mod} [MPa] | μ | Limit inférieure [mm] | Limite supérieure [mm] | F_y [MPa] | F_u [MPa] | Colour |
|----------|--------------------------------|--------------------|--------------------|--------------------------|---------------------------|----------------|----------------|---|
| | | G_{mod} [MPa] | α [m/mK] | | | | | |
| Material | 7850,00 | 6,8970e+04 | 0.2 | 0 | 40 | 235,0 | 360,0 |  |
| | | 2,8738e+04 | 0,01e-003 | 40 | 80 | 215,0 | 360,0 | |

3. LOAD

3.1. LC1 / Tot. value



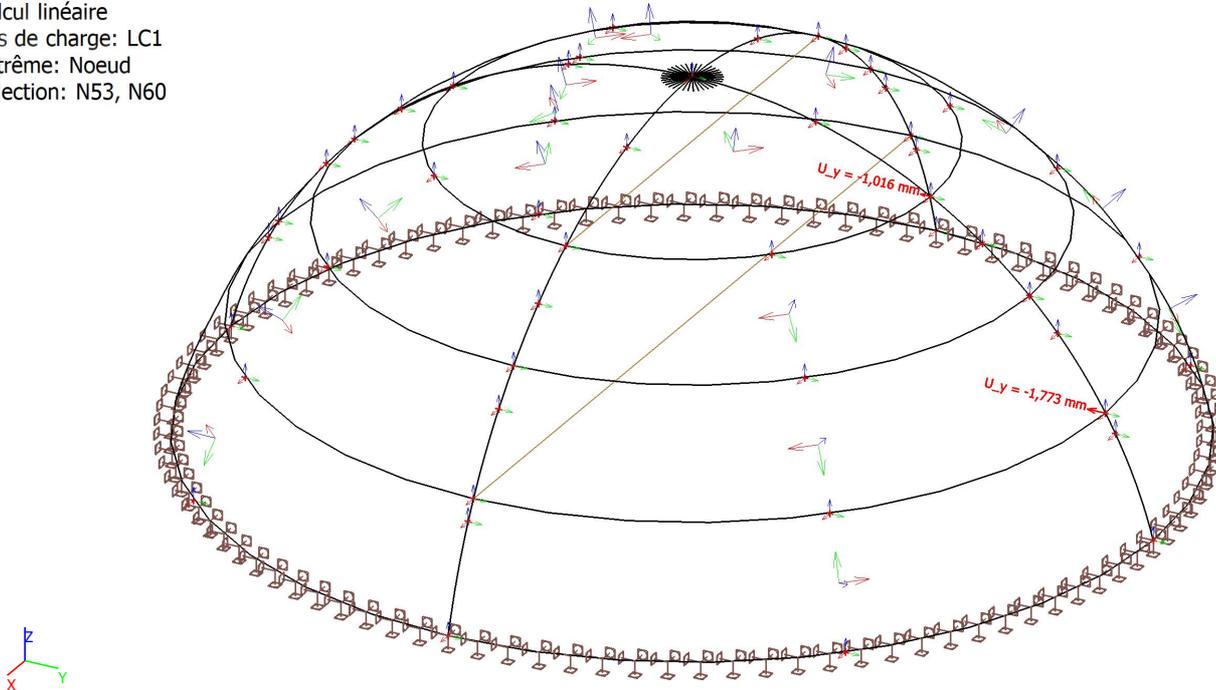
3.2. Surface load

| Name | Dir | Type | Value [N/m ²] | 2D member | Load case | System | Loc |
|------|-----|-------|---------------------------|-----------|-----------|--------|--------|
| SF1 | Z | Force | -689700,00 | S1 | LC1 | LCS | Length |
| SF2 | Z | Force | -689700,00 | S3 | LC1 | LCS | Length |
| SF3 | Z | Force | -689700,00 | S5 | LC1 | LCS | Length |
| SF4 | Z | Force | -689700,00 | S6 | LC1 | LCS | Length |
| SF5 | Z | Force | -689700,00 | S7 | LC1 | LCS | Length |
| SF6 | Z | Force | -689700,00 | S8 | LC1 | LCS | Length |
| SF7 | Z | Force | -689700,00 | S9 | LC1 | LCS | Length |
| SF8 | Z | Force | -689700,00 | S10 | LC1 | LCS | Length |
| SF9 | Z | Force | -689700,00 | S11 | LC1 | LCS | Length |
| SF10 | Z | Force | -689700,00 | S12 | LC1 | LCS | Length |
| SF11 | Z | Force | -689700,00 | S13 | LC1 | LCS | Length |
| SF12 | Z | Force | -689700,00 | S14 | LC1 | LCS | Length |
| SF13 | Z | Force | -689700,00 | S15 | LC1 | LCS | Length |
| SF14 | Z | Force | -689700,00 | S16 | LC1 | LCS | Length |
| SF15 | Z | Force | -689700,00 | S17 | LC1 | LCS | Length |
| SF16 | Z | Force | -689700,00 | S18 | LC1 | LCS | Length |

4. RESULTS

4.1. Déplacement des noeuds; U_y

Valeur: U_y
 Calcul linéaire
 Cas de charge: LC1
 Extrême: Noeud
 Sélection: N53, N60



4.2. Displacement of nodes

Linear calculation
 Load case: LC1
 Extreme: Global
 Selection: N53, N60

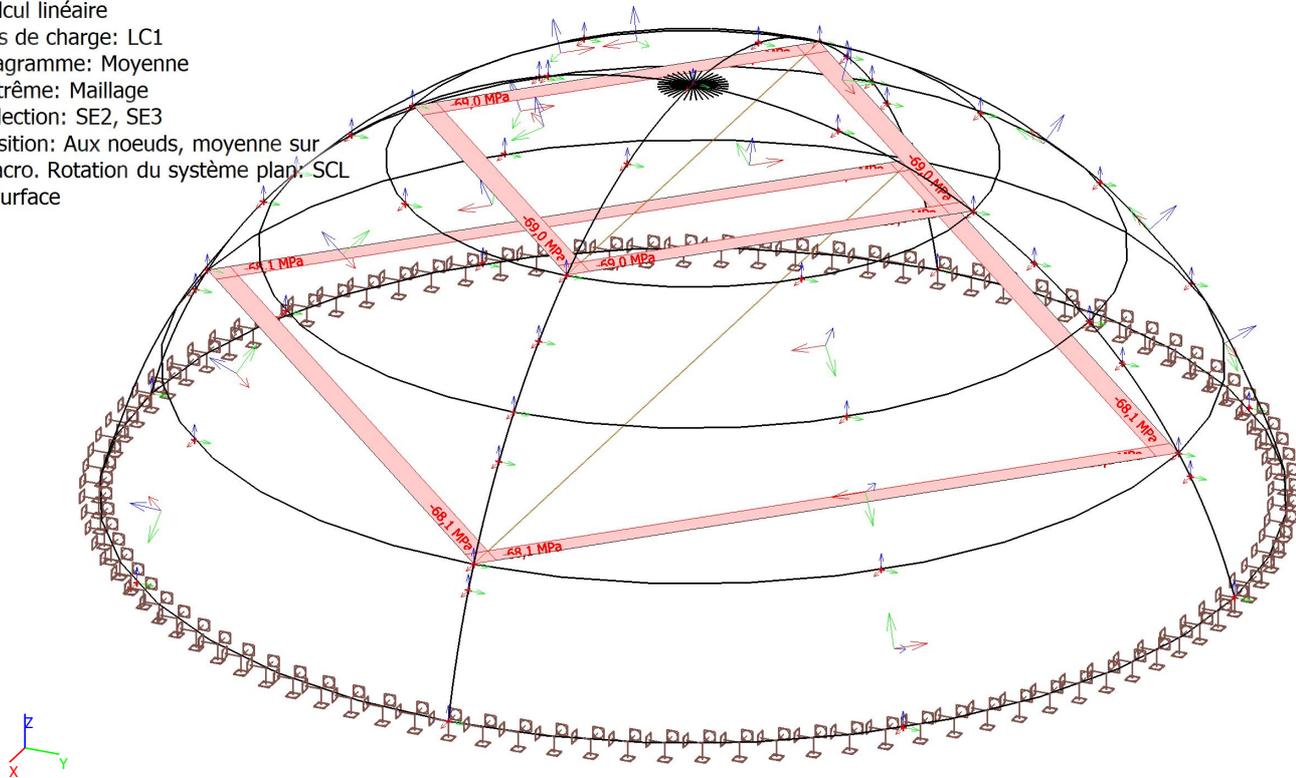
| Name | Case | U _y [mm] |
|------|------|--------------------------|
| N53 | LC1 | -1,773 |
| N60 | LC1 | -1,016 |

For $\Psi = 15^\circ$; $u = -1,776 \text{ mm}$

For $\Psi = 45^\circ$; $u = -1,017 \text{ mm}$

4.3. Contraintes/déformations 2D; σ_{1+}

Valeur: σ_{1+}
 Calcul linéaire
 Cas de charge: LC1
 Diagramme: Moyenne
 Extrême: Maillage
 Sélection: SE2, SE3
 Position: Aux noeuds, moyenne sur macro. Rotation du système plan: SCL
 - Surface



For $\Psi = 15^\circ$; $\sigma = -68,1$ MPa

For $\Psi = 45^\circ$; $u = -69,0$ MPa

5. EXPECTED AFNOR RESULTS

For $\Psi = 15^\circ$; $\sigma = -74$ MPa ; $u = -1,73 \text{ e-}3$ m

For $\Psi = 45^\circ$; $\sigma = -68$ MPa ; $u = -1,02 \text{ e-}3$ m

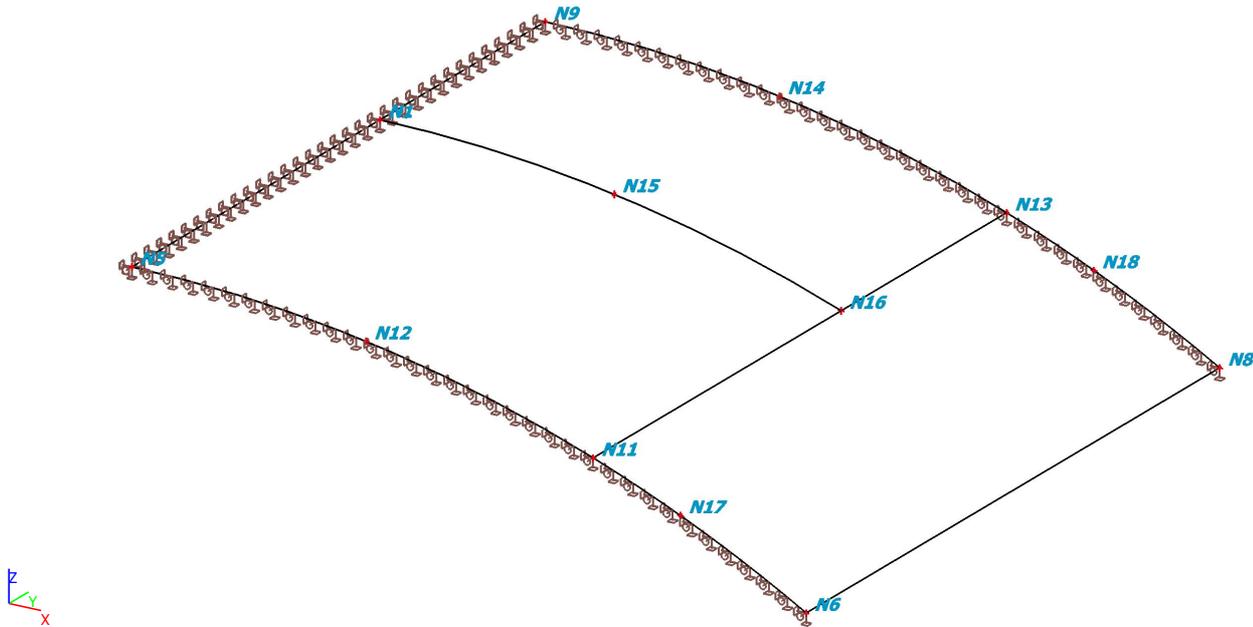
REFERENCE : "Guide de validation des progiciels de calcul de structures" AFNOR, 1990

1. TESTCASE DESCRIPTION

Cylindrical membrane in bending and membrane behavior.

2. MODEL

2.1. Analysis model



2.2. Nodes

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] |
|------|-------------|-------------|-------------|
| N5 | 0,000 | 0,000 | 1,000 |
| N6 | 0,500 | 0,000 | 0,866 |
| N8 | 0,500 | 0,500 | 0,866 |
| N9 | 0,000 | 0,500 | 1,000 |
| N11 | 0,342 | 0,000 | 0,940 |

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] |
|------|-------------|-------------|-------------|
| N12 | 0,174 | 0,000 | 0,985 |
| N13 | 0,342 | 0,500 | 0,940 |
| N14 | 0,174 | 0,500 | 0,985 |
| N1 | 0,000 | 0,300 | 1,000 |
| N15 | 0,174 | 0,300 | 0,985 |

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] |
|------|-------------|-------------|-------------|
| N16 | 0,342 | 0,300 | 0,940 |
| N17 | 0,407 | 0,000 | 0,914 |
| N18 | 0,407 | 0,500 | 0,914 |

2.3. 2D members

| Name | Layer | Type | Element type | Material | Thickness type | Th. [mm] |
|------|---------|------------|--------------|----------|----------------|----------|
| S5 | Calque1 | coque (98) | Standard | S 275 | constant | 10 |
| S6 | Calque1 | coque (98) | Standard | S 275 | constant | 10 |
| S7 | Calque1 | coque (98) | Standard | S 275 | constant | 10 |

2.4. Supports on 2D member edge

| Name | 2D member Edge | Orig Coor | Pos x ₁ Pos x ₂ | X | Y | Z | Rx | Ry | Rz |
|------|----------------|--------------------|---------------------------------------|-------|-------|-------|-------|-------|-------|
| Sle1 | S5 4 | From start Rela | 0.000 1.000 | Rigid | Rigid | Rigid | Rigid | Rigid | Rigid |
| Sle2 | S6 4 | From start Rela | 0.000 1.000 | Rigid | Rigid | Rigid | Rigid | Rigid | Rigid |
| Sle3 | S5 1 | From start Rela | 0.000 1.000 | Free | Rigid | Free | Rigid | Free | Rigid |
| Sle4 | S7 1 | From start Rela | 0.000 1.000 | Free | Rigid | Free | Rigid | Free | Rigid |
| Sle5 | S6 3 | From start Rela | 0.000 1.000 | Free | Rigid | Free | Rigid | Free | Rigid |

| Name | 2D member | Orig | Pos x ₁ | X | Y | Z | Rx | Ry | Rz |
|------|-----------|------------|--------------------|------|-------|------|-------|------|-------|
| | Edge | Coor | Pos x ₂ | | | | | | |
| Sle6 | S7 | From start | 0.000 | Free | Rigid | Free | Rigid | Free | Rigid |
| | 3 | Rela | 1.000 | | | | | | |

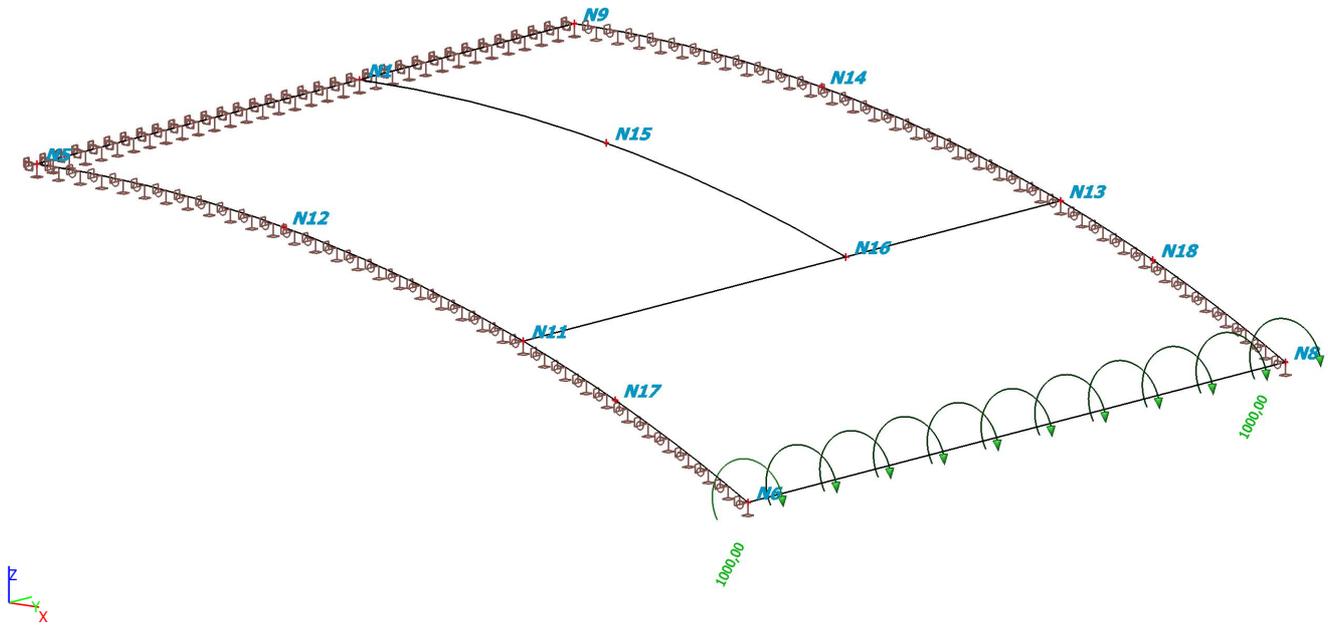
2.5. Materials

Steel EC3

| Name | ρ [kg/m ³] | E_{mod} [MPa] | μ | Limit inférieure [mm] | Limite supérieure [mm] | F_y [MPa] | F_u [MPa] | Colour |
|-------|--------------------------------|--------------------|--------------------|--------------------------|---------------------------|----------------|----------------|--------|
| | | G_{mod} [MPa] | α [m/mK] | | | | | |
| S 275 | 7850,00 | 2,1000e+05 | 0.3 | 0 | 40 | 275,0 | 430,0 | ■ |
| | | 8,0769e+04 | 0,01e-003 | 40 | 80 | 255,0 | 410,0 | |

3. LOAD

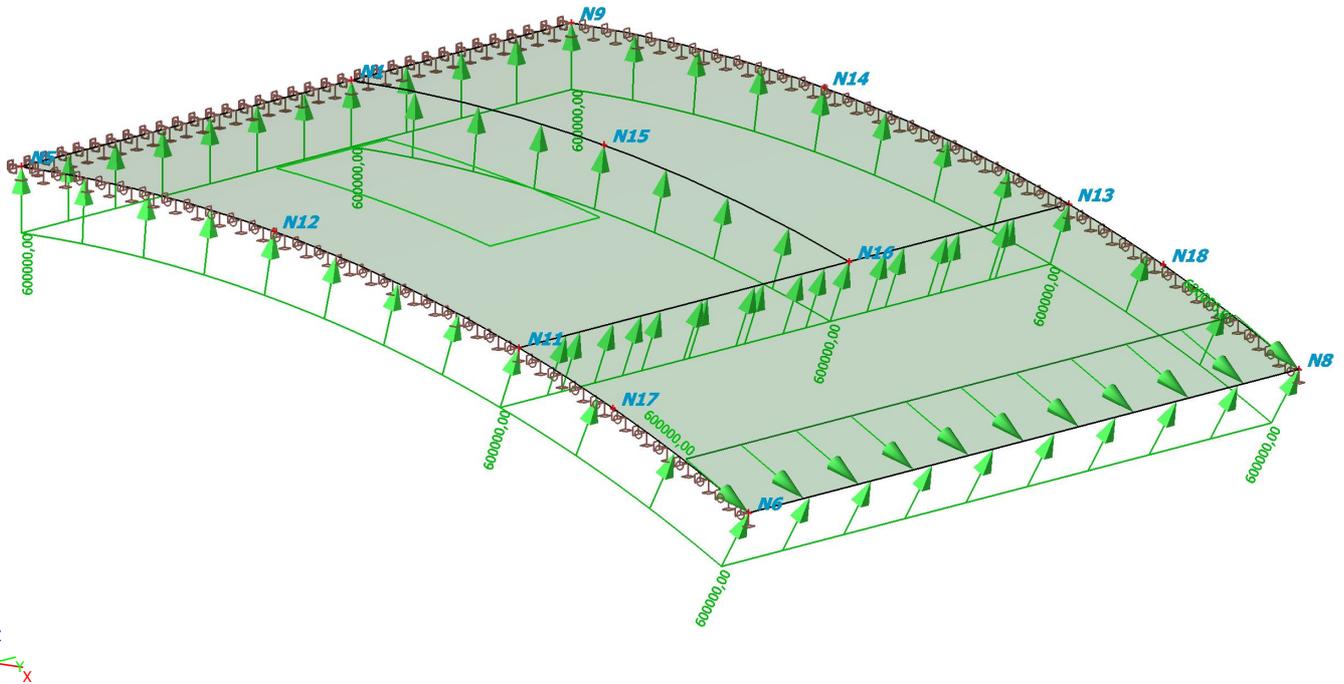
3.1. LC1 - Bending



3.2. Line moment on 2D member edge

| Name | 2D member | Type | Dir | Value - M ₁ [Nm/m] | Pos x ₁ | Loc | Edge |
|------|-----------|--------|--------------|----------------------------------|--------------------|--------|------------|
| | Load case | System | Distribution | Value - M ₂ [Nm/m] | Pos x ₂ | Coor | Orig |
| LMS1 | S7 | Moment | Mx | 1000,00 | 0.000 | Length | 2 |
| | LC1 | LCS | Uniform | | 1.000 | Rela | From start |

3.3. LC1 - Membrane



3.4. Line force on 2D member edge

| Name | 2D member | Type | Dir | Value - P ₁ [N/m] | Pos x ₁ | Loc | Edge |
|------|-----------|--------|--------------|---------------------------------|--------------------|--------|----------|
| | Load case | System | Distribution | Value - P ₂ [N/m] | Pos x ₂ | Coor | Orig |
| LFS3 | S7 | Force | X | 600000,00 | 0.000 | Length | 2 |
| | LC2 | UCS | Uniform | | 1.000 | Rela | From end |

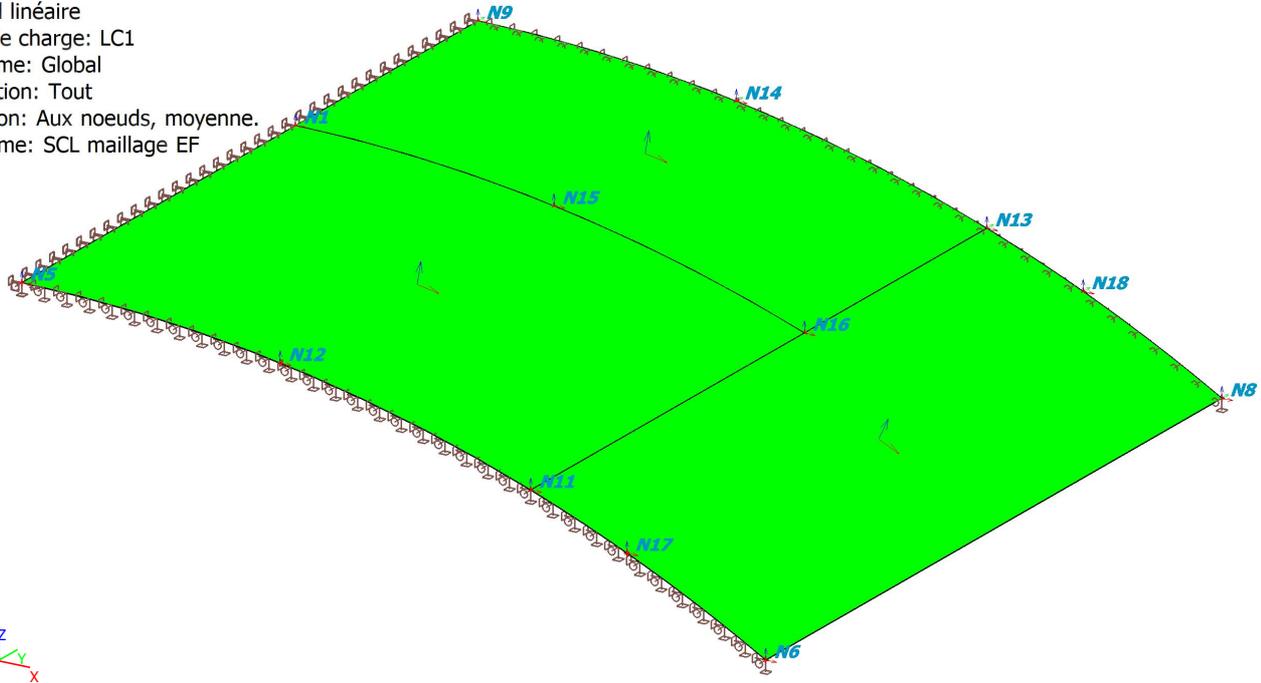
3.5. Surface load

| Name | Dir | Type | Value [N/m ²] | 2D member | Load case | System | Loc |
|------|-----|-------|------------------------------|-----------|-----------|--------|--------|
| SF3 | Z | Force | 600000,00 | S5 | LC2 | LCS | Length |
| SF4 | Z | Force | 600000,00 | S6 | LC2 | LCS | Length |
| SF5 | Z | Force | 600000,00 | S7 | LC2 | LCS | Length |

4. RESULTS

4.1. LC1 - BENDING

Valeur: σ_{x+}
 Calcul linéaire
 Cas de charge: LC1
 Extrême: Global
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: SCL maillage EF



Valeur constante 60,0
 σ_{x+} [MPa]

4.2. 2D stress/strain

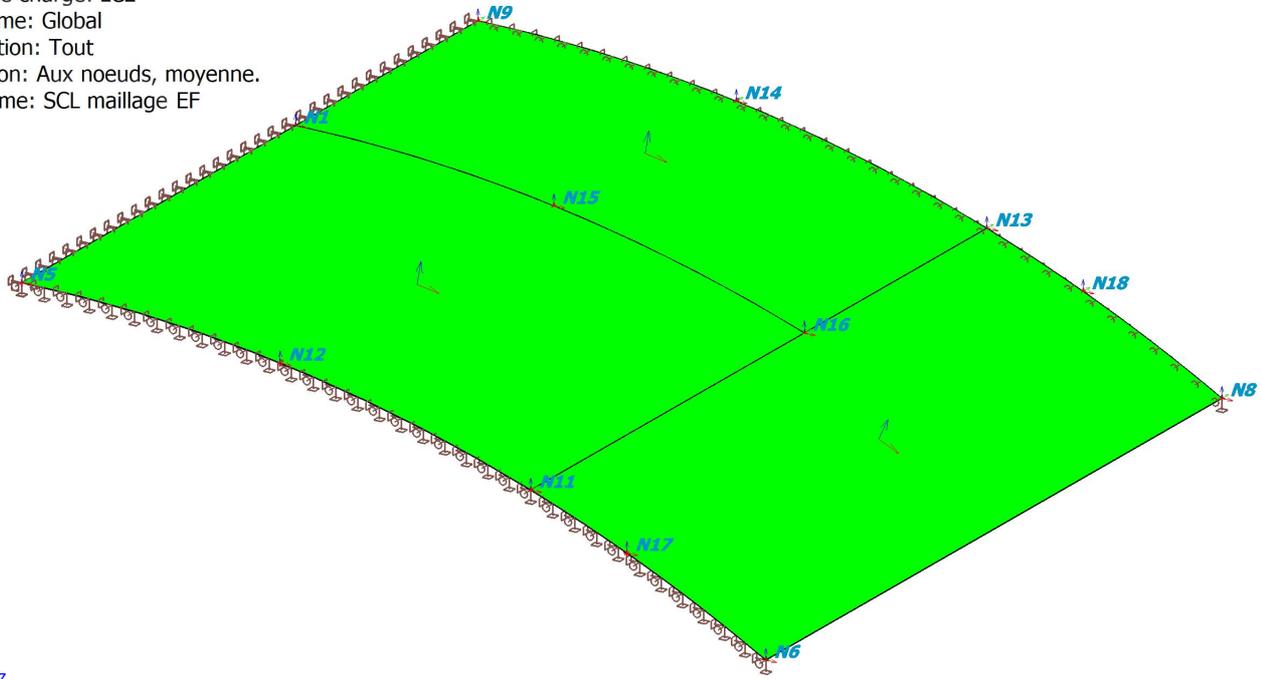
Linear calculation
 Load case: LC1
 Extreme: Global
 Selection: All
 Location: In nodes avg. on macro. System: LCS mesh element

Basic stress

| Name | Mesh | Position [m] | Case | σ_{x+} [MPa] |
|------|------------------------|-------------------------|------|---------------------|
| S5 | Element: 30 Node: 1 | 0,000 0,000 1,000 | LC1 | 60,0 |
| S5 | Element: 1 Node: 6 | 0,000 0,300 1,000 | LC1 | 60,0 |

4.3. LC2 - MEMBRANE

Valeur: σ_{x+}
 Calcul linéaire
 Cas de charge: LC2
 Extrême: Global
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: SCL maillage EF



Valeur constante 60,3
 σ_{x+} [MPa]

4.4. 2D stress/strain

Linear calculation
 Load case: LC2
 Extreme: Global
 Selection: All
 Location: In nodes avg. on macro. System: LCS mesh element

Basic stress

| Name | Mesh | Position [m] | Case | σ_{x+} [MPa] |
|------|---------------------------|-------------------------|------|---------------------|
| S7 | Element: 1818 Node: 11 | 0,500 0,000 0,866 | LC2 | 60,3 |
| S7 | Element: 1801 Node: 3 | 0,342 0,000 0,940 | LC2 | 60,3 |

5. EXPECTED AFNOR RESULTS

LC1 - BENDING

σ_{x+} = 60 MPa

LC2 - MEMBRANE

σ_{x+} = 60 MPa

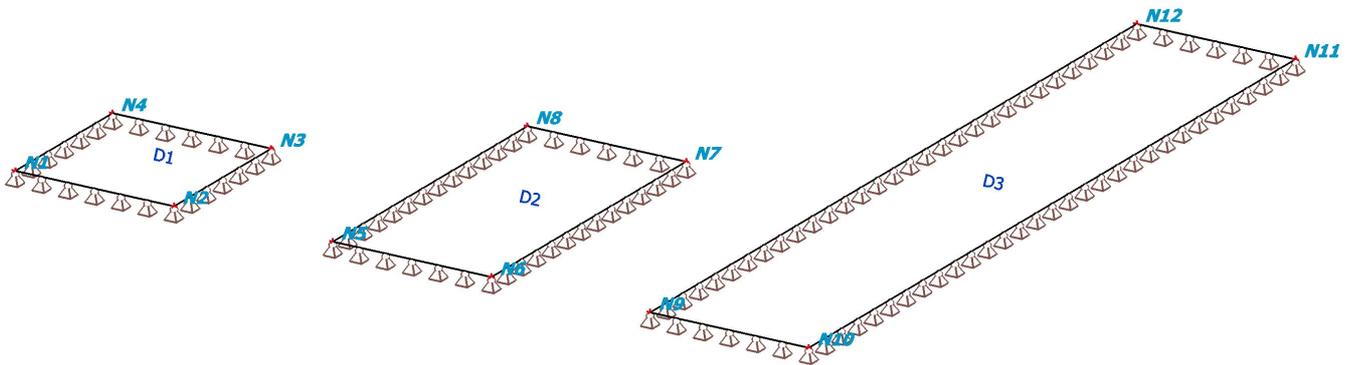
REFERENCE : "Guide de validation des progiciels de calcul de structures" AFNOR, 1990

1. TESTCASE DESCRIPTION

Simply supported rectangular plate with uniform load
Specification: Plate - Pressure - Simple support.

2. MODEL

2.1. Analysis model



2.2. Nodes

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] |
|------|-------------|-------------|-------------|
| N1 | 0,000 | 0,000 | 0,000 |
| N2 | 1,000 | 0,000 | 0,000 |
| N3 | 1,000 | 1,000 | 0,000 |
| N4 | 0,000 | 1,000 | 0,000 |

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] |
|------|-------------|-------------|-------------|
| N5 | 2,000 | 0,000 | 0,000 |
| N6 | 3,000 | 0,000 | 0,000 |
| N7 | 3,000 | 2,000 | 0,000 |
| N8 | 2,000 | 2,000 | 0,000 |

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] |
|------|-------------|-------------|-------------|
| N9 | 4,000 | 0,000 | 0,000 |
| N10 | 5,000 | 0,000 | 0,000 |
| N11 | 5,000 | 5,000 | 0,000 |
| N12 | 4,000 | 5,000 | 0,000 |

2.3. 2D members

| Name | Layer | Type | Element type | Material | Thickness type | Th. [mm] |
|------|---------|------------|--------------|----------|----------------|----------|
| D1 | Calque1 | dalle (90) | Standard | S 235 | constant | 10 |
| D2 | Calque1 | dalle (90) | Standard | S 235 | constant | 10 |
| D3 | Calque1 | dalle (90) | Standard | S 235 | constant | 10 |

2.4. Supports on 2D member edge

| Name | 2D member Edge | Orig Coor | Pos x ₁ Pos x ₂ | X | Y | Z | Rx | Ry | Rz |
|------|----------------|------------|---------------------------------------|-------|-------|-------|------|------|------|
| Sle1 | D1 1 | From start | 0.000 | Rigid | Rigid | Rigid | Free | Free | Free |
| | | Rela | 1.000 | | | | | | |
| Sle2 | D1 2 | From start | 0.000 | Rigid | Rigid | Rigid | Free | Free | Free |
| | | Rela | 1.000 | | | | | | |
| Sle3 | D1 3 | From start | 0.000 | Rigid | Rigid | Rigid | Free | Free | Free |
| | | Rela | 1.000 | | | | | | |
| Sle4 | D1 4 | From start | 0.000 | Rigid | Rigid | Rigid | Free | Free | Free |
| | | Rela | 1.000 | | | | | | |
| Sle5 | D2 1 | From start | 0.000 | Rigid | Rigid | Rigid | Free | Free | Free |
| | | Rela | 1.000 | | | | | | |

| Name | 2D member Edge | Orig Coor | Pos x ₁ Pos x ₂ | X | Y | Z | Rx | Ry | Rz |
|-------|-------------------|--------------|--|-------|-------|-------|------|------|------|
| Sle6 | D2 | From start | 0.000 | Rigid | Rigid | Rigid | Free | Free | Free |
| | 2 | Rela | 1.000 | | | | | | |
| Sle7 | D2 | From start | 0.000 | Rigid | Rigid | Rigid | Free | Free | Free |
| | 3 | Rela | 1.000 | | | | | | |
| Sle8 | D2 | From start | 0.000 | Rigid | Rigid | Rigid | Free | Free | Free |
| | 4 | Rela | 1.000 | | | | | | |
| Sle9 | D3 | From start | 0.000 | Rigid | Rigid | Rigid | Free | Free | Free |
| | 1 | Rela | 1.000 | | | | | | |
| Sle10 | D3 | From start | 0.000 | Rigid | Rigid | Rigid | Free | Free | Free |
| | 2 | Rela | 1.000 | | | | | | |
| Sle11 | D3 | From start | 0.000 | Rigid | Rigid | Rigid | Free | Free | Free |
| | 3 | Rela | 1.000 | | | | | | |
| Sle12 | D3 | From start | 0.000 | Rigid | Rigid | Rigid | Free | Free | Free |
| | 4 | Rela | 1.000 | | | | | | |

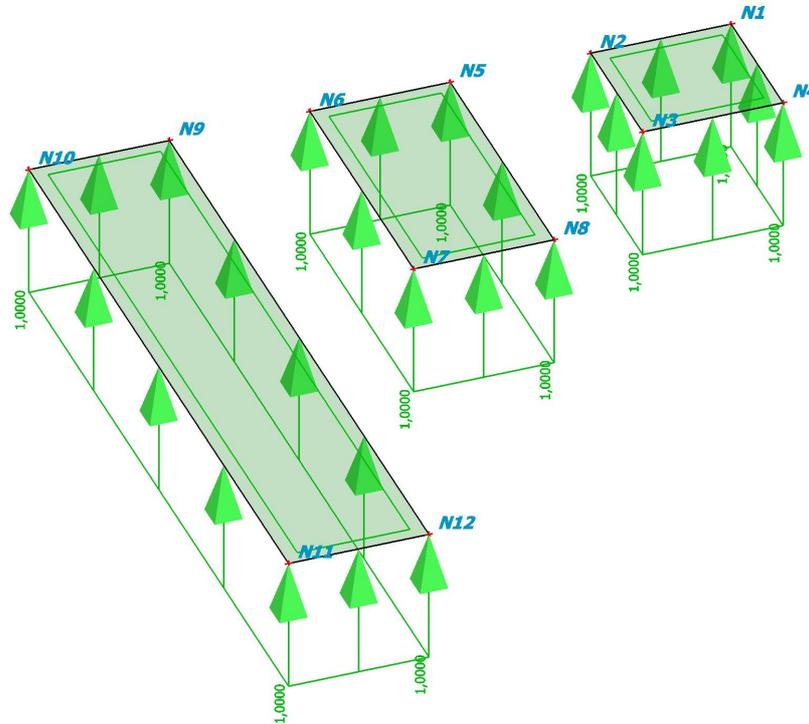
2.5. Materials

Steel EC3

| Name | ρ [kg/m ³] | E_{mod} [MPa] | μ | Limit inférieure [mm] | Limite supérieure [mm] | F_y [MPa] | F_u [MPa] | Colour |
|-------|--------------------------------|--------------------|--------------------|--------------------------|---------------------------|----------------|----------------|--------|
| | | G_{mod} [MPa] | α [m/mK] | | | | | |
| S 235 | 7850,00 | 1,0000e+01 | 0.3 | 0 | 40 | 235,0 | 360,0 | ■ |
| | | 3,8462e+00 | 0,01e-003 | 40 | 80 | 215,0 | 360,0 | |

3. LOAD

3.1. LC1 / Tot. value



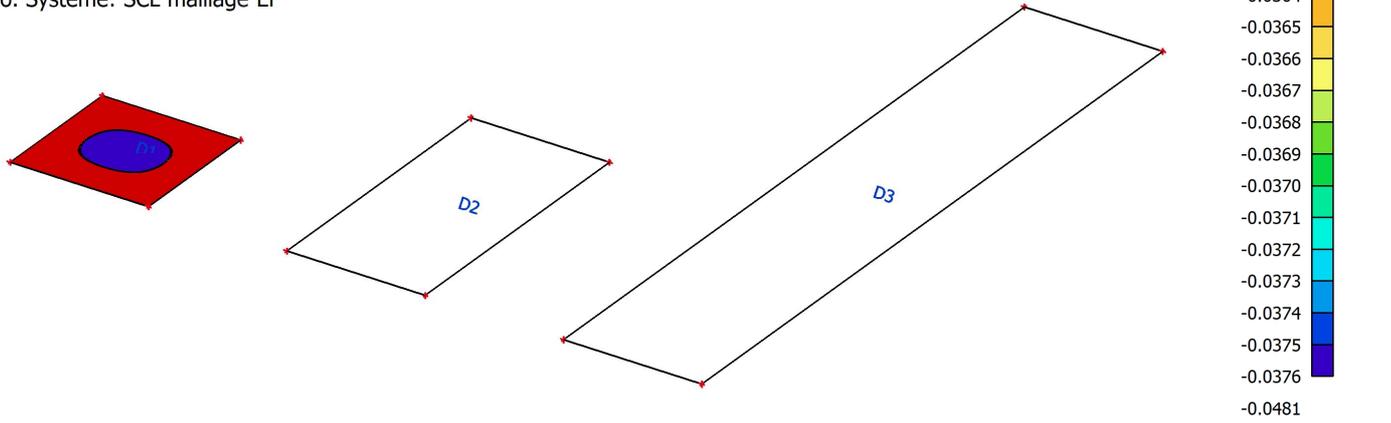
3.2. Surface load

| Name | Dir | Type | Value [N/m ²] | 2D member | Load case | System | Loc |
|------|-----|-------|---------------------------|-----------|-----------|--------|--------|
| SF1 | Z | Force | 1,0000 | D3 | LC2 | GCS | Length |
| SF2 | Z | Force | 1,0000 | D2 | LC2 | GCS | Length |
| SF3 | Z | Force | 1,0000 | D1 | LC2 | GCS | Length |

4. RESULTS

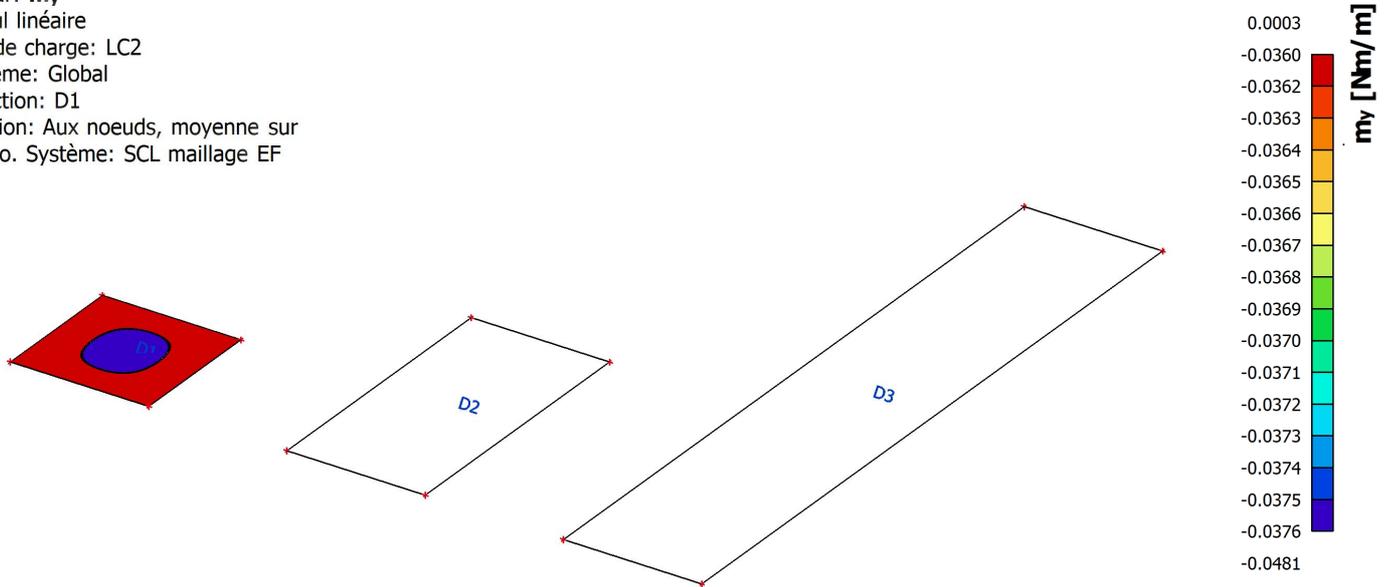
4.1. 2D internal forces; m_x

Valeur: m_x
 Calcul linéaire
 Cas de charge: LC2
 Extrême: Global
 Sélection: D1
 Position: Aux noeuds, moyenne sur macro. Système: SCL maillage EF



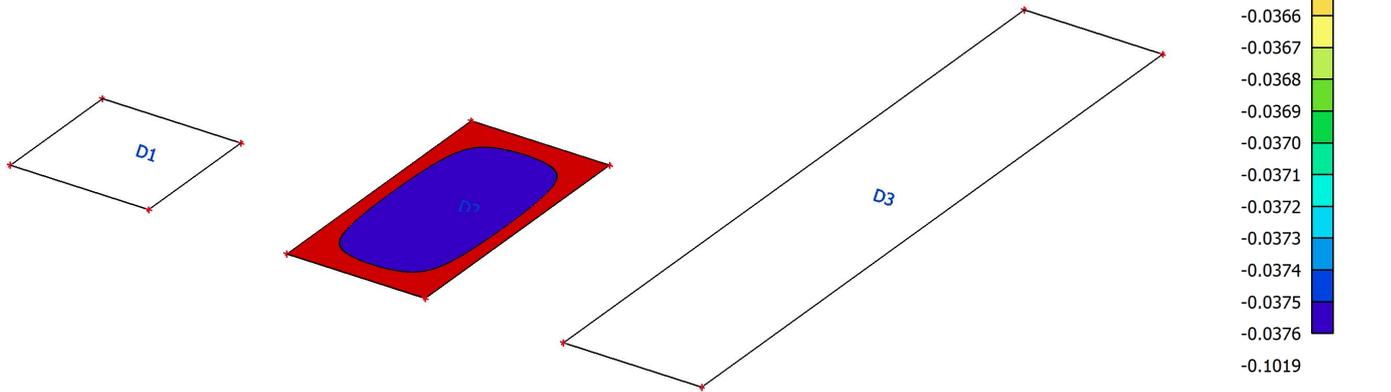
4.2. 2D internal forces; m_y

Valeur: m_y
 Calcul linéaire
 Cas de charge: LC2
 Extrême: Global
 Sélection: D1
 Position: Aux noeuds, moyenne sur macro. Système: SCL maillage EF



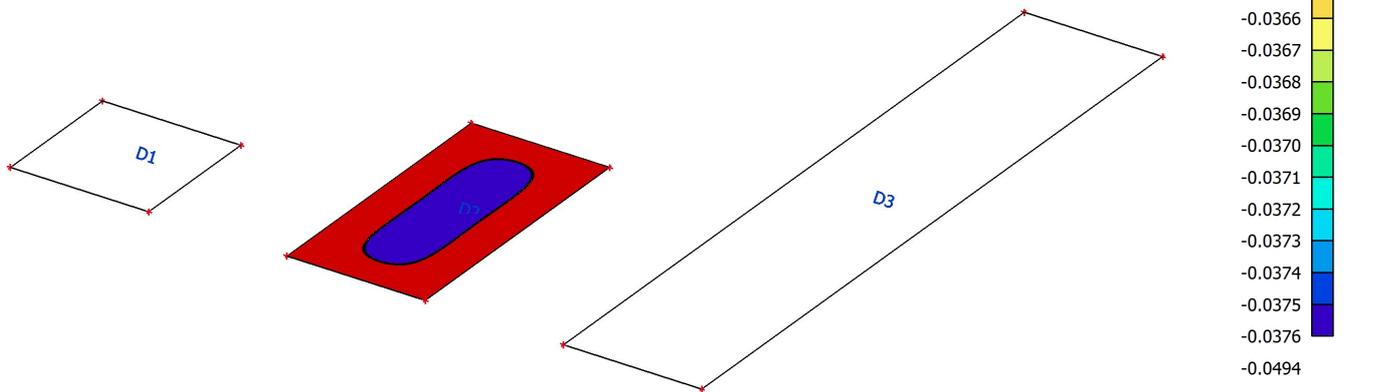
4.3. 2D internal forces; m_x

Valeur: m_x
 Calcul linéaire
 Cas de charge: LC2
 Extrême: Global
 Sélection: D2
 Position: Aux noeuds, moyenne sur macro. Système: SCL maillage EF



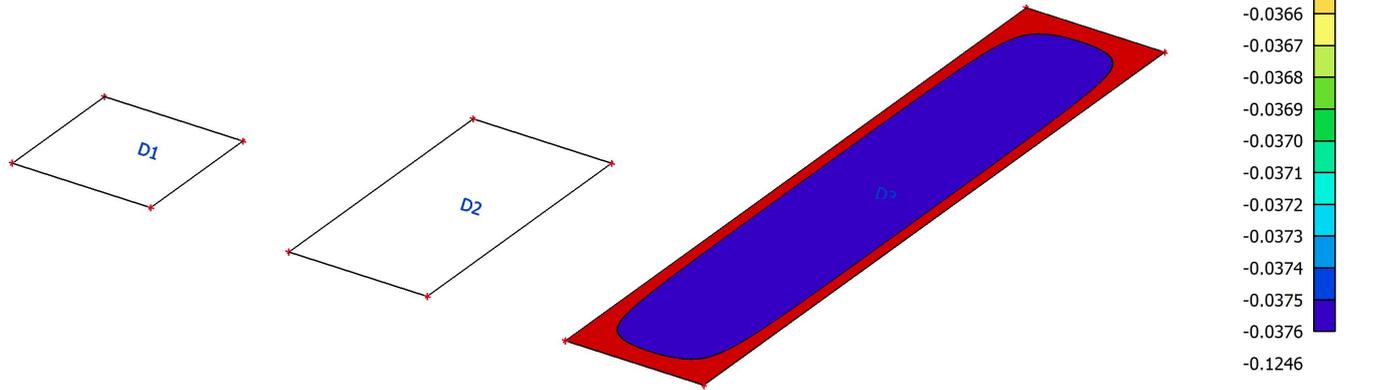
4.4. 2D internal forces; m_y

Valeur: m_y
 Calcul linéaire
 Cas de charge: LC2
 Extrême: Global
 Sélection: D2
 Position: Aux noeuds, moyenne sur macro. Système: SCL maillage EF



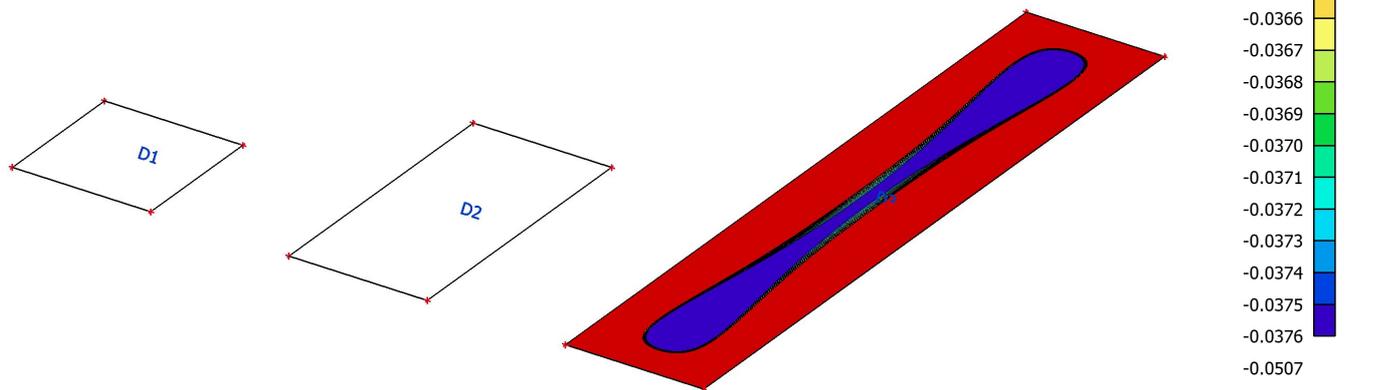
4.5. 2D internal forces; m_x

Valeur: m_x
 Calcul linéaire
 Cas de charge: LC2
 Extrême: Global
 Sélection: D3
 Position: Aux noeuds, moyenne sur macro. Système: SCL maillage EF



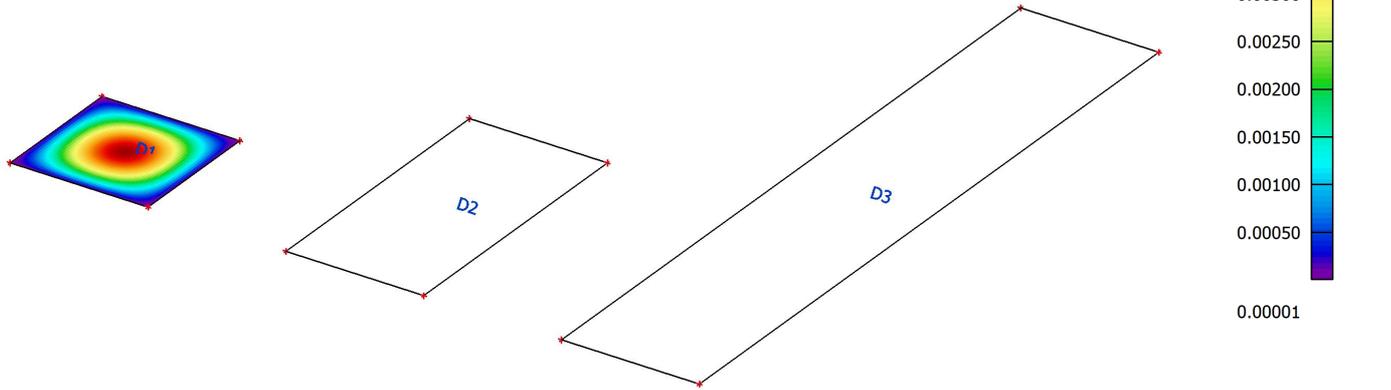
4.6. 2D internal forces; m_y

Valeur: m_y
 Calcul linéaire
 Cas de charge: LC2
 Extrême: Global
 Sélection: D3
 Position: Aux noeuds, moyenne sur macro. Système: SCL maillage EF



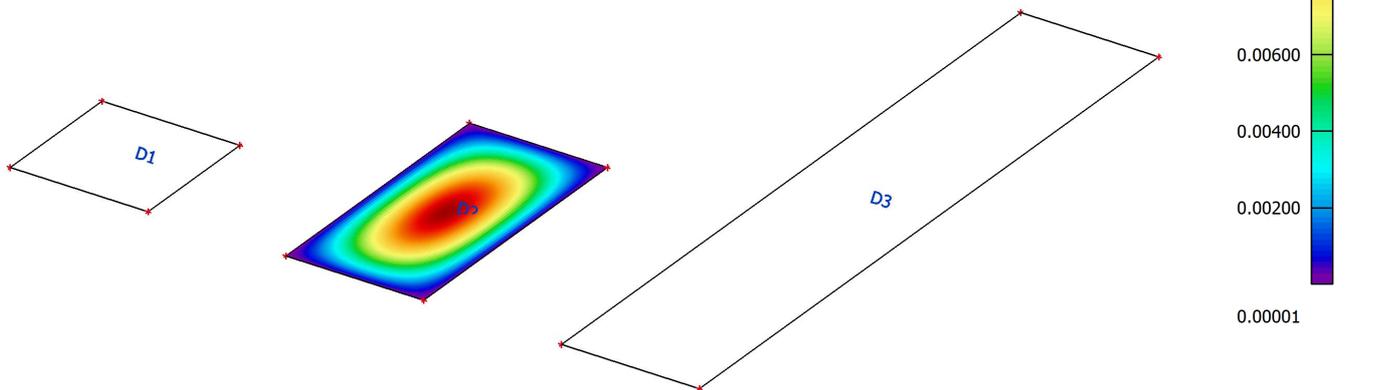
4.7. 2D displacement; u_z

Valeur: u_z
Calcul linéaire
Cas de charge: LC2
Extrême: Elément
Sélection: D1
Position: Aux centres. Système: SCL
maillage EF



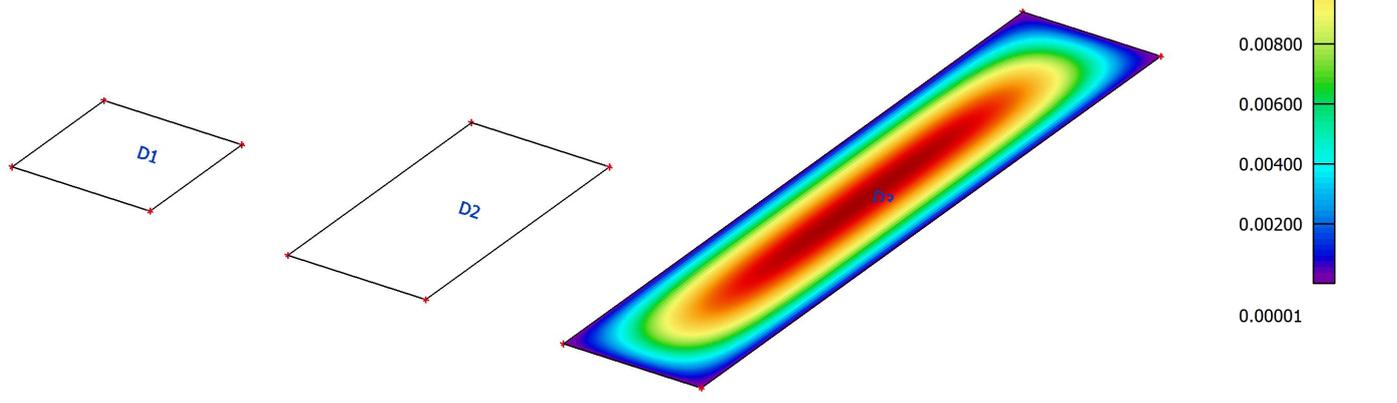
4.8. 2D displacement; u_z

Valeur: u_z
Calcul linéaire
Cas de charge: LC2
Extrême: Elément
Sélection: D2
Position: Aux centres. Système: SCL
maillage EF



4.9. 2D displacement; u_z

Valeur: u_z
 Calcul linéaire
 Cas de charge: LC2
 Extrême: Elément
 Sélection: D3
 Position: Aux centres. Système: SCL
 maillage EF



4.10. 2D internal forces

Linear calculation

Load case: LC2

Extreme: Member

Selection: All

Location: In nodes avg. on macro. System: LCS mesh element

Basic magnitudes

| Name | Mesh | x [m] | y [m] | z [m] | Case | m _x [Nm/m] | m _y [Nm/m] |
|------|--------------------------------|----------|----------|----------|------|--------------------------|--------------------------|
| D1 | Element: 1151; Node: 1226 | 0,000 | 0,480 | 0,000 | LC2 | 0,0003 | -0,0001 |
| D1 | Element: 1225; Node: 1301 | 0,500 | 0,500 | 0,000 | LC2 | -0,0481 | -0,0481 |
| D1 | Element: 24; Node: 49 | 0,480 | 0,000 | 0,000 | LC2 | -0,0001 | 0,0003 |
| D2 | Element: 4975; Node: 5177 | 2,500 | 1,000 | 0,000 | LC2 | -0,1019 | -0,0464 |
| D2 | Element: 4251; Node: 4439 | 2,000 | 0,720 | 0,000 | LC2 | 0,0004 | -0,0003 |
| D2 | Element: 2501; Node: 5 | 2,000 | 0,000 | 0,000 | LC2 | -0,0494 | -0,0494 |
| D2 | Element: 2522; Node: 2646 | 2,440 | 0,000 | 0,000 | LC2 | 0,0000 | 0,0003 |
| D3 | Element: 13675; Node: 14102 | 4,500 | 2,480 | 0,000 | LC2 | -0,1246 | -0,0377 |
| D3 | Element: 9501; Node: 9845 | 4,000 | 0,820 | 0,000 | LC2 | 0,0004 | -0,0003 |
| D3 | Element: 7501; Node: 9 | 4,000 | 0,000 | 0,000 | LC2 | -0,0507 | -0,0507 |
| D3 | Element: 7525; Node: 7803 | 4,500 | 0,000 | 0,000 | LC2 | 0,0000 | 0,0003 |

5. EXPECTED AFNOR RESULTS

Plate D1 :

Max deflection : 0.0443

Mx max = 0.0479

My max = 0.0479

Plate D2 :

Max deflection : 0.1106

Mx max = 0.1017

My max = 0.0464

Plate D3 :

Max deflection : 0.1416

Mx max = 0.1246

My max = 0.0375

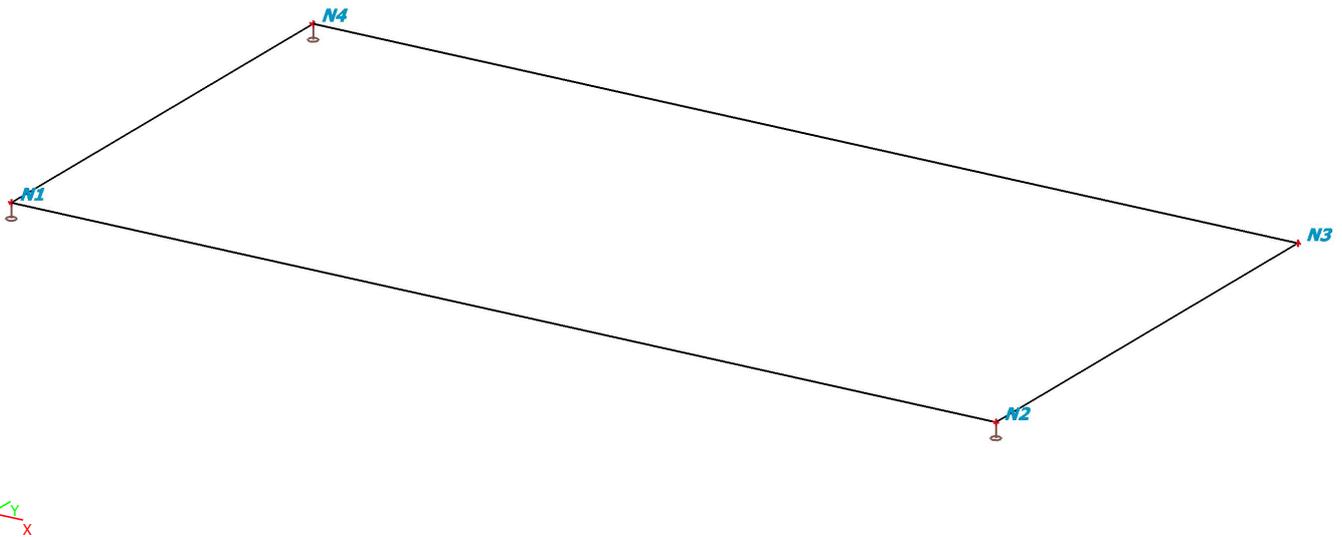
REFERENCE : "Guide de validation des progiciels de calcul de structures" AFNOR, 1990

1. TESTCASE DESCRIPTION

Simply supported rectangular plate with bending moment
Specification: Plate - Pressure - Simple support – Nodal moment

2. MODEL

2.1. Analysis model



2.2. Nodes

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] |
|------|-------------|-------------|-------------|
| N1 | 0,000 | 0,000 | 0,000 |
| N2 | 40,000 | 0,000 | 0,000 |
| N3 | 40,000 | 20,000 | 0,000 |
| N4 | 0,000 | 20,000 | 0,000 |

2.3. 2D members

| Name | Layer | Type | Element type | Material | Thickness type | Th. [mm] |
|------|---------|------------|--------------|----------|----------------|----------|
| D1 | Calque1 | dalle (90) | Standard | S 235 | constant | 1000 |

2.4. Nodal supports

| Name | Node | System | Type | X | Y | Z | Rx | Ry | Rz |
|------|------|--------|----------|------|------|-------|------|------|------|
| Sn1 | N1 | GCS | Standard | Free | Free | Rigid | Free | Free | Free |
| Sn2 | N4 | GCS | Standard | Free | Free | Rigid | Free | Free | Free |
| Sn3 | N2 | GCS | Standard | Free | Free | Rigid | Free | Free | Free |

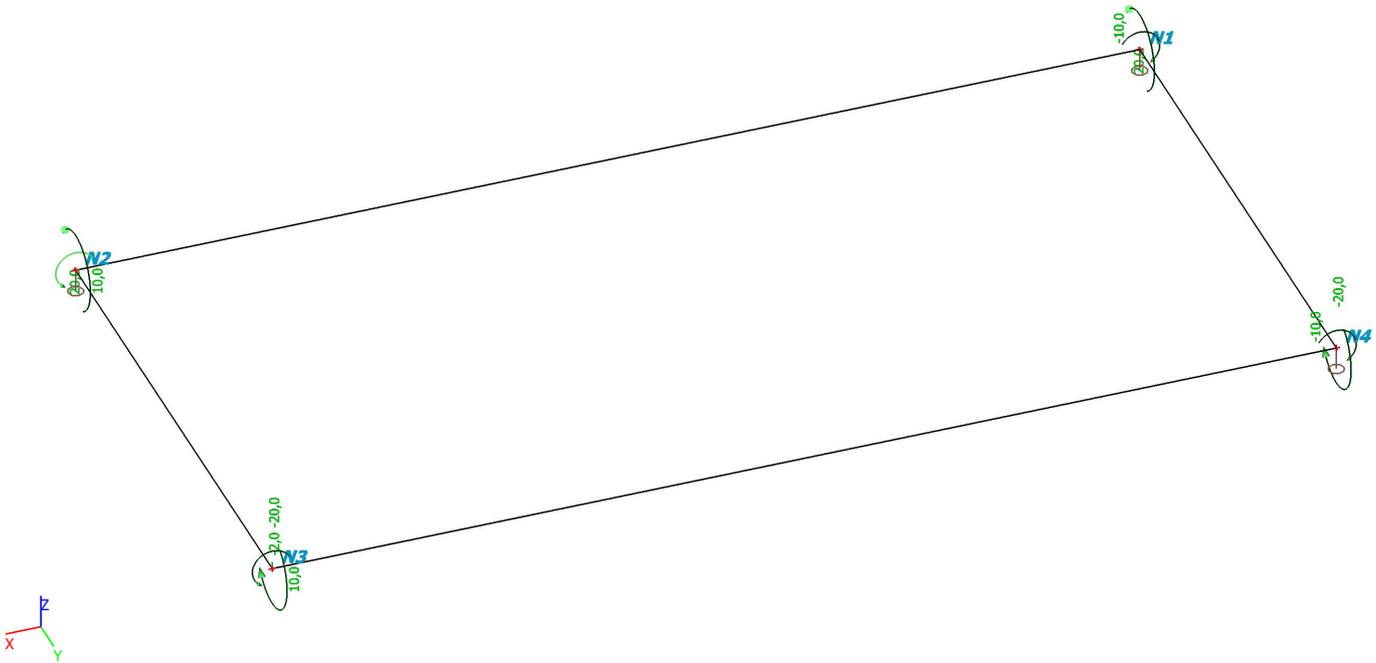
2.5. Materials

Steel EC3

| Name | ρ [kg/m ³] | E_{mod} [MPa] | μ | Limit inférieure [mm] | Limite supérieure [mm] | F_y [MPa] | F_u [MPa] | Colour |
|-------|-----------------------------|-----------------|-----------------|-----------------------|------------------------|-------------|-------------|--------|
| | | G_{mod} [MPa] | α [m/mK] | | | | | |
| S 235 | 7850,00 | 1,0000e-03 | 0.3 | 0 | 40 | 235,0 | 360,0 | ■ |
| | | 3,8462e-04 | 0,01e-003 | 40 | 80 | 215,0 | 360,0 | |

3. LOAD

3.1. LC1 / Tot. value



3.2. Point force in node

| Name | Node | Load case | System | Dir | Type | Value - F [N] |
|------|------|-----------------|--------|-----|-------|---------------|
| F1 | N3 | LC2 - Permanent | GCS | Z | Force | -2,0 |

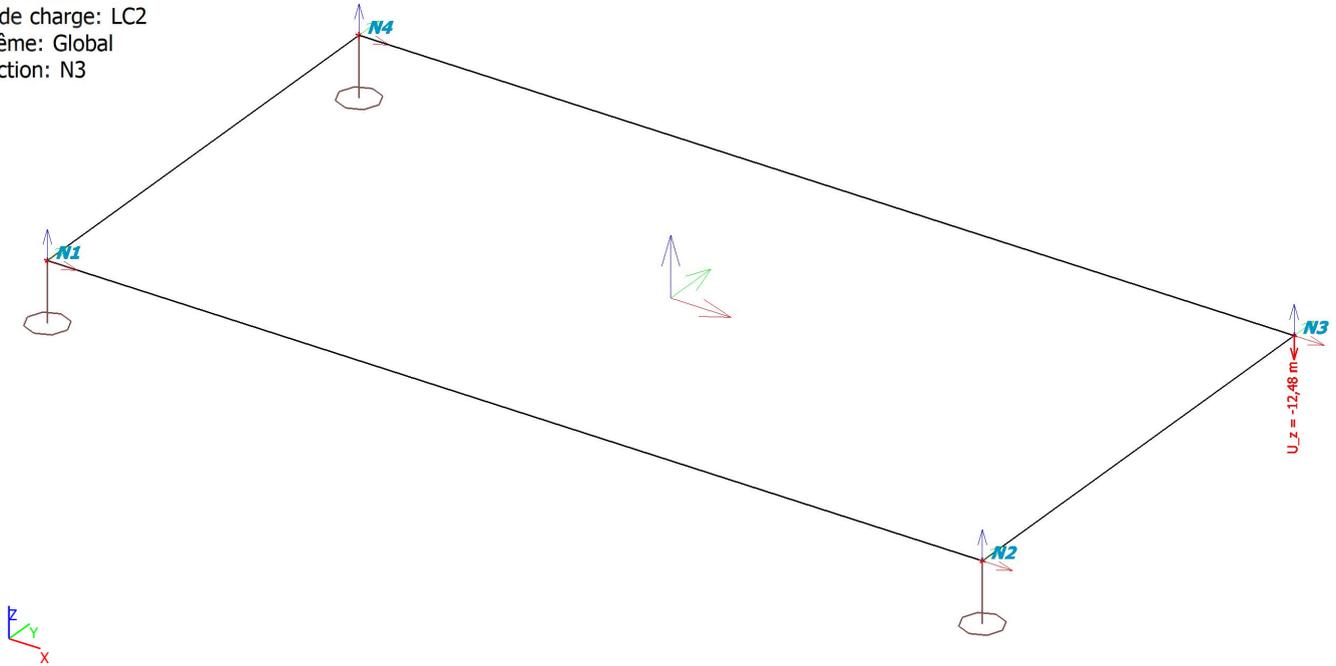
3.3. Moment in node

| Name | Node | Load case | System | Dir | Type | Value - M [Nm] |
|------|------|-----------------|--------|-----|--------|----------------|
| M1 | N2 | LC2 - Permanent | GCS | My | Moment | 10,0 |
| M2 | N3 | LC2 - Permanent | GCS | My | Moment | 10,0 |
| M3 | N1 | LC2 - Permanent | GCS | My | Moment | -10,0 |
| M4 | N4 | LC2 - Permanent | GCS | My | Moment | -10,0 |
| M5 | N2 | LC2 - Permanent | GCS | Mx | Moment | 20,0 |
| M6 | N1 | LC2 - Permanent | GCS | Mx | Moment | 20,0 |
| M7 | N4 | LC2 - Permanent | GCS | Mx | Moment | -20,0 |
| M8 | N3 | LC2 - Permanent | GCS | Mx | Moment | -20,0 |

4. RESULTS

4.1. Displacement of nodes; U_z

Valeur: U_z
Calcul linéaire
Cas de charge: LC2
Extrême: Global
Sélection: N3



4.2. Displacement of nodes

Linear calculation
Load case: LC2
Extreme: Node
Selection: N3

| Name | Case | U _z [m] |
|------|------|-----------------------|
| N3 | LC2 | -12,48 |

5. EXPECTED AFNOR RESULTS

Displacement uz in node N3= -12,48 mm

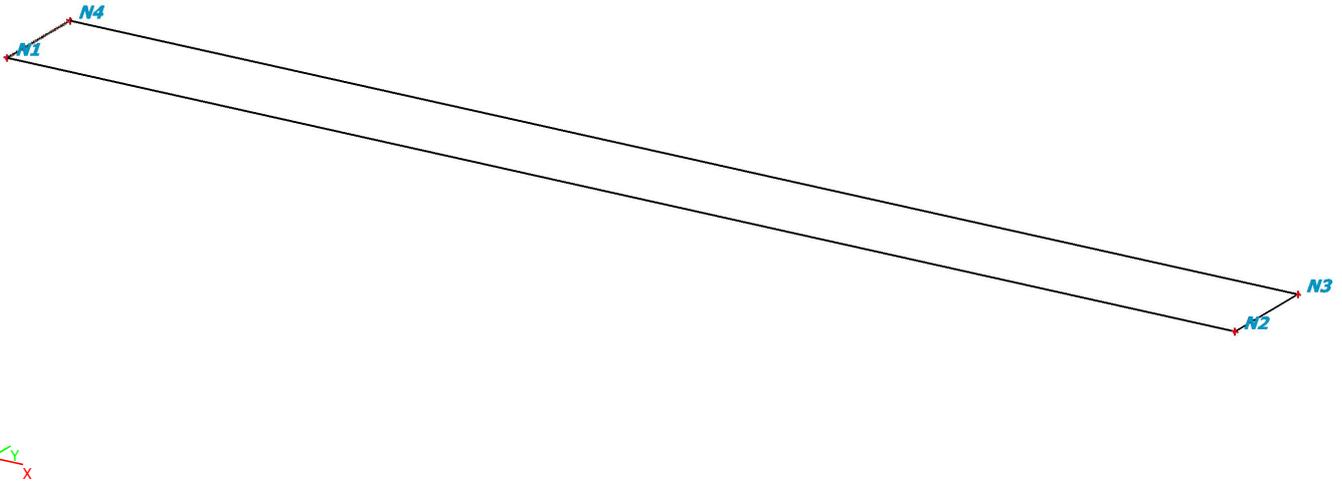
REFERENCE : "Guide de validation des progiciels de calcul de structures" AFNOR, 1990

1. TESTCASE DESCRIPTION

Plate under perpendicular shear with one edge fixed

2. MODEL

2.1. Analysis model



2.2. Nodes

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] |
|------|-------------|-------------|-------------|
| N1 | 0,000 | 0,000 | 0,000 |
| N2 | 12,000 | 0,000 | 0,000 |
| N3 | 12,000 | 1,000 | 0,000 |
| N4 | 0,000 | 1,000 | 0,000 |

2.3. 2D members

| Name | Layer | Type | Element type | Material | Thickness type | Th. [mm] |
|------|---------|------------|--------------|----------|----------------|----------|
| D1 | Calque1 | dalle (90) | Standard | S 235 | constant | 50 |

2.4. Supports on 2D member edge

| Name | 2D member Edge | Orig Coor | Pos x ₁ Pos x ₂ | X | Y | Z | Rx | Ry | Rz |
|------|----------------|--------------------|---------------------------------------|-------|-------|-------|-------|-------|-------|
| Sle2 | D1 4 | From start Rela | 0.000 1.000 | Rigid | Rigid | Rigid | Rigid | Rigid | Rigid |

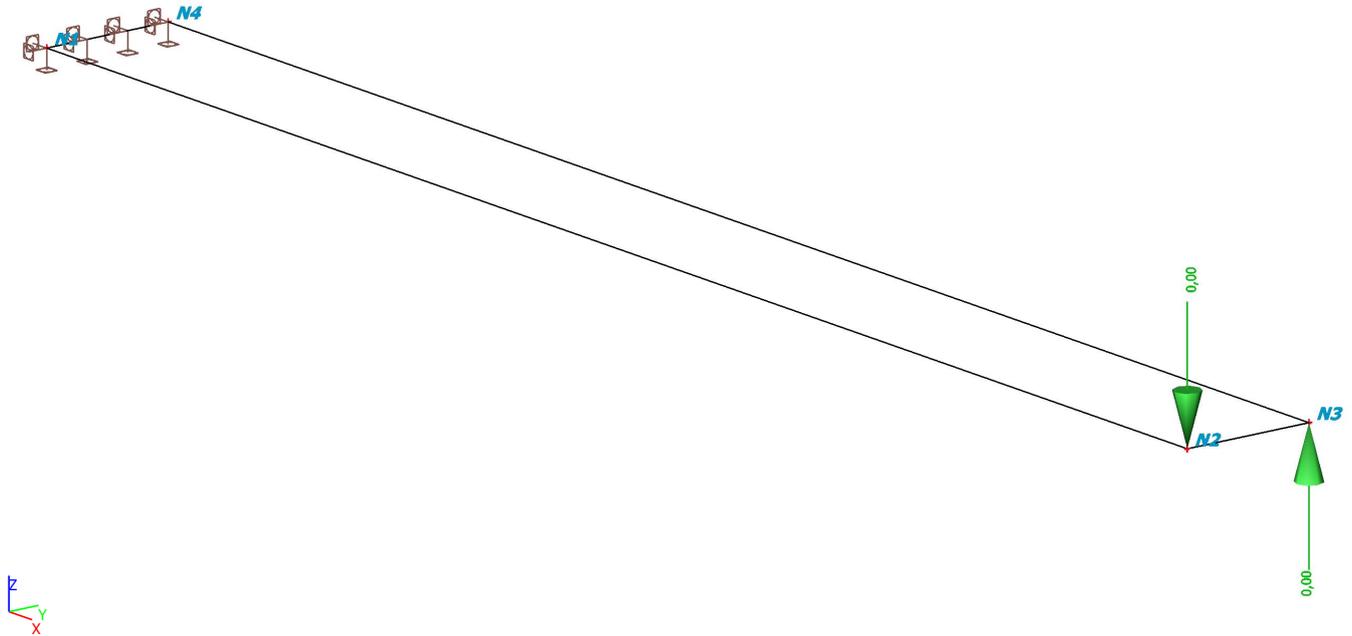
2.5. Materials

Steel EC3

| Name | ρ [kg/m ³] | E _{mod} [MPa] | μ | Limit inférieure [mm] | Limite supérieure [mm] | F _y [MPa] | F _u [MPa] | Colour |
|-------|------------------------|------------------------|-----------|-----------------------|------------------------|----------------------|----------------------|--------|
| | | G _{mod} [MPa] | α [m/mK] | | | | | |
| S 235 | 7850,00 | 1,0000e+01 | 0.25 | 0 | 40 | 235,0 | 360,0 | ■ |
| | | 4,0000e+00 | 0,01e-003 | 40 | 80 | 215,0 | 360,0 | |

3. LOAD

3.1. LC1 / Tot. value



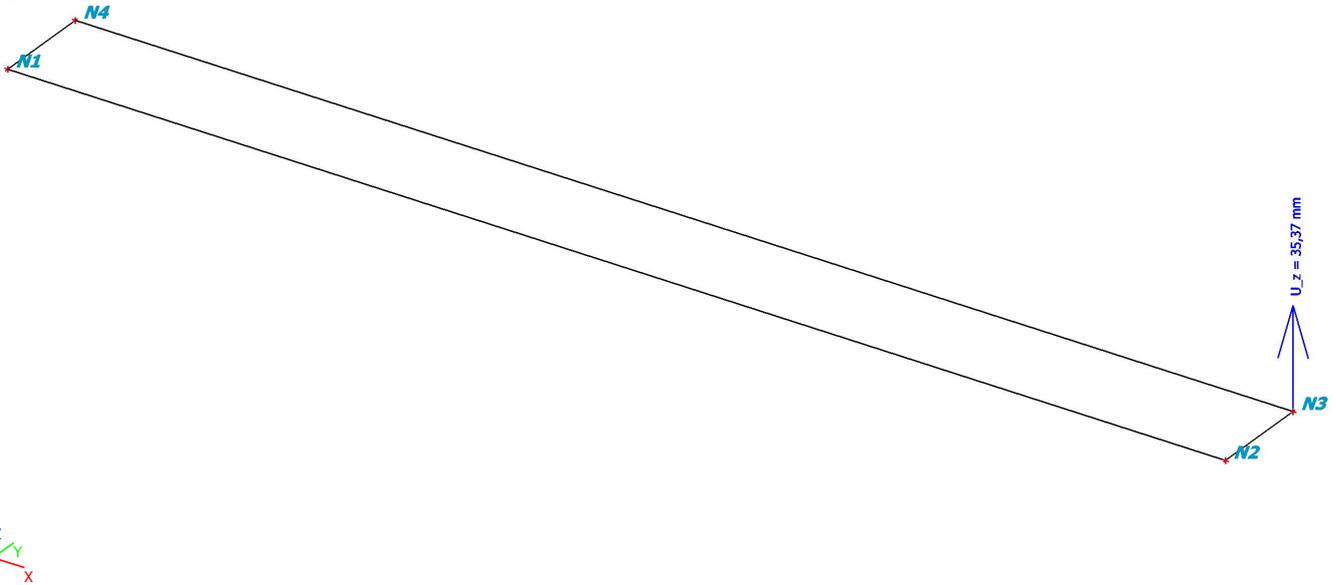
3.2. Point force in node

| Name | Node | Load case | System | Dir | Type | Value - F [kN] |
|------|------|-----------------|--------|-----|-------|----------------|
| F1 | N2 | LC2 - Permanent | GCS | Z | Force | 0,00 |
| F2 | N3 | LC2 - Permanent | GCS | Z | Force | 0,00 |

4. RESULTS

4.1. Displacement of nodes; U_z

Valeur: U_z
Calcul linéaire
Cas de charge: LC2
Extrême: Global
Sélection: N3



4.2. Displacement of nodes

Linear calculation
Load case: LC2
Extreme: Node
Selection: N3

| Name | Case | U _z [mm] |
|------|------|------------------------|
| N3 | LC2 | 35,37 |

5. EXPECTED AFNOR RESULTS

Displacement uz in node N3= 35,37mm

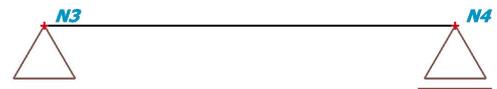
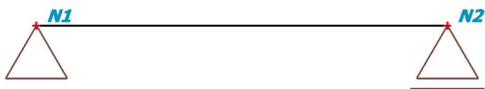
REFERENCE : "Guide de validation des progiciels de calcul de structures" AFNOR, 1990

1. TESTCASE DESCRIPTION

Modal analysis of a simply supported beam with and without prestress

2. MODEL

2.1. Analysis model



2.2. Nodes

| Name | Coord X [m] | Coord Z [m] | Member | Data |
|------|-------------|-------------|--------|------|
| N1 | 0,000 | 0,000 | B1 | Sn1 |
| N2 | 2,000 | 0,000 | B1 | Sn2 |
| N3 | 4,000 | 0,000 | B2 | Sn3 |
| N4 | 6,000 | 0,000 | B2 | Sn4 |

2.3. Members

| Name | Cross-section | Material | Length [m] | Beg. node | End node | Type |
|------|--------------------------|----------------|------------|-----------|----------|-----------|
| B1 | CS3 - Rectangle (50; 50) | S 235 modified | 2,000 | N1 | N2 | beam (80) |
| B2 | CS3 - Rectangle (50; 50) | S 235 modified | 2,000 | N3 | N4 | beam (80) |

2.4. Nodal supports

| Name | Node | System | Type | X | Z | Ry |
|------|------|--------|----------|-------|-------|------|
| Sn1 | N1 | GCS | Standard | Rigid | Rigid | Free |
| Sn2 | N2 | GCS | Standard | Free | Rigid | Free |
| Sn3 | N3 | GCS | Standard | Rigid | Rigid | Free |
| Sn4 | N4 | GCS | Standard | Free | Rigid | Free |

2.5. Materials

Steel EC3

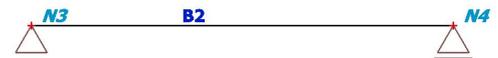
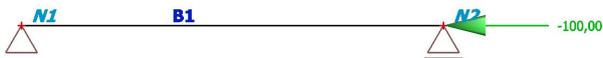
| Name | ρ [kg/m ³] | E_{mod} [MPa] | μ | Limit inférieure [mm] | Limite supérieure [mm] | F_y [MPa] | F_u [MPa] | Colour |
|----------------|--------------------------------|--------------------|--------------------|--------------------------|---------------------------|----------------|----------------|---|
| | | G_{mod} [MPa] | α [m/mK] | | | | | |
| S 235 modified | 7800,00 | 2,0000e+05 | 0.3 | 0 | 40 | 235,0 | 360,0 |  |
| | | 7,6923e+04 | 0,01e-003 | 40 | 80 | 215,0 | 360,0 | |

2.6. Cross-sections

| CS3 | | |
|--|----------------|------------|
| Type | Rectangle | |
| Detailed | 50; 50 | |
| Item material | S 235 modified | |
| A [m ²] | 2,5000e-03 | |
| A _y [m ²], A _z [m ²] | 2,0833e-05 | 2,0833e-05 |
| A _L [m ² /m], A _D [m ² /m] | 2,0000e-01 | 2,0000e-01 |
| c _{y,UCS} [mm], c _{z,UCS} [mm] | 25 | 25 |
| α [deg] | 0,00 | |
| I _y [m ⁴], I _z [m ⁴] | 5,2083e-07 | 5,2083e-09 |
| i _y [mm], i _z [mm] | 14 | 1 |
| W _{el,y} [m ³], W _{el,z} [m ³] | 2,0833e-05 | 2,0833e-07 |
| W _{pl,y} [m ³], W _{pl,z} [m ³] | 3,1250e-05 | 3,1250e-05 |
| M _{pl,y,+} [Nm], M _{pl,y,-} [Nm] | 7343,75 | 7343,75 |
| M _{pl,z,+} [Nm], M _{pl,z,-} [Nm] | 7343,75 | 7343,75 |
| d _y [mm], d _z [mm] | 0 | |
| I _E [m ⁴], I _w [m ⁶] | 8,7957e-09 | 0,0000e+00 |
| β _y [mm], β _z [mm] | 0 | |
| Picture | | |

3. LOAD and MASS

3.1. LC1 / Tot. value



3.2. Point force on beam

| Name | Member | System | Value - F [kN] | Pos x | Coor | Rep (n) |
|------|-----------------|--------|----------------|-------|----------|-----------|
| | Load case | Dir | Type | | Orig | Regularly |
| Fb2 | B1 | GCS | -100,00 | 0.000 | Rela | 1 |
| | LC2 - Permanent | X | Force | | From end | |

3.3. Mass groups

| Name | Load case |
|------|--------------------|
| MG1 | LC1 - Poids propre |

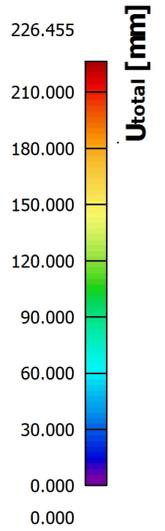
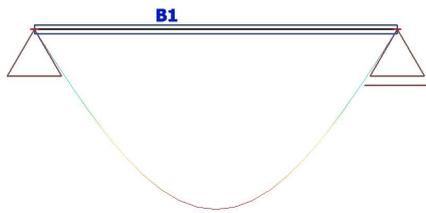
4. RESULTS

4.1. Eigen frequencies

| N | f [Hz] | ω [1/s] | ω^2 [1/s ²] | T [s] |
|-------------------------------|-----------|-------------------|-----------------------------------|----------|
| Mass combination : CM1 | | | | |
| 1 | 22,43 | 140,95 | 19866,96 | 0,04 |
| 2 | 28,70 | 180,33 | 32519,53 | 0,03 |
| 3 | 109,08 | 685,34 | 469694,71 | 0,01 |
| 4 | 114,81 | 721,32 | 520303,68 | 0,01 |

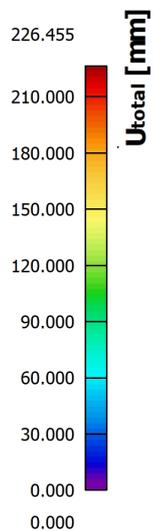
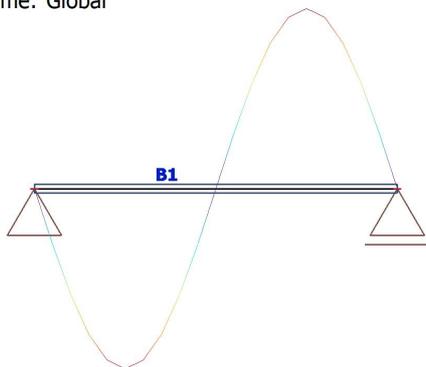
4.2. 3D displacement; U_{total}

Valeur: U_{total}
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/1 - 22,43
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



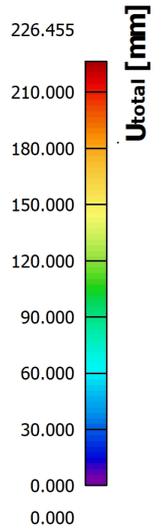
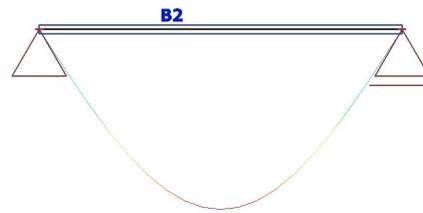
4.3. 3D displacement; U_{total}

Valeur: U_{total}
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/3 - 109,08
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



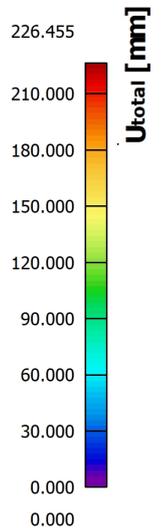
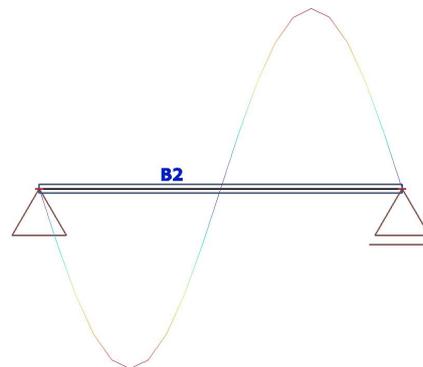
4.4. 3D displacement; U_{total}

Valeur: U_{total}
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/2 - 28,70
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



4.5. 3D displacement; U_{total}

Valeur: U_{total}
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/4 - 114,81
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



5. EXPECTED AFNOR RESULTS

Beam B1 (with initial stress):

f1 = 22.434 Hz

f2 = 109.080 Hz

Beam B2 (without initial stress):

f1 = 28.702 Hz

f2= 114.807 Hz

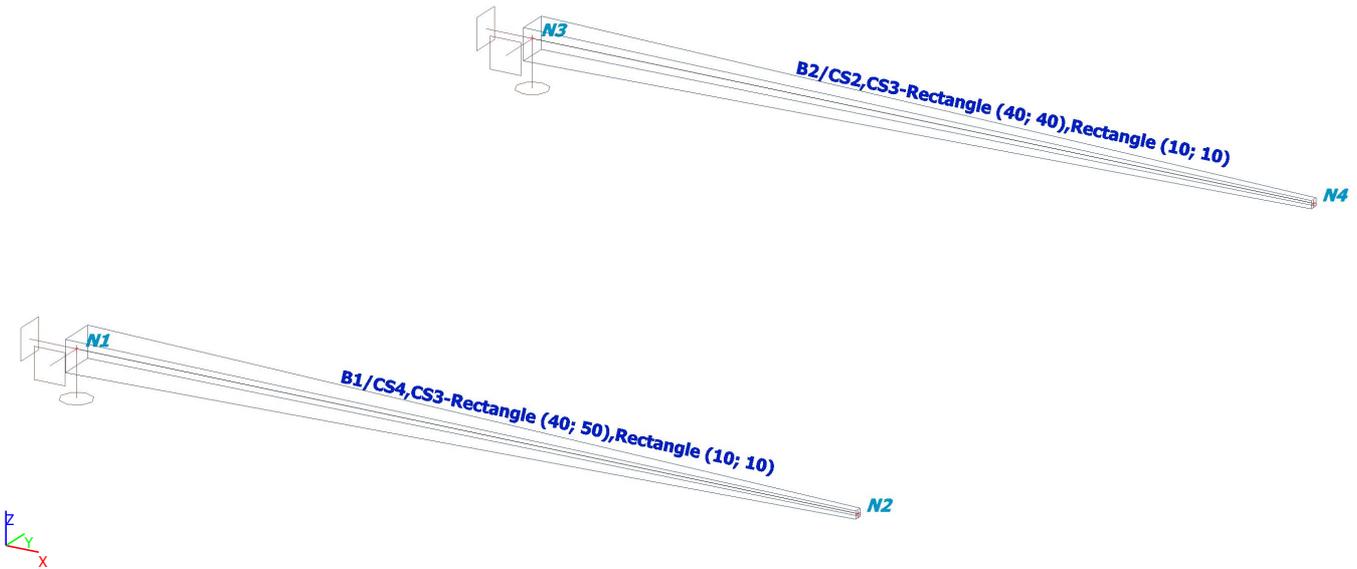
REFERENCE : "Guide de validation des progiciels de calcul de structures" AFNOR, 1990

1. TESTCASE DESCRIPTION

Modal analysis of cantilever beams with variable cross-sections

2. MODEL

2.1. Analysis model



2.2. Nodes

| Name | Coord X [m] | Coord Y [m] | Member | Data |
|------|-------------|-------------|--------|------|
| N1 | 0,000 | 0,000 | B1 | Sn1 |
| N2 | 1,000 | 0,000 | B1 | |
| N3 | -0,001 | 1,020 | B2 | Sn2 |
| N4 | 0,999 | 1,020 | B2 | |

2.3. Members

| Name | Cross-section | Material | Length [m] | Beg. node | End node | Type |
|------|---------------|----------|------------|-----------|----------|-----------|
| B1 | CS1 - IPE240 | S 235 | 1,000 | N1 | N2 | beam (80) |
| B2 | CS1 - IPE240 | S 235 | 1,000 | N3 | N4 | beam (80) |

2.4. Arbitrary members

| AP | | | |
|--|-------|--------------------------|--------------------------|
| Member | B1 | | |
| Coor | Rela | | |
| length 1, C _{ss} 1(1), C _{ss} 2(1) | 1.000 | CS4 - Rectangle (40; 50) | CS3 - Rectangle (10; 10) |
| length 2, C _{ss} 1(2), C _{ss} 2(2) | 0.000 | CS3 - Rectangle (10; 10) | |
| AP1 | | | |
| Member | B2 | | |
| Coor | Rela | | |
| length 1, C _{ss} 1(1), C _{ss} 2(1) | 1.000 | CS2 - Rectangle (40; 40) | CS3 - Rectangle (10; 10) |
| length 2, C _{ss} 1(2), C _{ss} 2(2) | 0.000 | CS3 - Rectangle (10; 10) | |

2.5. Nodal supports

| Name | Node | System | Type | Z | Rx | Ry |
|------|------|--------|----------|-------|-------|-------|
| Sn1 | N1 | GCS | Standard | Rigid | Rigid | Rigid |
| Sn2 | N3 | GCS | Standard | Rigid | Rigid | Rigid |

2.6. Materials

Steel EC3

| Name | ρ [kg/m ³] | E_{mod} [MPa] | μ | Limit inférieure [mm] | Limite supérieure [mm] | F_y [MPa] | F_u [MPa] | Colour |
|-------|--------------------------------|--------------------|--------------------|--------------------------|---------------------------|----------------|----------------|--------|
| | | G_{mod} [MPa] | α [m/mK] | | | | | |
| S 235 | 7800,00 | 2,0000e+05 | 0.3 | 0 | 40 | 235,0 | 360,0 | ■ |
| | | 7,6923e+04 | 0,01e-003 | 40 | 80 | 215,0 | 360,0 | |

2.7. Cross-sections

| CS2 | | |
|--|------------|------------|
| Type | Rectangle | |
| Detailed | 40; 40 | |
| Item material | S 235 | |
| A [m ²] | 1,6000e-03 | |
| A _y [m ²], A _z [m ²] | 1,3333e-03 | 1,3333e-03 |
| A _L [m ² /m], A _D [m ² /m] | 1,6000e-01 | 1,6000e-01 |
| c _{y,UCS} [mm], c _{z,UCS} [mm] | 20 | 20 |
| α [deg] | 0,00 | |
| I _y [m ⁴], I _z [m ⁴] | 2,1333e-07 | 2,1333e-07 |
| i _y [mm], i _z [mm] | 12 | 12 |
| W _{el,y} [m ³], W _{el,z} [m ³] | 1,0667e-05 | 1,0667e-05 |
| W _{pl,y} [m ³], W _{pl,z} [m ³] | 1,6000e-05 | 1,6000e-05 |
| M _{pl,y,+} [Nm], M _{pl,y,-} [Nm] | 3760,00 | 3760,00 |
| M _{pl,z,+} [Nm], M _{pl,z,-} [Nm] | 3760,00 | 3760,00 |
| d _y [mm], d _z [mm] | 0 | 0 |
| I _t [m ⁴], I _w [m ⁶] | 3,6027e-07 | 0,0000e+00 |
| β _y [mm], β _z [mm] | 0 | 0 |
| Picture | | |

| CS4 | | |
|--|------------|------------|
| Type | Rectangle | |
| Detailed | 40; 50 | |
| Item material | S 235 | |
| A [m ²] | 2,0000e-03 | |
| A _y [m ²], A _z [m ²] | 1,6667e-03 | 1,6667e-03 |
| A _L [m ² /m], A _D [m ² /m] | 1,8000e-01 | 1,8000e-01 |
| c _{y,UCS} [mm], c _{z,UCS} [mm] | 25 | 20 |
| α [deg] | 0,00 | |
| I _y [m ⁴], I _z [m ⁴] | 2,6667e-07 | 4,1667e-07 |
| i _y [mm], i _z [mm] | 12 | 14 |
| W _{el,y} [m ³], W _{el,z} [m ³] | 1,3333e-05 | 1,6667e-05 |
| W _{pl,y} [m ³], W _{pl,z} [m ³] | 2,0000e-05 | 2,5000e-05 |
| M _{pl,y,+} [Nm], M _{pl,y,-} [Nm] | 4700,00 | 4700,00 |
| M _{pl,z,+} [Nm], M _{pl,z,-} [Nm] | 5875,00 | 5875,00 |
| d _y [mm], d _z [mm] | 0 | 0 |
| I _t [m ⁴], I _w [m ⁶] | 5,4984e-07 | 0,0000e+00 |
| β _y [mm], β _z [mm] | 0 | 0 |
| Picture | | |

| CS3 | | |
|--|------------|------------|
| Type | Rectangle | |
| Detailed | 10; 10 | |
| Item material | S 235 | |
| A [m ²] | 1,0000e-04 | |
| A _y [m ²], A _z [m ²] | 8,3333e-05 | 8,3333e-05 |
| A _L [m ² /m], A _D [m ² /m] | 4,0000e-02 | 4,0000e-02 |
| c _{y,UCS} [mm], c _{z,UCS} [mm] | 5 | 5 |
| α [deg] | 0,00 | |
| I _y [m ⁴], I _z [m ⁴] | 8,3333e-10 | 8,3333e-10 |
| i _y [mm], i _z [mm] | 3 | 3 |
| W _{el,y} [m ³], W _{el,z} [m ³] | 1,6667e-07 | 1,6667e-07 |
| W _{pl,y} [m ³], W _{pl,z} [m ³] | 2,5000e-07 | 2,5000e-07 |
| M _{pl,y,+} [Nm], M _{pl,y,-} [Nm] | 58,75 | 58,75 |
| M _{pl,z,+} [Nm], M _{pl,z,-} [Nm] | 58,75 | 58,75 |
| d _y [mm], d _z [mm] | 0 | 0 |
| I _t [m ⁴], I _w [m ⁶] | 1,4073e-09 | 0,0000e+00 |
| β _y [mm], β _z [mm] | 0 | 0 |
| Picture | | |

3. LOAD and MASS

3.1. Mass groups

| Name | Load case |
|------|--------------------|
| MG1 | LC1 - Poids propre |

4. RESULTS

4.1. Eigen frequencies

| N | f [Hz] | ω [1/s] | ω^2 [1/s ²] | T [s] |
|-------------------------------|-----------|-------------------|-----------------------------------|----------|
| Mass combination : CM1 | | | | |
| 1 | 54,17 | 340,38 | 115857,84 | 0,02 |
| 2 | 56,54 | 355,26 | 126211,87 | 0,02 |
| 3 | 171,88 | 1079,91 | 1166197,96 | 0,01 |
| 4 | 175,73 | 1104,11 | 1219056,08 | 0,01 |
| 5 | 384,23 | 2414,09 | 5827850,05 | 0,00 |
| 6 | 388,78 | 2442,72 | 5966859,07 | 0,00 |
| 7 | 696,70 | 4377,38 | 19161477,19 | 0,00 |
| 8 | 701,68 | 4408,64 | 19436098,08 | 0,00 |
| 9 | 1111,04 | 6980,67 | 48729819,24 | 0,00 |
| 10 | 1116,28 | 7013,62 | 49190808,83 | 0,00 |

4.2. 3D displacement; U_{total}

Valeur: U_{total}

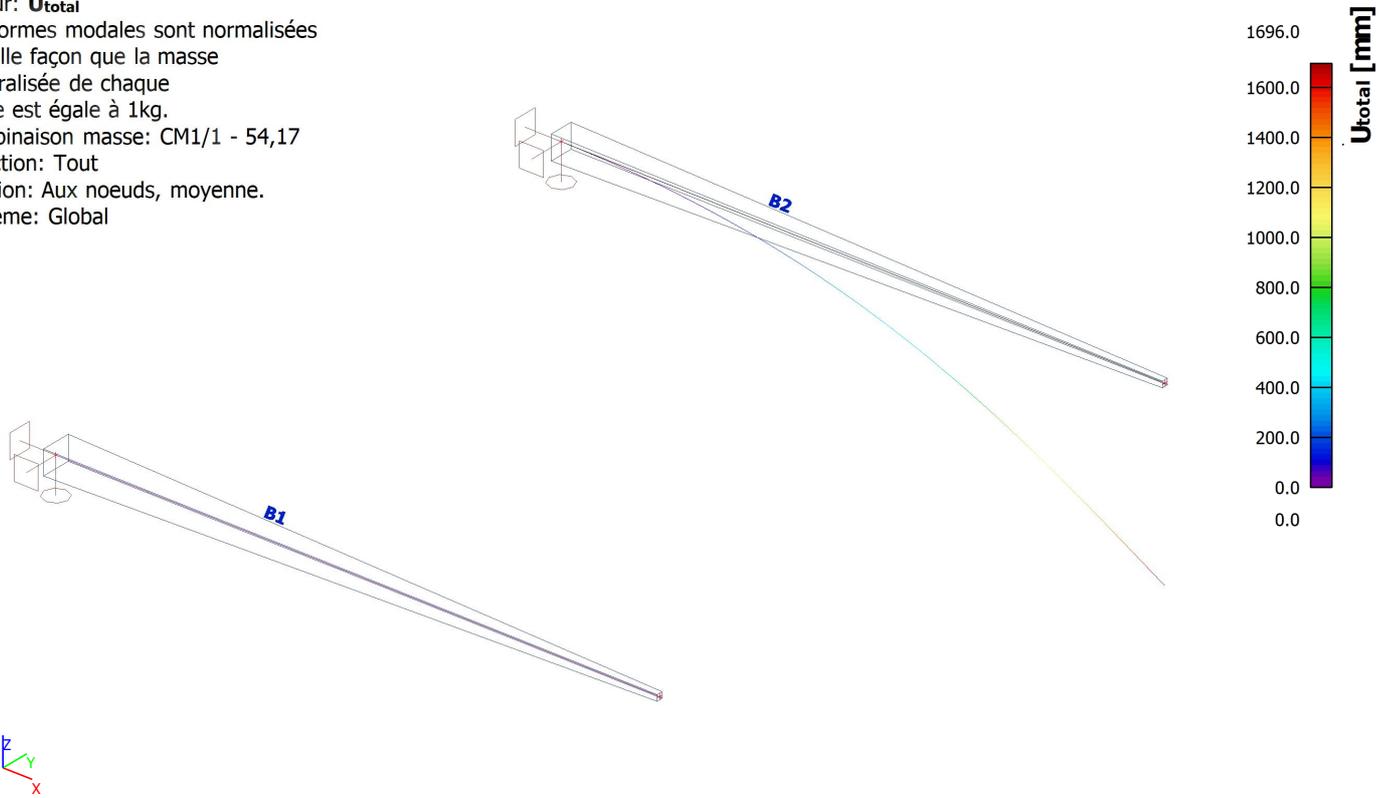
Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.

Combinaison masse: CM1/1 - 54,17

Sélection: Tout

Position: Aux noeuds, moyenne.

Système: Global



4.3. 3D displacement; U_{total}

Valeur: U_{total}

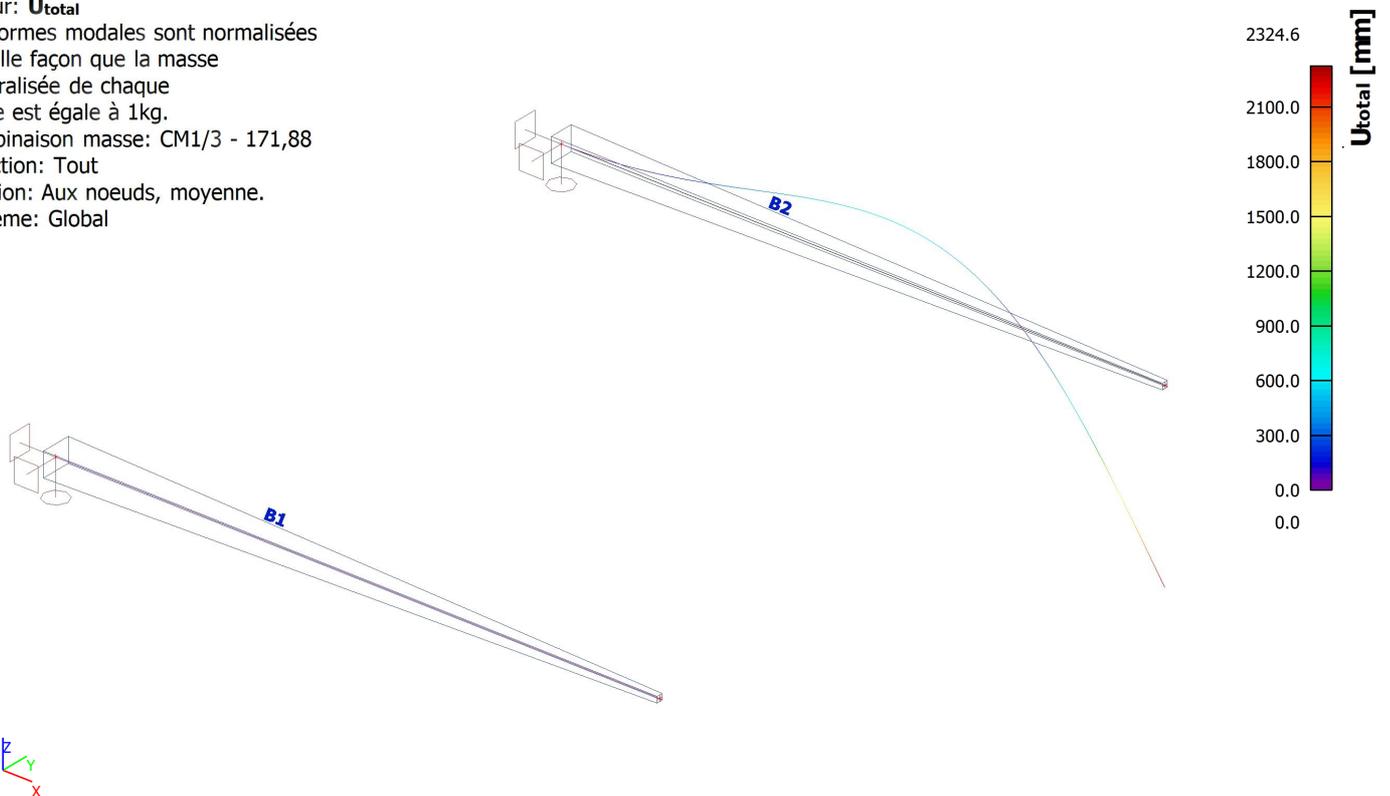
Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.

Combinaison masse: CM1/3 - 171,88

Sélection: Tout

Position: Aux noeuds, moyenne.

Système: Global



4.4. 3D displacement; U_{total}

Valeur: U_{total}

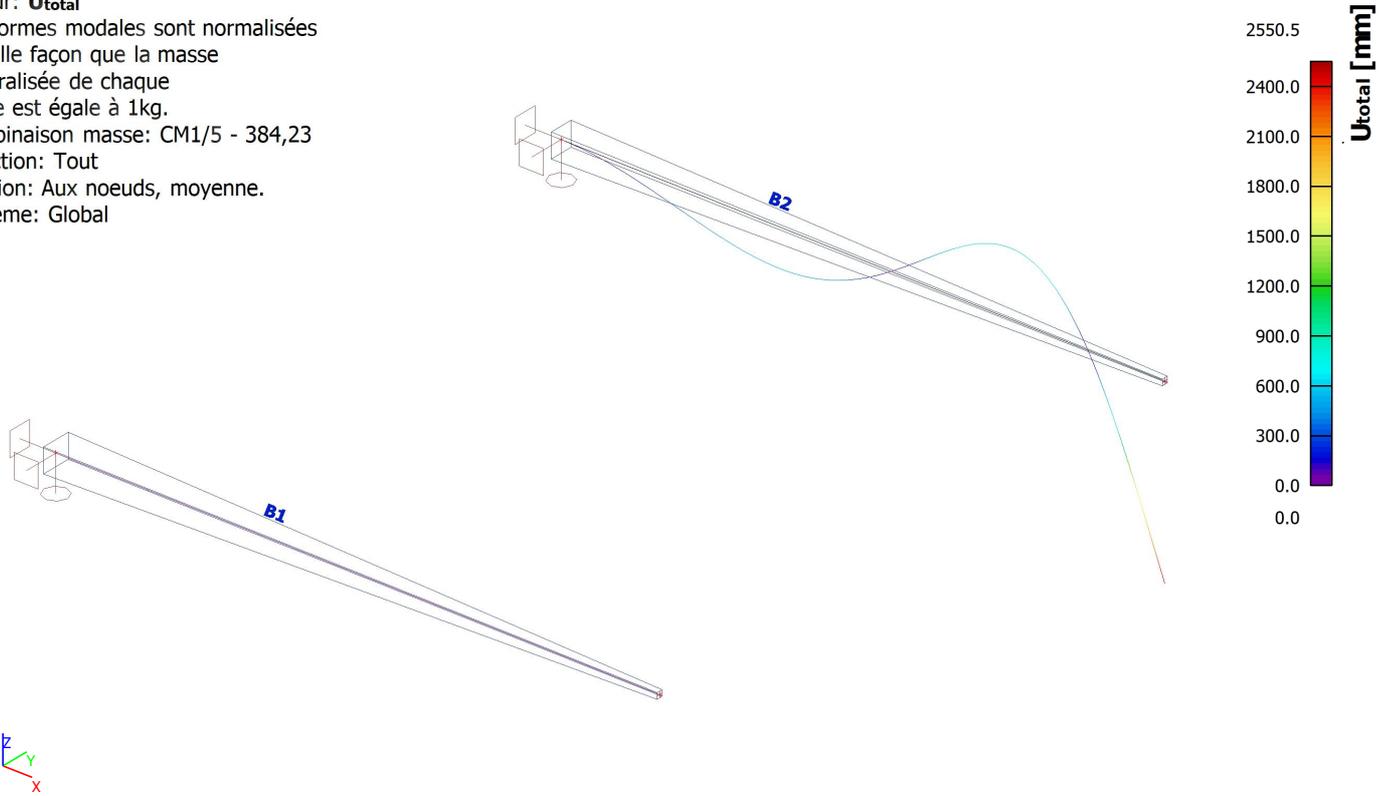
Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.

Combinaison masse: CM1/5 - 384,23

Sélection: Tout

Position: Aux noeuds, moyenne.

Système: Global



4.5. 3D displacement; U_{total}

Valeur: U_{total}

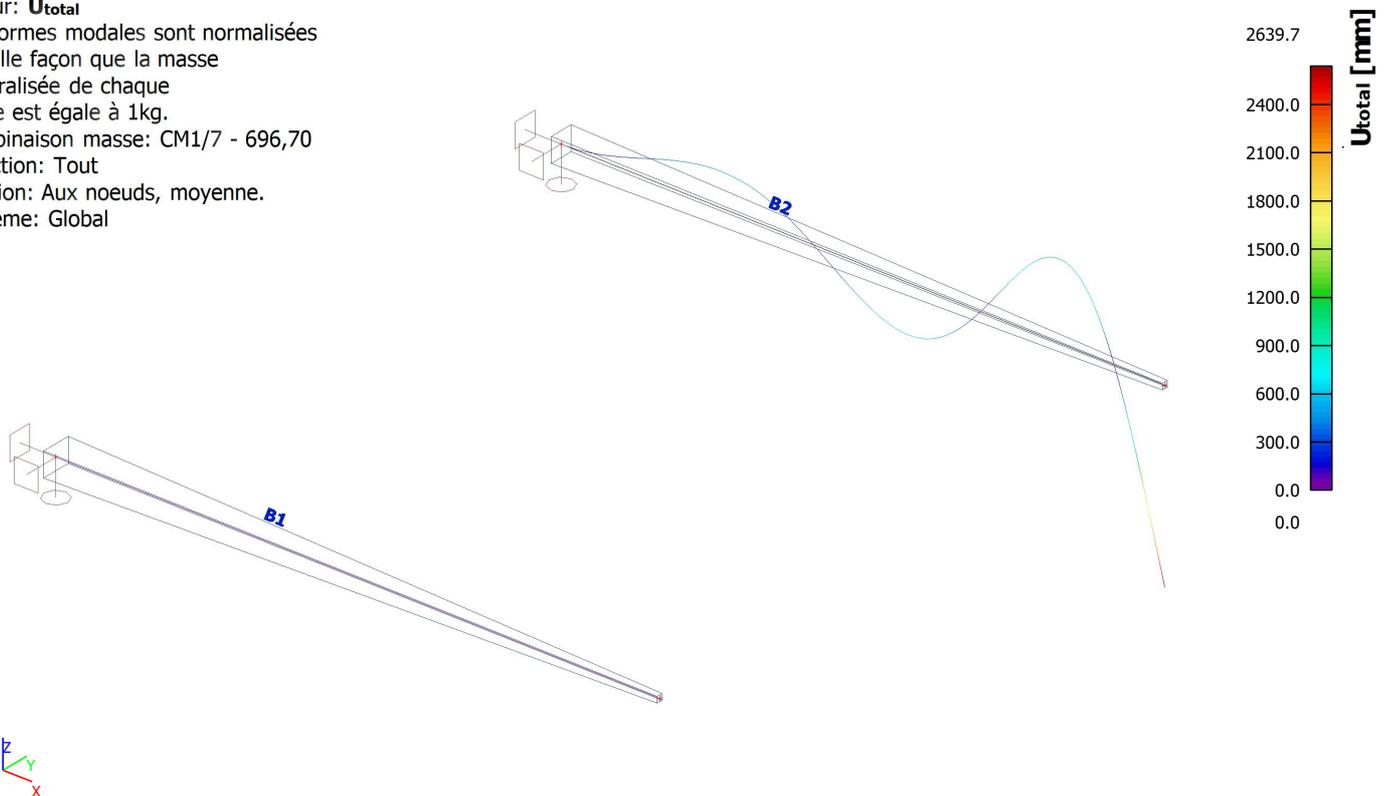
Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.

Combinaison masse: CM1/7 - 696,70

Sélection: Tout

Position: Aux noeuds, moyenne.

Système: Global



4.6. 3D displacement; U_{total}

Valeur: U_{total}

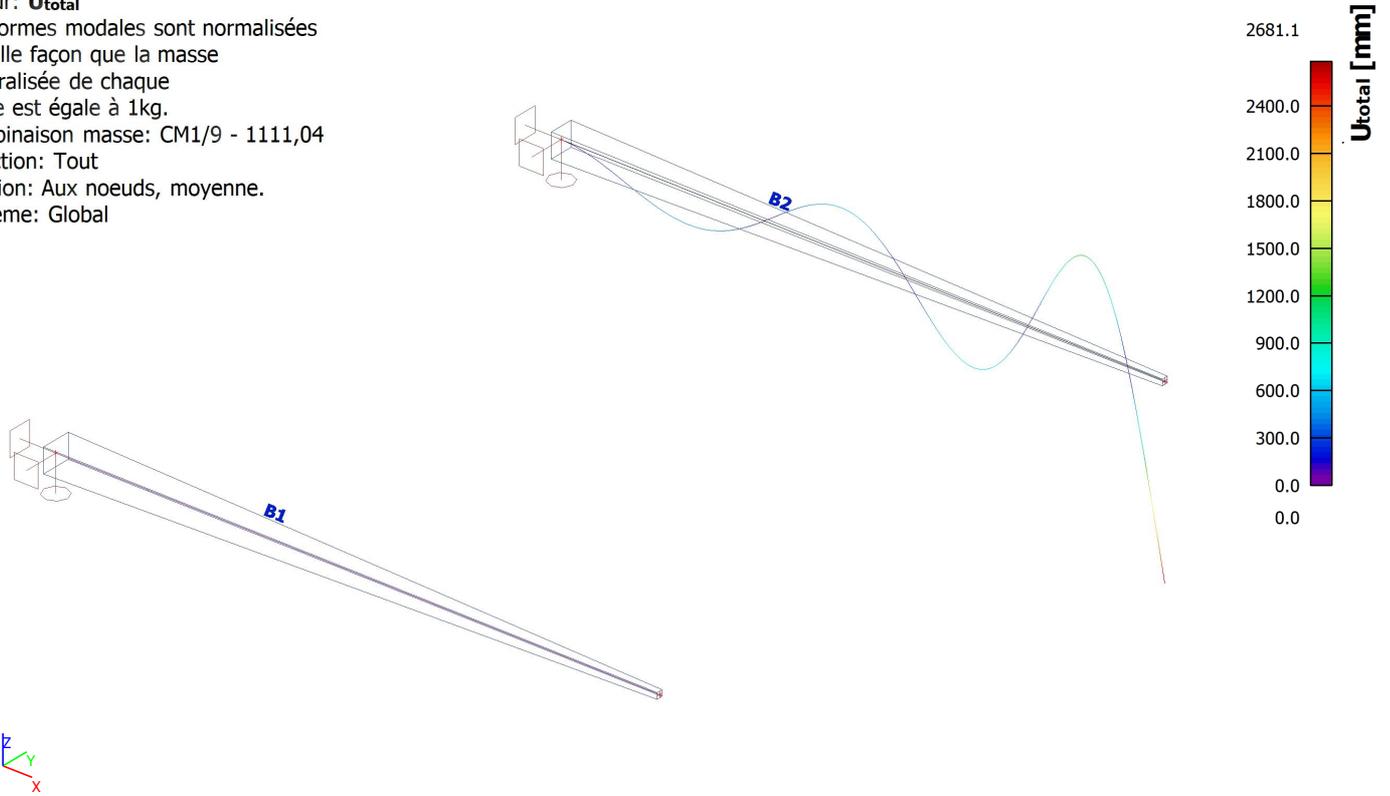
Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.

Combinaison masse: CM1/9 - 1111,04

Sélection: Tout

Position: Aux noeuds, moyenne.

Système: Global



4.7. 3D displacement; U_{total}

Valeur: U_{total}

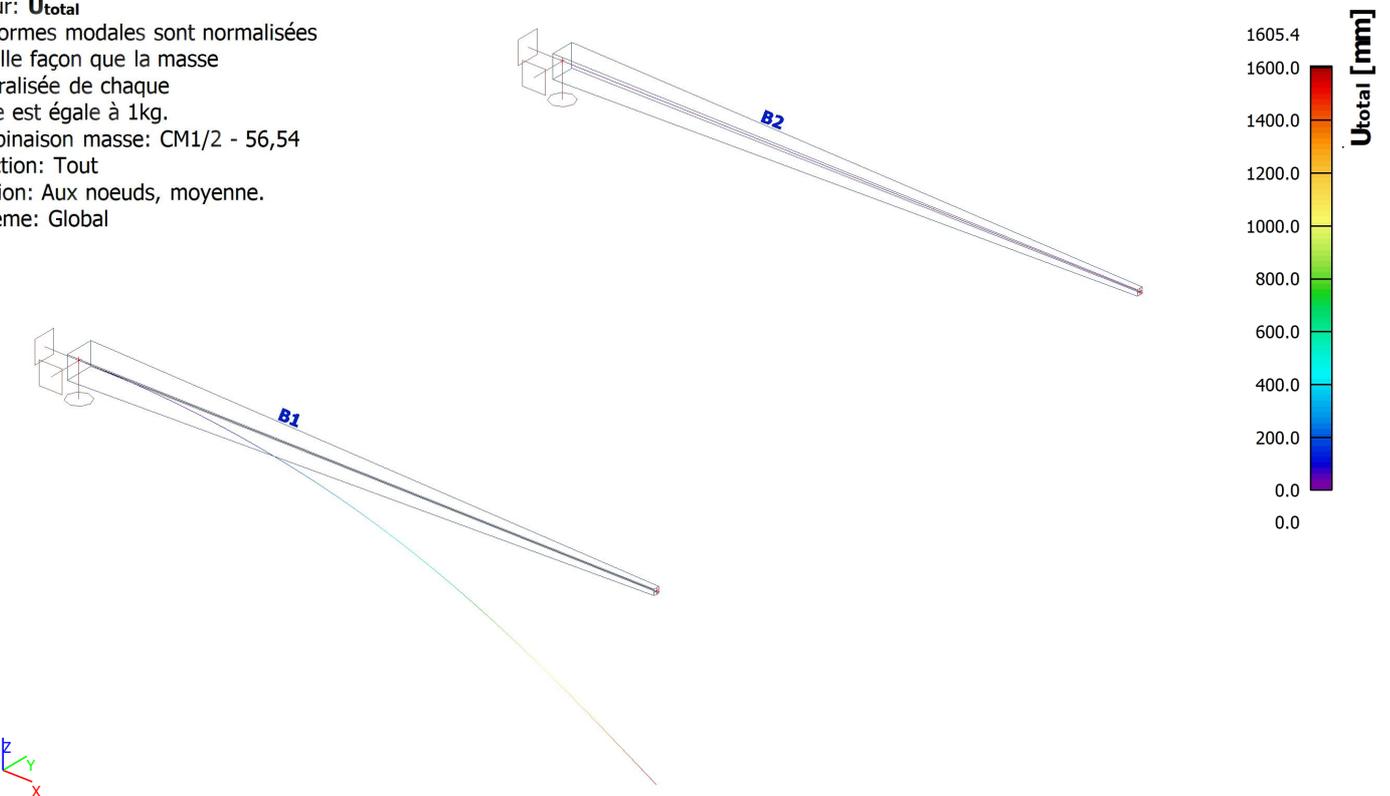
Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.

Combinaison masse: CM1/2 - 56,54

Sélection: Tout

Position: Aux noeuds, moyenne.

Système: Global



4.8. 3D displacement; U_{total}

Valeur: U_{total}

Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.

Combinaison masse: CM1/4 - 175,73

Sélection: Tout

Position: Aux noeuds, moyenne.

Système: Global



4.9. 3D displacement; U_{total}

Valeur: U_{total}

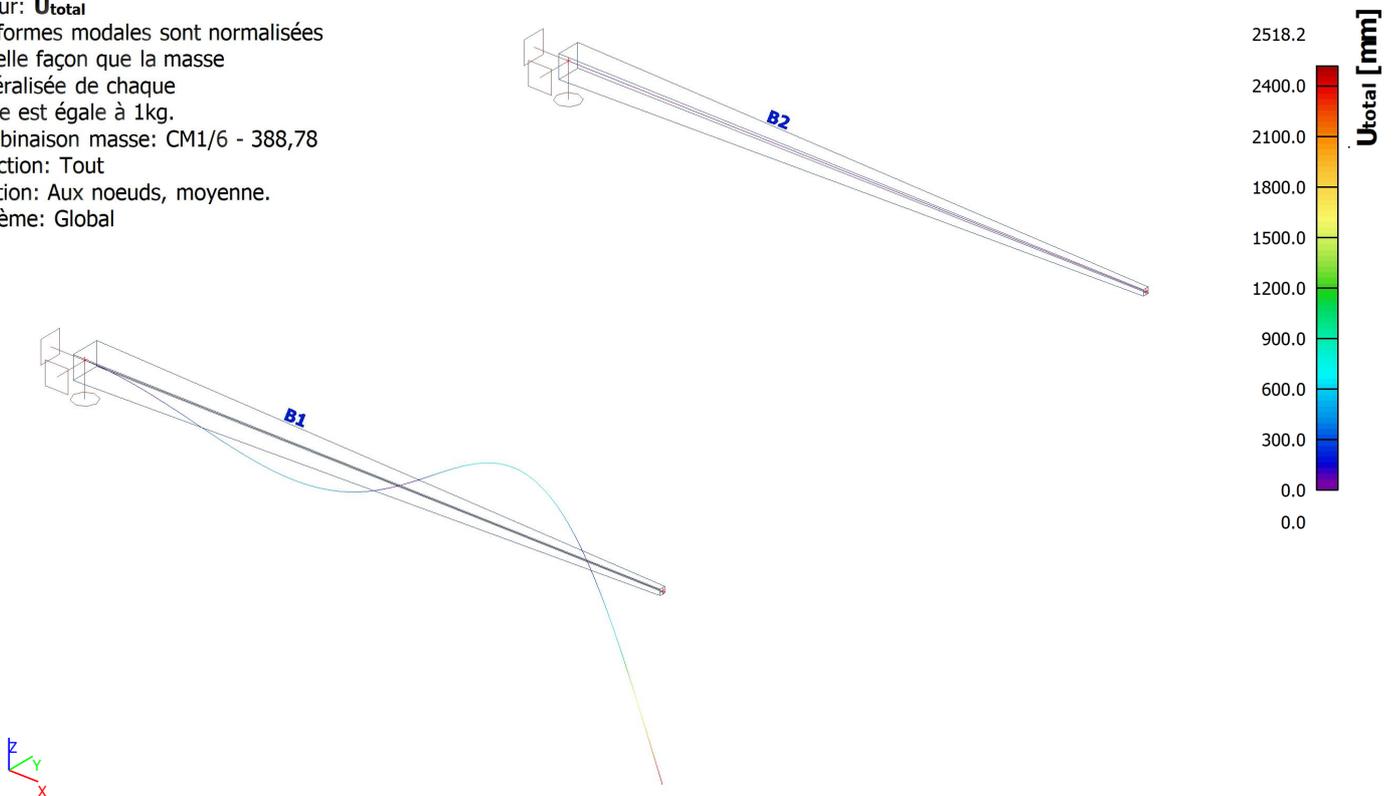
Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.

Combinaison masse: CM1/6 - 388,78

Sélection: Tout

Position: Aux noeuds, moyenne.

Système: Global



4.10. 3D displacement; U_{total}

Valeur: U_{total}

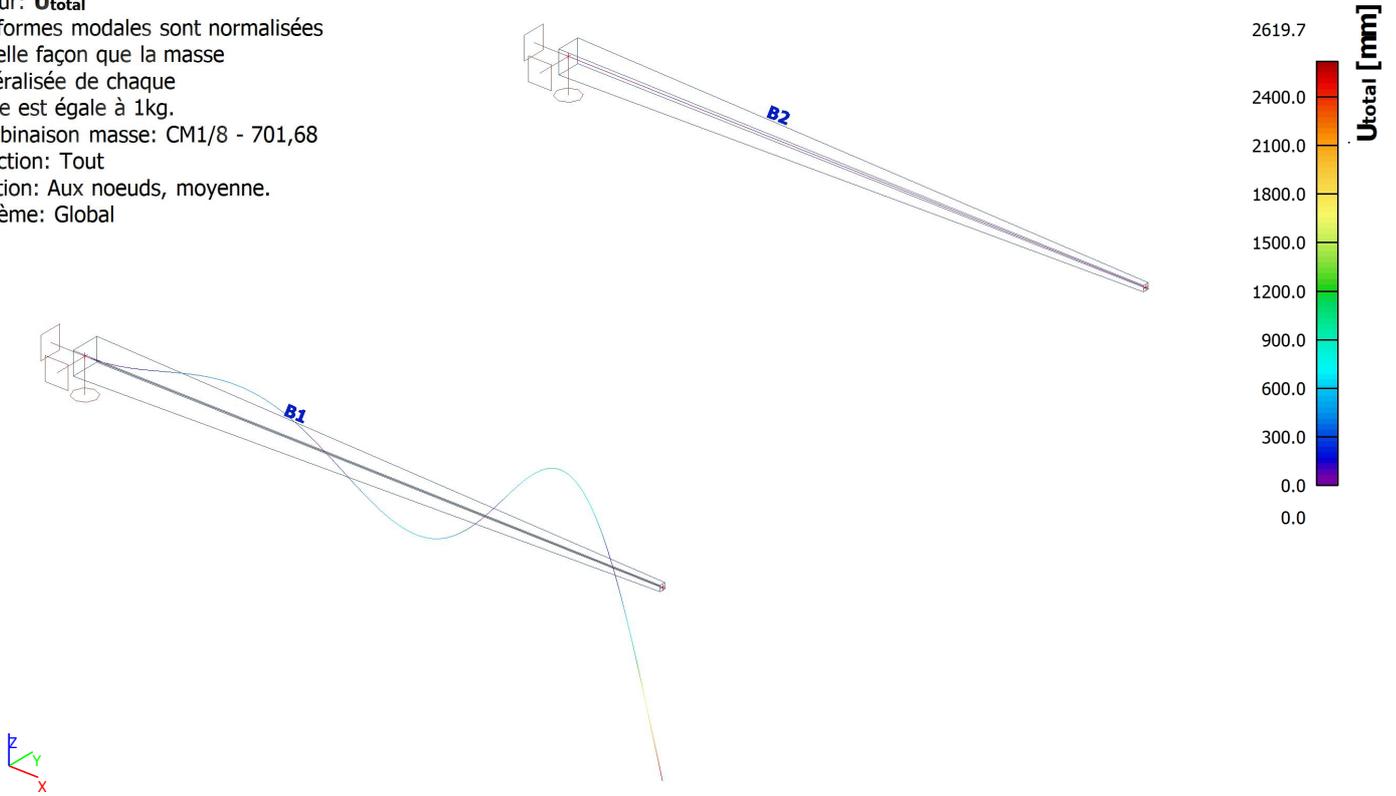
Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.

Combinaison masse: CM1/8 - 701,68

Sélection: Tout

Position: Aux noeuds, moyenne.

Système: Global



4.11. 3D displacement; U_{total}

Valeur: U_{total}

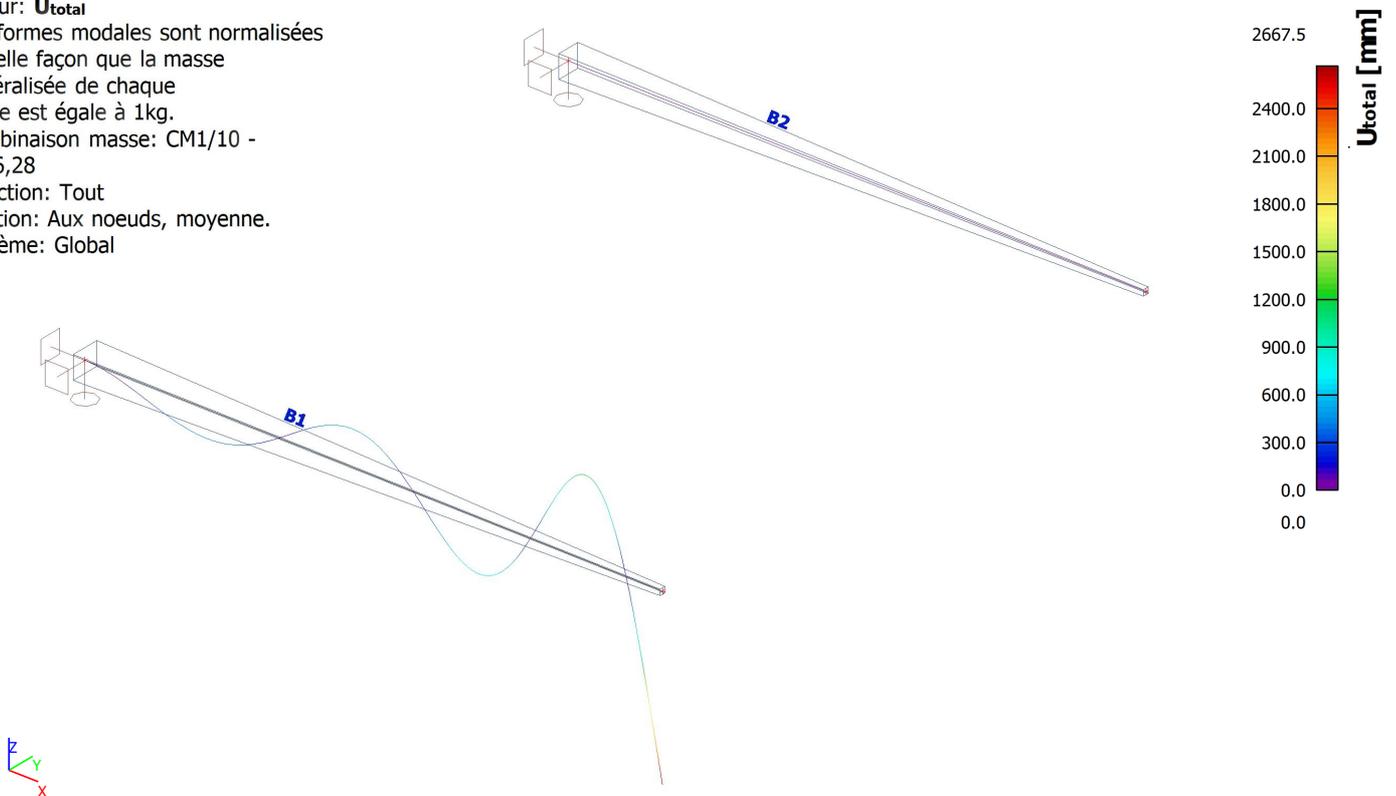
Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.

Combinaison masse: CM1/10 - 1116,28

Sélection: Tout

Position: Aux noeuds, moyenne.

Système: Global



5. EXPECTED AFNOR RESULTS

Beam B1:

f1 = 56.55 Hz

f2 = 175.79 Hz

f3 = 389.01 Hz

f4 = 702.36 Hz

f5 = 1117.63 Hz

Beam B2:

f1 = 54.18 Hz

f2 = 171.94 Hz

f3 = 384.40 Hz

f4 = 697.24 Hz

f5 = 1112.28 Hz

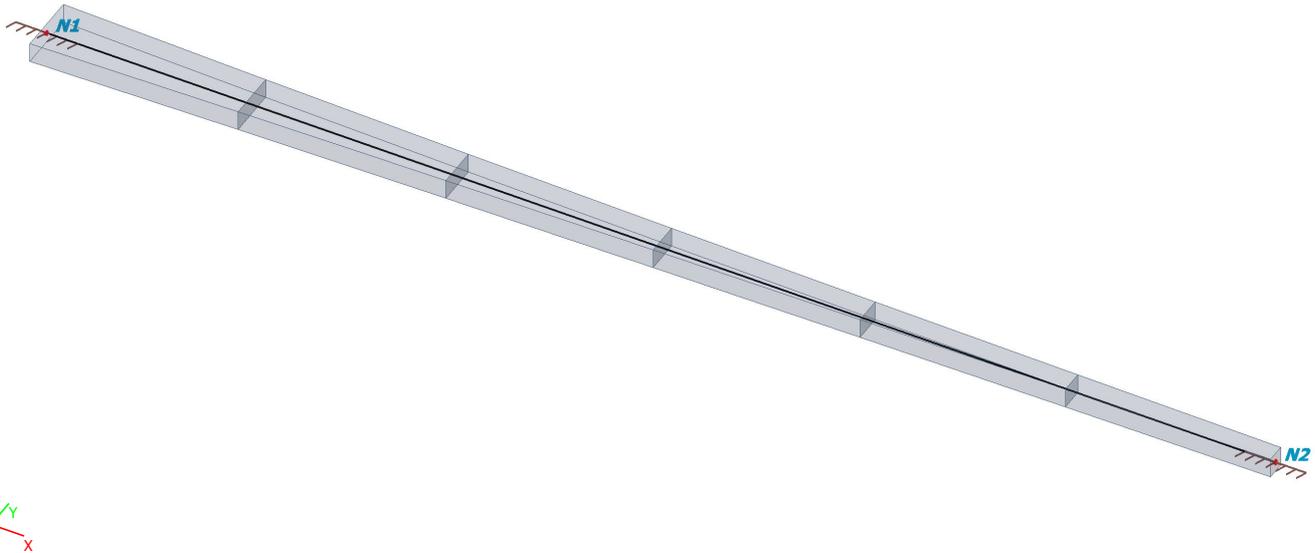
REFERENCE : "Guide de validation des progiciels de calcul de structures" AFNOR, 1990

1. TESTCASE DESCRIPTION

Modal analysis of a fixed beam with variable cross-section.

2. MODEL

2.1. Analysis model



2.2. Nodes

| Name | Coord X [m] | Coord Z [m] | Member | Data |
|------|-------------|-------------|--------|------|
| N1 | 0,000 | 0,000 | B1 | Sn1 |
| N2 | 0,600 | 0,000 | B1 | Sn2 |

2.3. Members

2.3.1. Members - B1

| Name | Cross-section | Material | Length [m] | Beg. node | End node | Type |
|------|--------------------------|----------|------------|-----------|----------|-----------|
| B1 | CS2 - Rectangle (10; 25) | Material | 0,600 | N1 | N2 | beam (80) |

2.3.1.1. Arbitrary members

| AP | | | |
|--|-------|--------------------------|--------------------------|
| Member | B1 | | |
| Coor | Rela | | |
| length 1, C _{ss} 1(1), C _{ss} 2(1) | 0.167 | CS1 - Rectangle (10; 30) | CS2 - Rectangle (10; 25) |
| length 2, C _{ss} 1(2), C _{ss} 2(2) | 0.167 | CS2 - Rectangle (10; 25) | CS3 - Rectangle (10; 20) |
| length 3, C _{ss} 1(3), C _{ss} 2(3) | 0.167 | CS3 - Rectangle (10; 20) | CS4 - Rectangle (10; 16) |
| length 4, C _{ss} 1(4), C _{ss} 2(4) | 0.167 | CS4 - Rectangle (10; 16) | CS5 - Rectangle (10; 13) |
| length 5, C _{ss} 1(5), C _{ss} 2(5) | 0.166 | CS5 - Rectangle (10; 13) | CS6 - Rectangle (10; 11) |
| length 6, C _{ss} 1(6), C _{ss} 2(6) | 0.166 | CS6 - Rectangle (10; 11) | CS7 - Rectangle (10; 9) |

2.4. Nodal supports

| Name | Node | System | Type | X | Z | Ry |
|------|------|--------|----------|-------|-------|-------|
| Sn1 | N1 | GCS | Standard | Rigid | Rigid | Rigid |
| Sn2 | N2 | GCS | Standard | Rigid | Rigid | Rigid |

2.5. Materials

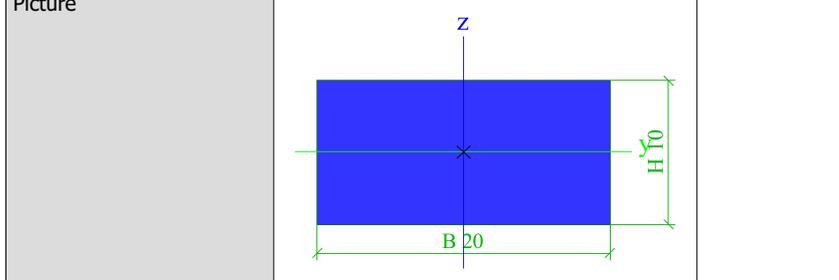
Steel EC3

| Name | ρ [kg/m ³] | E_{mod} [MPa] | μ | Limit inférieure [mm] | Limite supérieure [mm] | F_y [MPa] | F_u [MPa] | Colour |
|----------|--------------------------------|--------------------|--------------------|--------------------------|---------------------------|----------------|----------------|--------|
| | | G_{mod} [MPa] | α [m/mK] | | | | | |
| Material | 7800,00 | 2,0000e+05 | 0.3 | 0 | 40 | 235,0 | 360,0 | ■ |
| | | 7,6923e+04 | 0,01e-003 | 40 | 80 | 215,0 | 360,0 | |

2.6. Cross-sections

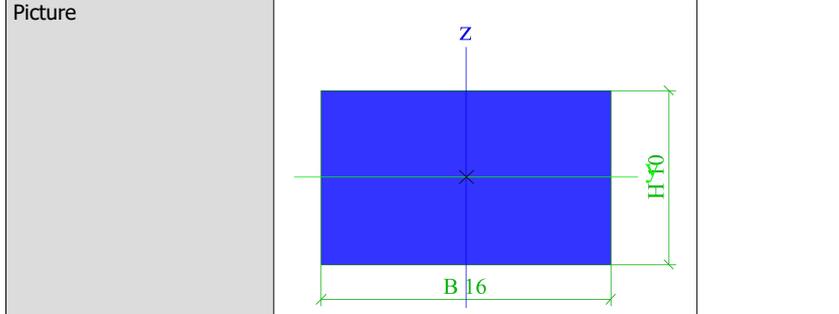
| CS1 | | | |
|--|------------|------------|--|
| Type | Rectangle | | |
| Detailed | 10; 30 | | |
| Item material | Material | | |
| A [m ²] | 3,0000e-04 | | |
| A _y [m ²], A _z [m ²] | 2,5000e-04 | 2,5000e-04 | |
| A _L [m ² /m], A _D [m ² /m] | 8,0000e-02 | 8,0000e-02 | |
| c _{y,UCS} [mm], c _{z,UCS} [mm] | 15 | 5 | |
| α [deg] | 0,00 | | |
| I _y [m ⁴], I _z [m ⁴] | 2,5000e-09 | 2,2500e-08 | |
| i _y [mm], i _z [mm] | 3 | 9 | |
| W _{el,y} [m ³], W _{el,z} [m ³] | 5,0000e-07 | 1,5000e-06 | |
| W _{pl,y} [m ³], W _{pl,z} [m ³] | 7,5000e-07 | 2,2500e-06 | |
| M _{pl,y,+} [Nm], M _{pl,y,-} [Nm] | 176,25 | 176,25 | |
| M _{pl,z,+} [Nm], M _{pl,z,-} [Nm] | 528,75 | 528,75 | |
| d _y [mm], d _z [mm] | 0 | 0 | |
| I _E [m ⁴], I _w [m ⁶] | 7,9003e-09 | 0,0000e+00 | |
| β _y [mm], β _z [mm] | 0 | 0 | |
| Picture | | | |
| CS2 | | | |
| Type | Rectangle | | |
| Detailed | 10; 25 | | |
| Item material | Material | | |
| A [m ²] | 2,4562e-04 | | |
| A _y [m ²], A _z [m ²] | 2,0468e-04 | 2,0468e-04 | |
| A _L [m ² /m], A _D [m ² /m] | 6,9124e-02 | 6,9124e-02 | |
| c _{y,UCS} [mm], c _{z,UCS} [mm] | 12 | 5 | |
| α [deg] | 0,00 | | |
| I _y [m ⁴], I _z [m ⁴] | 2,0468e-09 | 1,2348e-08 | |
| i _y [mm], i _z [mm] | 3 | 7 | |
| W _{el,y} [m ³], W _{el,z} [m ³] | 4,0937e-07 | 1,0055e-06 | |
| W _{pl,y} [m ³], W _{pl,z} [m ³] | 6,1405e-07 | 1,5082e-06 | |
| M _{pl,y,+} [Nm], M _{pl,y,-} [Nm] | 144,30 | 144,30 | |
| M _{pl,z,+} [Nm], M _{pl,z,-} [Nm] | 354,43 | 354,43 | |
| d _y [mm], d _z [mm] | 0 | 0 | |
| I _E [m ⁴], I _w [m ⁶] | 6,0892e-09 | 0,0000e+00 | |
| β _y [mm], β _z [mm] | 0 | 0 | |
| Picture | | | |
| CS3 | | | |
| Type | Rectangle | | |
| Detailed | 10; 20 | | |
| Item material | Material | | |
| A [m ²] | 2,0110e-04 | | |
| A _y [m ²], A _z [m ²] | 1,6758e-04 | 1,6758e-04 | |
| A _L [m ² /m], A _D [m ² /m] | 6,0219e-02 | 6,0219e-02 | |
| c _{y,UCS} [mm], c _{z,UCS} [mm] | 10 | 5 | |
| α [deg] | 0,00 | | |
| I _y [m ⁴], I _z [m ⁴] | 1,6758e-09 | 6,7769e-09 | |
| i _y [mm], i _z [mm] | 3 | 6 | |

| | | |
|--|------------|------------|
| $W_{el,y}$ [m ³], $W_{el,z}$ [m ³] | 3,3516e-07 | 6,7399e-07 |
| $W_{pl,y}$ [m ³], $W_{pl,z}$ [m ³] | 5,0274e-07 | 1,0110e-06 |
| $M_{pl,y,+}$ [Nm], $M_{pl,y,-}$ [Nm] | 118,14 | 118,14 |
| $M_{pl,z,+}$ [Nm], $M_{pl,z,-}$ [Nm] | 237,58 | 237,58 |
| d_y [mm], d_z [mm] | 0 | 0 |
| I_t [m ⁴], I_w [m ⁶] | 4,6108e-09 | 0,0000e+00 |
| β_y [mm], β_z [mm] | 0 | 0 |



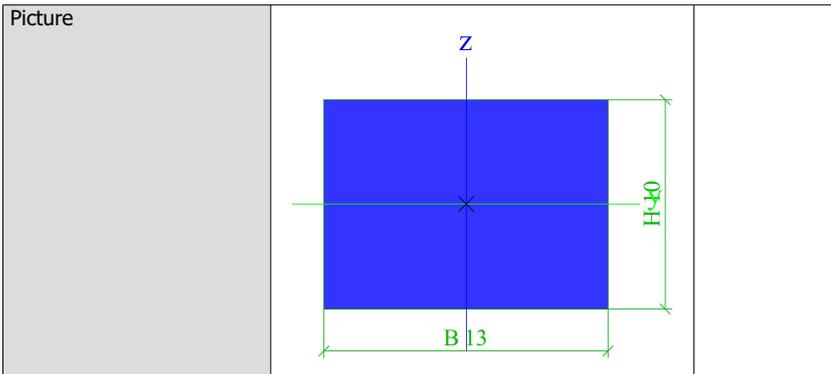
CS4

| | | |
|--|------------|------------|
| Type | Rectangle | |
| Detailed | 10; 16 | |
| Item material | Material | |
| A [m ²] | 1,6464e-04 | |
| A_y [m ²], A_z [m ²] | 1,3720e-04 | 1,3720e-04 |
| A_L [m ² /m], A_D [m ² /m] | 5,2929e-02 | 5,2929e-02 |
| $c_{y,UCS}$ [mm], $c_{z,UCS}$ [mm] | 8 | 5 |
| α [deg] | 0,00 | |
| I_y [m ⁴], I_z [m ⁴] | 1,3720e-09 | 3,7192e-09 |
| i_y [mm], i_z [mm] | 3 | 5 |
| $W_{el,y}$ [m ³], $W_{el,z}$ [m ³] | 2,7441e-07 | 4,5179e-07 |
| $W_{pl,y}$ [m ³], $W_{pl,z}$ [m ³] | 4,1161e-07 | 6,7768e-07 |
| $M_{pl,y,+}$ [Nm], $M_{pl,y,-}$ [Nm] | 96,73 | 96,73 |
| $M_{pl,z,+}$ [Nm], $M_{pl,z,-}$ [Nm] | 159,26 | 159,26 |
| d_y [mm], d_z [mm] | 0 | 0 |
| I_t [m ⁴], I_w [m ⁶] | 3,4118e-09 | 0,0000e+00 |
| β_y [mm], β_z [mm] | 0 | 0 |



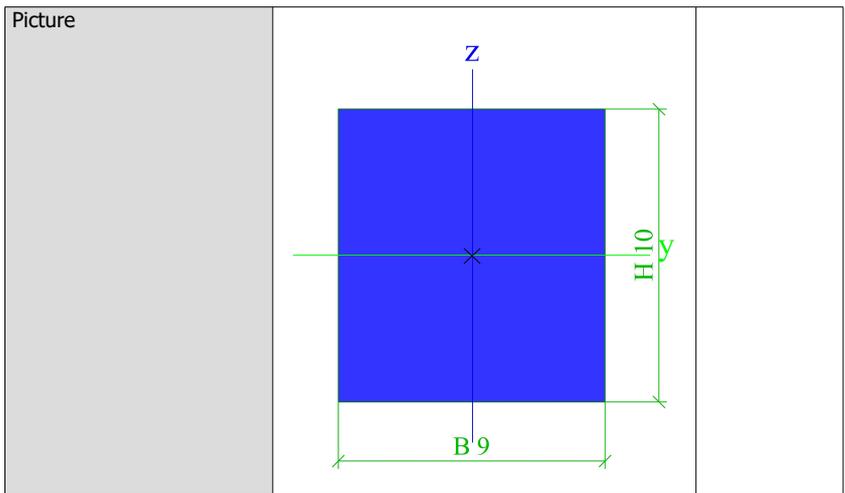
CS5

| | | |
|--|------------|------------|
| Type | Rectangle | |
| Detailed | 10; 13 | |
| Item material | Material | |
| A [m ²] | 1,3480e-04 | |
| A_y [m ²], A_z [m ²] | 1,1233e-04 | 1,1233e-04 |
| A_L [m ² /m], A_D [m ² /m] | 4,6960e-02 | 4,6960e-02 |
| $c_{y,UCS}$ [mm], $c_{z,UCS}$ [mm] | 7 | 5 |
| α [deg] | 0,00 | |
| I_y [m ⁴], I_z [m ⁴] | 1,1233e-09 | 2,0412e-09 |
| i_y [mm], i_z [mm] | 3 | 4 |
| $W_{el,y}$ [m ³], $W_{el,z}$ [m ³] | 2,2467e-07 | 3,0285e-07 |
| $W_{pl,y}$ [m ³], $W_{pl,z}$ [m ³] | 3,3700e-07 | 4,5427e-07 |
| $M_{pl,y,+}$ [Nm], $M_{pl,y,-}$ [Nm] | 79,19 | 79,19 |
| $M_{pl,z,+}$ [Nm], $M_{pl,z,-}$ [Nm] | 106,75 | 106,75 |
| d_y [mm], d_z [mm] | 0 | 0 |
| I_t [m ⁴], I_w [m ⁶] | 2,4533e-09 | 0,0000e+00 |
| β_y [mm], β_z [mm] | 0 | 0 |



| CS6 | | |
|--|------------|------------|
| Type | Rectangle | |
| Detailed | 10; 11 | |
| Item material | Material | |
| A [m ²] | 1,1036e-04 | |
| A _y [m ²], A _z [m ²] | 9,1970e-05 | 9,1970e-05 |
| A _L [m ² /m], A _D [m ² /m] | 4,2073e-02 | 4,2073e-02 |
| c _{y,ucs} [mm], c _{z,ucs} [mm] | 6 | 5 |
| α [deg] | 0,00 | |
| I _y [m ⁴], I _z [m ⁴] | 9,1970e-10 | 1,1202e-09 |
| i _y [mm], i _z [mm] | 3 | 3 |
| W _{el,y} [m ³], W _{el,z} [m ³] | 1,8394e-07 | 2,0300e-07 |
| W _{pl,y} [m ³], W _{pl,z} [m ³] | 2,7591e-07 | 3,0451e-07 |
| M _{pl,y,+} [Nm], M _{pl,y,-} [Nm] | 64,84 | 64,84 |
| M _{pl,z,+} [Nm], M _{pl,z,-} [Nm] | 71,56 | 71,56 |
| d _y [mm], d _z [mm] | 0 | 0 |
| I _t [m ⁴], I _w [m ⁶] | 1,7059e-09 | 0,0000e+00 |
| β _y [mm], β _z [mm] | 0 | 0 |
| Picture | | |

| CS7 | | |
|--|------------|------------|
| Type | Rectangle | |
| Detailed | 10; 9 | |
| Item material | Material | |
| A [m ²] | 9,0358e-05 | |
| A _y [m ²], A _z [m ²] | 7,5298e-05 | 7,5298e-05 |
| A _L [m ² /m], A _D [m ² /m] | 3,8072e-02 | 3,8072e-02 |
| c _{y,ucs} [mm], c _{z,ucs} [mm] | 5 | 5 |
| α [deg] | 0,00 | |
| I _y [m ⁴], I _z [m ⁴] | 7,5298e-10 | 6,1478e-10 |
| i _y [mm], i _z [mm] | 3 | 3 |
| W _{el,y} [m ³], W _{el,z} [m ³] | 1,5060e-07 | 1,3608e-07 |
| W _{pl,y} [m ³], W _{pl,z} [m ³] | 2,2589e-07 | 2,0411e-07 |
| M _{pl,y,+} [Nm], M _{pl,y,-} [Nm] | 53,09 | 53,09 |
| M _{pl,z,+} [Nm], M _{pl,z,-} [Nm] | 47,97 | 47,97 |
| d _y [mm], d _z [mm] | 0 | 0 |
| I _t [m ⁴], I _w [m ⁶] | 1,1432e-09 | 0,0000e+00 |
| β _y [mm], β _z [mm] | 0 | 0 |



3. LOAD and MASS

3.1. Mass groups

| Name | Load case |
|------|-------------------|
| MG1 | LC1 - Self weight |

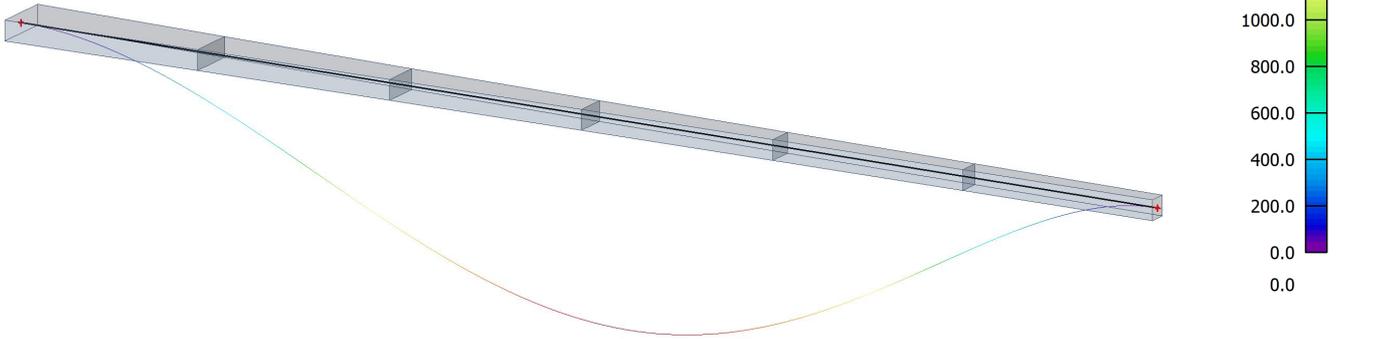
4. RESULTS

4.1. Eigen frequencies

| N | f [Hz] | ω [1/s] | ω^2 [1/s ²] | T [s] |
|-------------------------------|-----------|-------------------|-----------------------------------|----------|
| Mass combination : CM1 | | | | |
| 1 | 145,57 | 914,61 | 836511,57 | 0,01 |
| 2 | 398,64 | 2504,64 | 6273211,68 | 0,00 |
| 3 | 777,84 | 4887,18 | 23884511,22 | 0,00 |
| 4 | 1280,20 | 8043,48 | 64697574,50 | 0,00 |

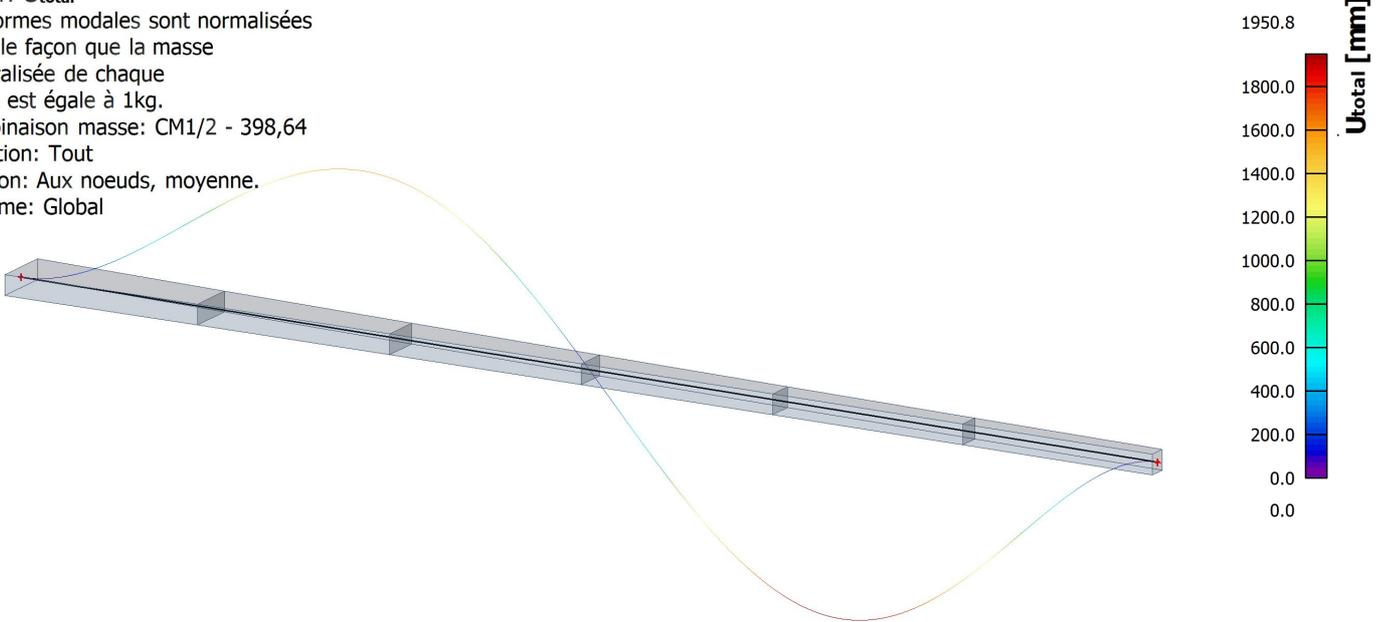
4.2. 3D displacement; U_{total}

Valeur: U_{total}
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/1 - 145,57
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



4.3. 3D displacement; U_{total}

Valeur: U_{total}
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/2 - 398,64
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



4.4. 3D displacement; U_{total}

Valeur: **U_{total}**

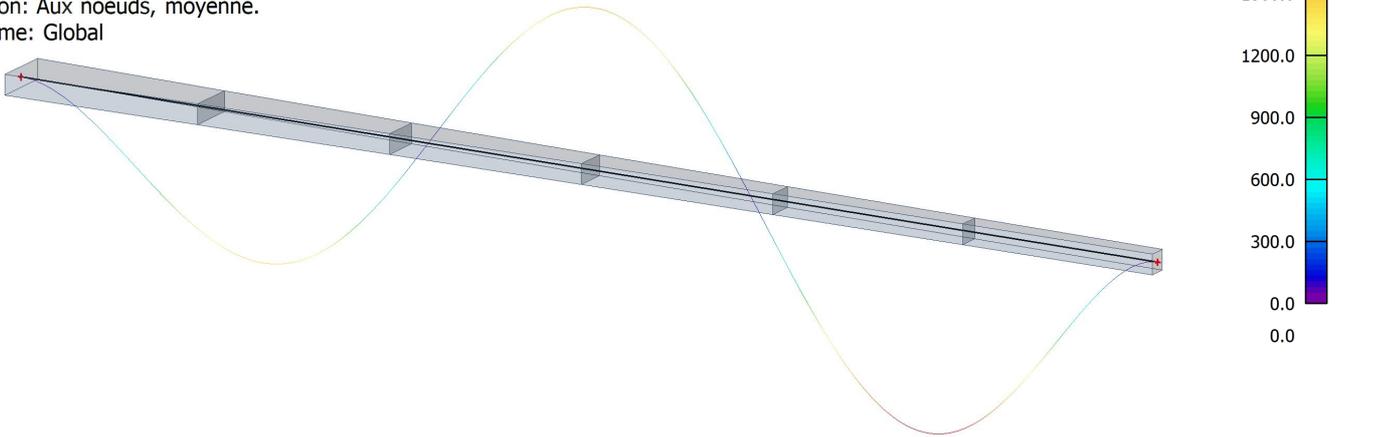
Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.

Combinaison masse: CM1/3 - 777,84

Sélection: Tout

Position: Aux noeuds, moyenne.

Système: Global



4.5. 3D displacement; U_{total}

Valeur: **U_{total}**

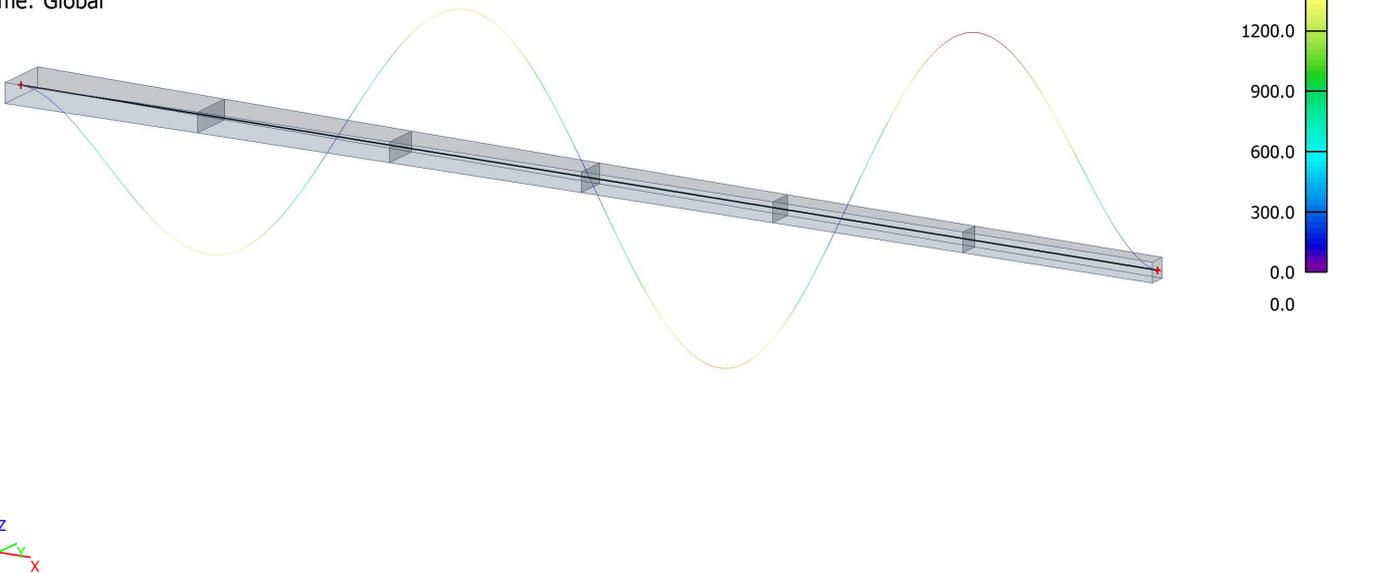
Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.

Combinaison masse: CM1/4 - 1280,20

Sélection: Tout

Position: Aux noeuds, moyenne.

Système: Global



5. EXPECTED AFNOR RESULTS

Eigenfrequencies:

f1 = 143.3 Hz

f2 = 396.8 Hz

f3= 779.4 Hz

f4 = 1289.6 Hz

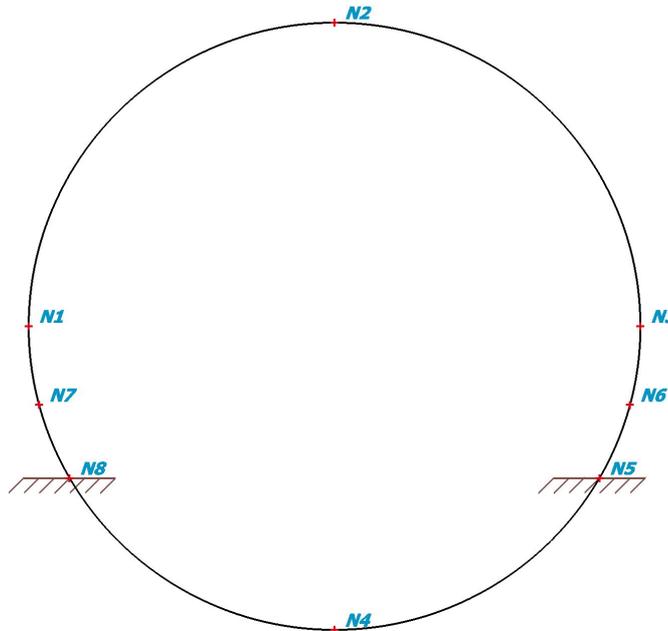
REFERENCE : "Guide de validation des progiciels de calcul de structures" AFNOR, 1990

1. TESTCASE DESCRIPTION

Modal analysis of a circular ring fixed in two points

2. MODEL

2.1. Analysis model



2.2. Nodes

| Name | Coord X [m] | Coord Z [m] | Member | Data |
|------|-------------|-------------|--------|------|
| N1 | 0,000 | 0,000 | B1 | |
| N2 | 0,100 | 0,100 | B1 | |
| N3 | 0,200 | 0,000 | B1 | |
| N4 | 0,100 | -0,100 | B4 | |

| Name | Coord X [m] | Coord Z [m] | Member | Data |
|------|-------------|-------------|----------|------|
| N5 | 0,187 | -0,050 | B1 B4 | Sn1 |
| N6 | 0,197 | -0,026 | B1 | |
| N7 | 0,003 | -0,026 | B1 | |
| N8 | 0,013 | -0,050 | B1 B4 | Sn2 |

2.3. Members

| Name | Cross-section | Material | Length [m] | Beg. node | End node | Type |
|------|-----------------------------|----------|------------|-----------|----------|-------------|
| B1 | CS2 - Rectangle (5,0; 10,0) | Material | 0,419 | N8 | N5 | general (0) |
| B4 | CS2 - Rectangle (5,0; 10,0) | Material | 0,209 | N8 | N5 | general (0) |

2.4. Nodal supports

| Name | Node | System | Type | X | Z | Ry |
|------|------|--------|----------|-------|-------|-------|
| Sn1 | N5 | GCS | Standard | Rigid | Rigid | Rigid |
| Sn2 | N8 | GCS | Standard | Rigid | Rigid | Rigid |

2.5. Materials

Steel EC3

| Name | ρ [kg/m ³] | E_{mod} [MPa] | μ | Limit inférieure [mm] | Limite supérieure [mm] | F_y [MPa] | F_u [MPa] | Colour |
|----------|--------------------------------|--------------------|--------------------|--------------------------|---------------------------|----------------|----------------|--------|
| | | G_{mod} [MPa] | α [m/mK] | | | | | |
| Material | 2700,00 | 7,2000e+04 | 0.3 | 0,0 | 40,0 | 235,0 | 360,0 | ■ |
| | | 2,7692e+04 | 0,01e-003 | 40,0 | 80,0 | 215,0 | 360,0 | |

2.6. Cross-sections

| CS2 | | |
|--|------------|------------|
| Type | Rectangle | |
| Detailed | 5,0; 10,0 | |
| Item material | Material | |
| A [m ²] | 5,0000e-05 | |
| A _y [m ²], A _z [m ²] | 4,1667e-05 | 4,1667e-05 |
| A _L [m ² /m], A _D [m ² /m] | 3,0000e-02 | 3,0000e-02 |
| c _{y,UCS} [mm], c _{z,UCS} [mm] | 5,0 | 2,5 |
| α [deg] | 0,00 | |
| I _y [m ⁴], I _z [m ⁴] | 1,0417e-10 | 4,1667e-10 |
| i _y [mm], i _z [mm] | 1,4 | 2,9 |
| W _{el,y} [m ³], W _{el,z} [m ³] | 4,1667e-08 | 8,3333e-08 |
| W _{pl,y} [m ³], W _{pl,z} [m ³] | 6,2500e-08 | 1,2500e-07 |
| M _{pl,y,+} [Nm], M _{pl,y,-} [Nm] | 14,69 | 14,69 |
| M _{pl,z,+} [Nm], M _{pl,z,-} [Nm] | 29,37 | 29,37 |
| d _y [mm], d _z [mm] | 0,0 | |
| I _t [m ⁴], I _w [m ⁶] | 2,8591e-10 | 0,0000e+00 |
| β_y [mm], β_z [mm] | 0,0 | |
| Picture | | |

3. LOAD and MASS

3.1. Mass groups

| Name | Load case |
|------|--------------------|
| MG1 | LC1 - Poids propre |

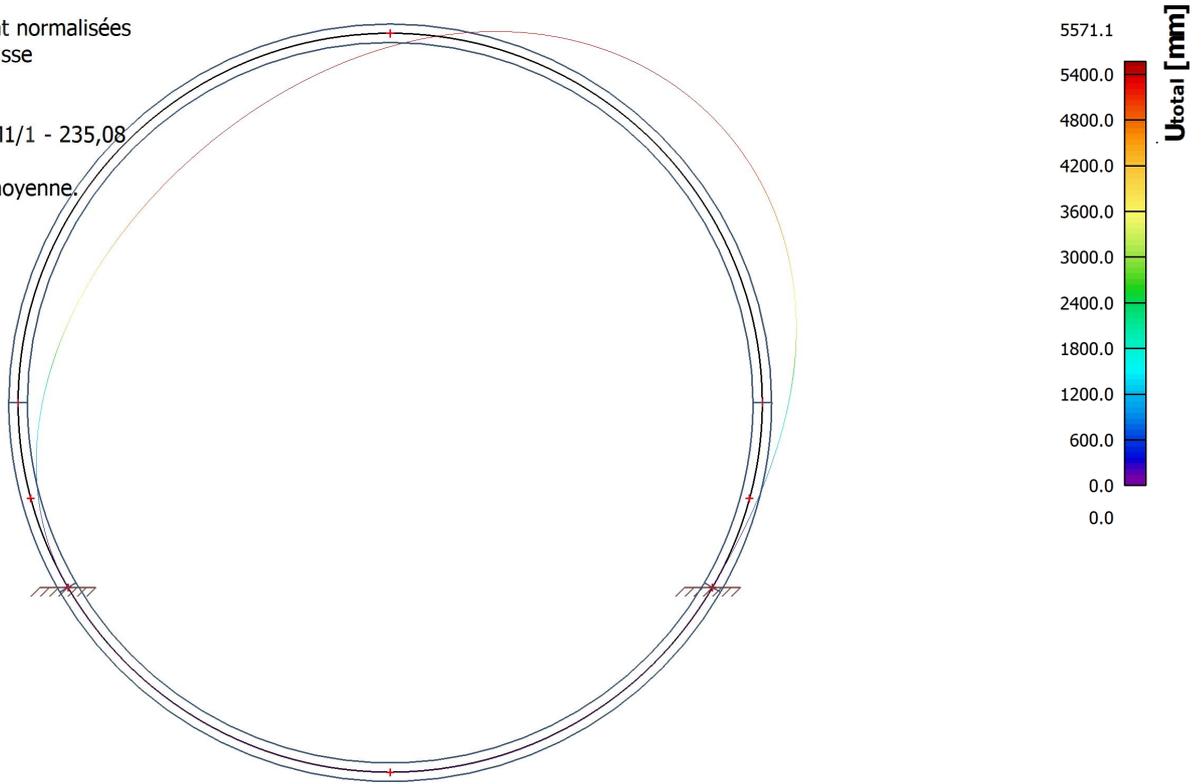
4. RESULTS

4.1. Eigen frequencies

| N | f [Hz] | ω [1/s] | ω^2 [1/s ²] | T [s] |
|-------------------------------|-----------|-------------------|-----------------------------------|----------|
| Mass combination : CM1 | | | | |
| 1 | 235,08 | 1476,98 | 2181477,29 | 0,00 |
| 2 | 574,44 | 3609,23 | 13026522,85 | 0,00 |
| 3 | 1103,78 | 6935,07 | 48095253,54 | 0,00 |
| 4 | 1403,35 | 8817,25 | 77743973,46 | 0,00 |
| 5 | 1745,56 | 10967,36 | 120283075,20 | 0,00 |
| 6 | 2548,65 | 16013,16 | 256421365,45 | 0,00 |
| 7 | 2750,68 | 17282,51 | 298685303,02 | 0,00 |

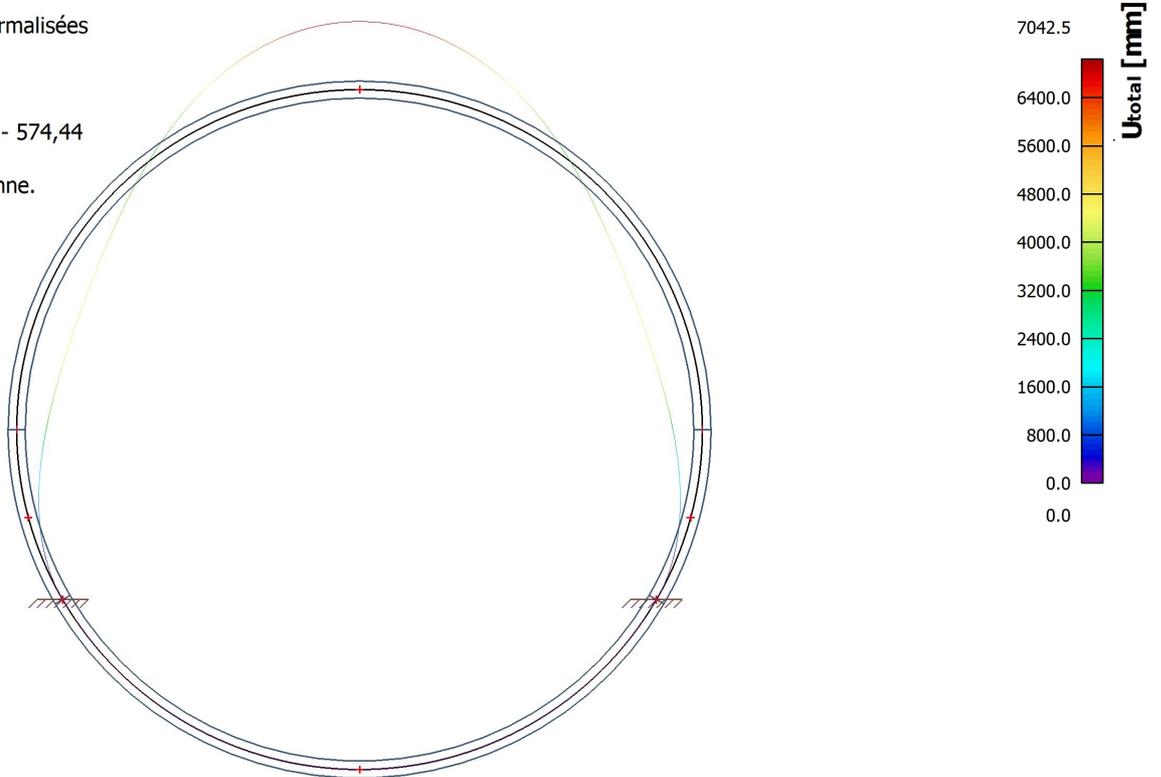
4.2. 3D displacement; U_{total}

Valeur: U_{total}
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/1 - 235,08
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



4.3. 3D displacement; U_{total}

Valeur: U_{total}
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/2 - 574,44
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



4.4. 3D displacement; U_{total}

Valeur: U_{total}

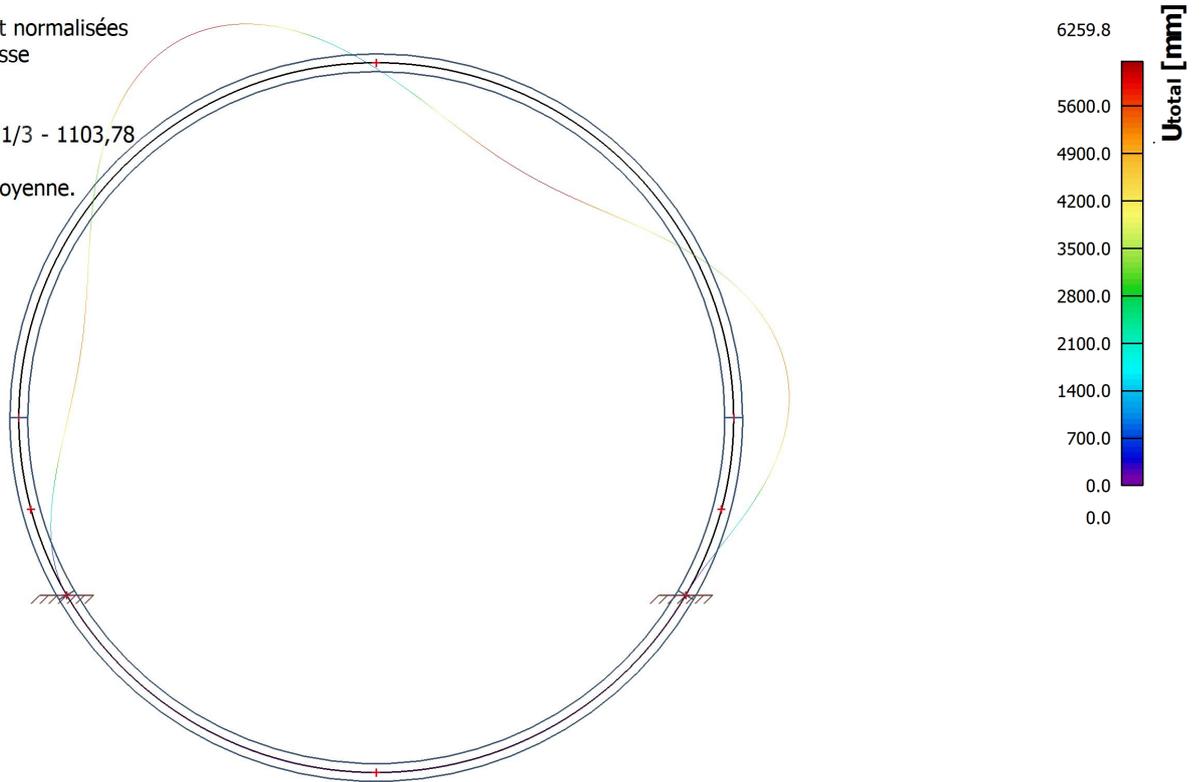
Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.

Combinaison masse: CM1/3 - 1103,78

Sélection: Tout

Position: Aux noeuds, moyenne.

Système: Global



4.5. 3D displacement; U_{total}

Valeur: U_{total}

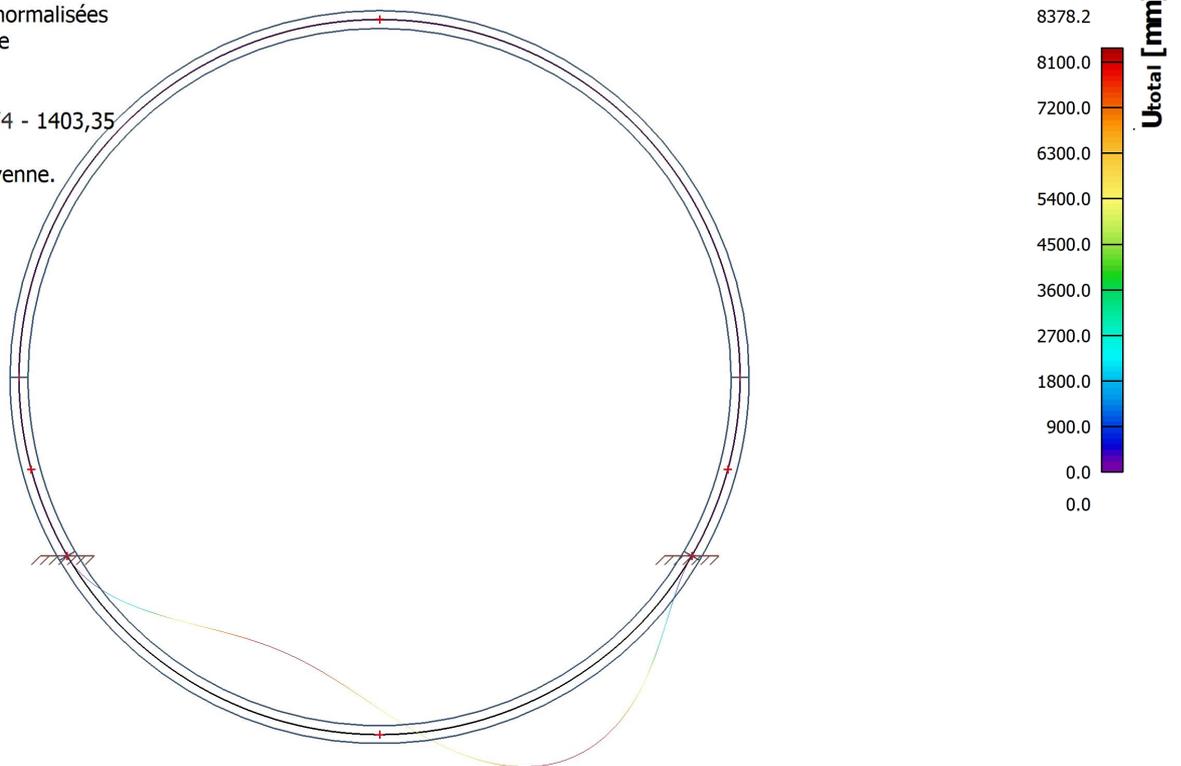
Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.

Combinaison masse: CM1/4 - 1403,35

Sélection: Tout

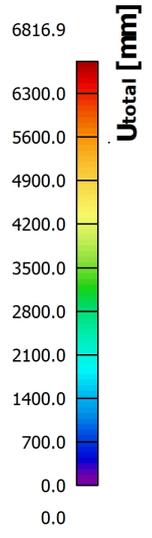
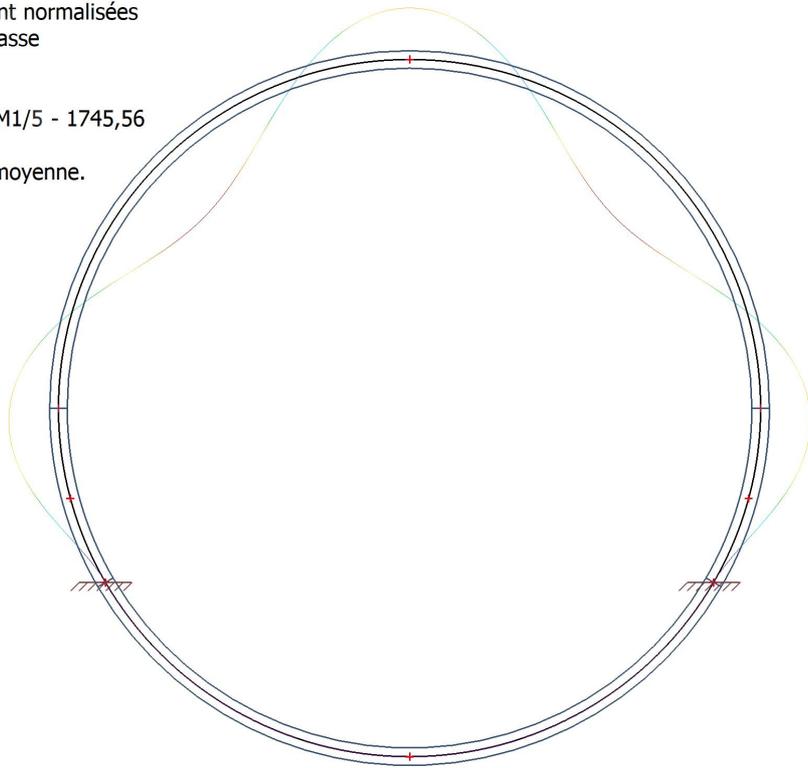
Position: Aux noeuds, moyenne.

Système: Global



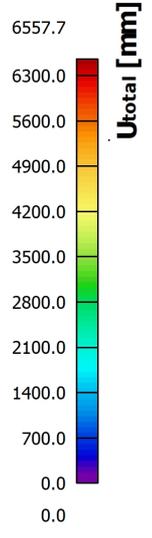
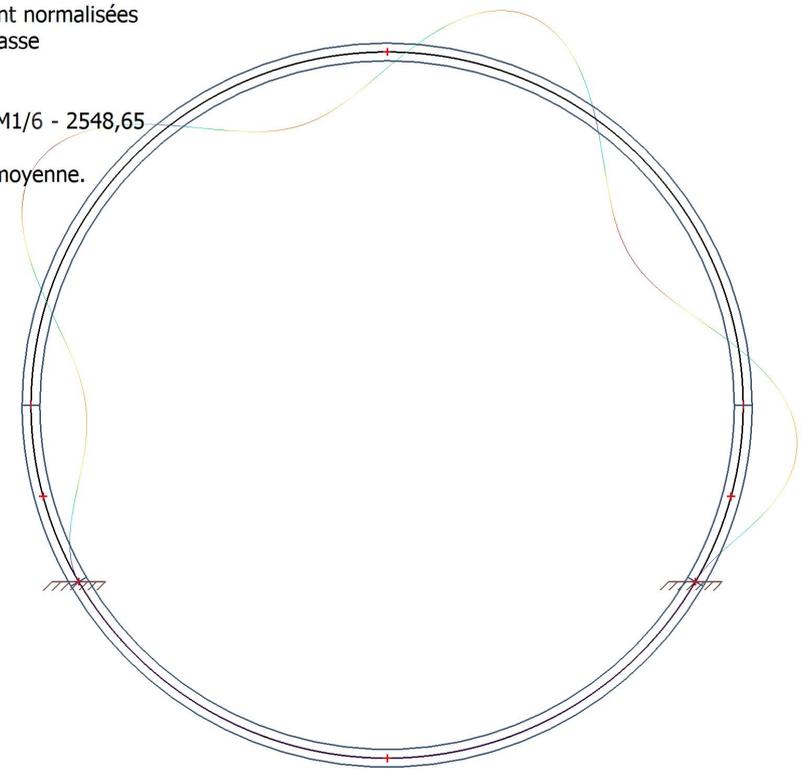
4.6. 3D displacement; U_{total}

Valeur: U_{total}
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/5 - 1745,56
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



4.7. 3D displacement; U_{total}

Valeur: U_{total}
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/6 - 2548,65
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



4.8. 3D displacement; U_total

Valeur: U_{total}

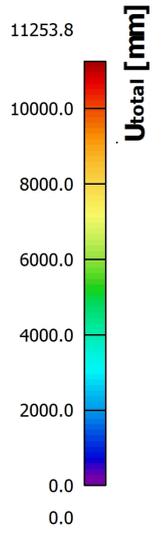
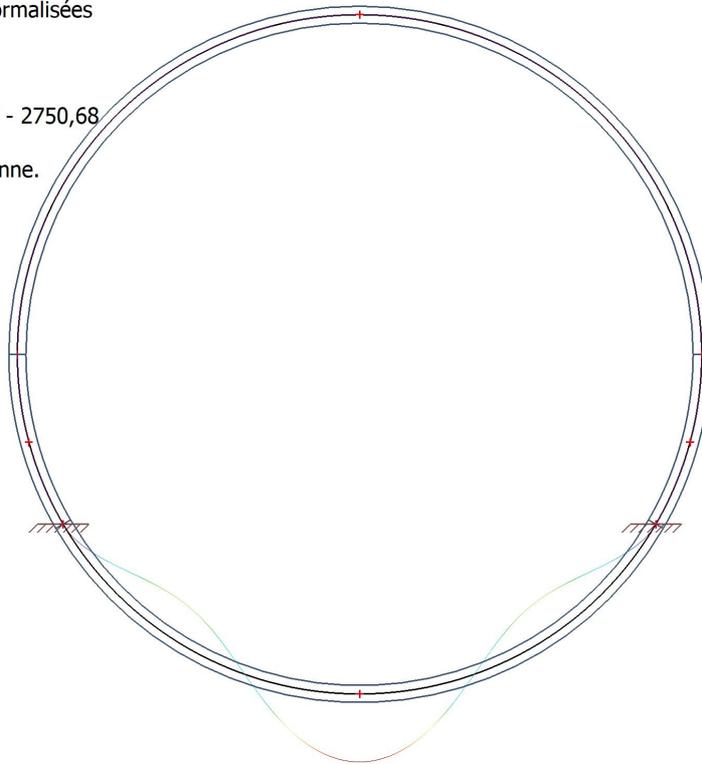
Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.

Combinaison masse: CM1/7 - 2750,68

Sélection: Tout

Position: Aux noeuds, moyenne.

Système: Global



5. EXPECTED AFNOR RESULTS

Eigenfrequencies:

f1 = 235.3 Hz

f2 = 575.3 Hz

f3 = 1105.7 Hz

f4 = 1405.6 Hz

f5 = 1751.1 Hz

f6 = 2557.0 Hz

f7 = 2801.5 Hz

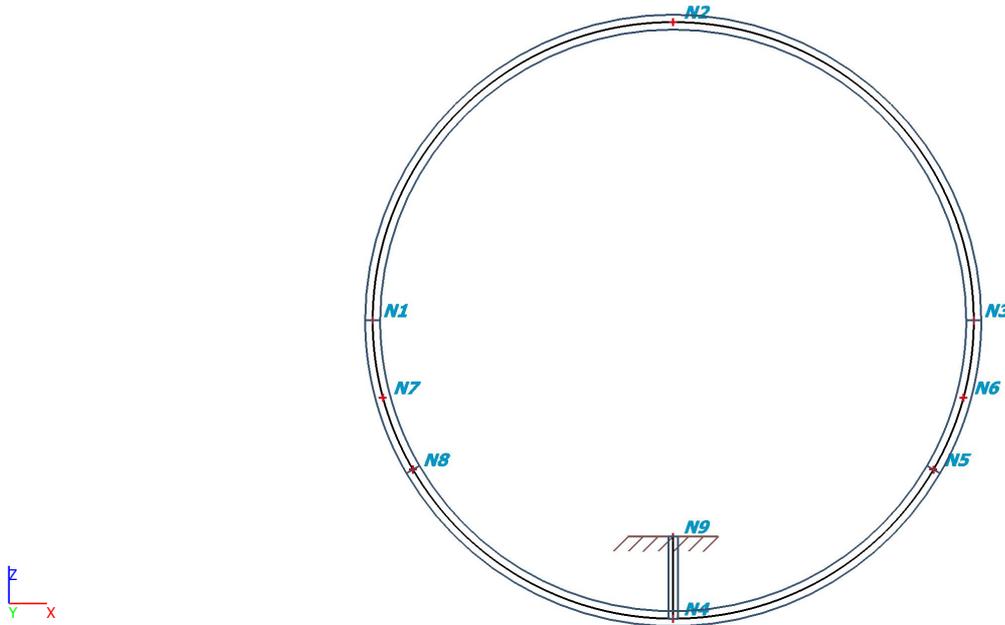
REFERENCE : "Guide de validation des progiciels de calcul de structures" AFNOR, 1990

1. TESTCASE DESCRIPTION

Modal analysis of a suspended circular ring

2. MODEL

2.1. Analysis model



2.2. Nodes

| Name | Coord X [m] | Coord Z [m] | Member | Data |
|------|-------------|-------------|--------|------|
| N1 | 0,000 | 0,000 | B1 | |
| N2 | 0,100 | 0,100 | B1 | |
| N3 | 0,200 | 0,000 | B1 | |
| N4 | 0,100 | -0,100 | B4 | |
| | | | B5 | |
| N5 | 0,187 | -0,050 | B1 | |
| | | | B4 | |

| Name | Coord X [m] | Coord Z [m] | Member | Data |
|------|-------------|-------------|--------|------|
| N6 | 0,197 | -0,026 | B1 | |
| N7 | 0,003 | -0,026 | B1 | |
| N8 | 0,013 | -0,050 | B1 | |
| | | | B4 | |
| N9 | 0,100 | -0,072 | B5 | Sn1 |

2.3. Members

| Name | Cross-section | Material | Length [m] | Beg. node | End node | Type |
|------|-----------------------------|----------|------------|-----------|----------|--------------|
| B1 | CS2 - Rectangle (5,0; 10,0) | Material | 0,419 | N8 | N5 | general (0) |
| B4 | CS2 - Rectangle (5,0; 10,0) | Material | 0,209 | N8 | N5 | general (0) |
| B5 | CS3 - Rectangle (3,0; 10,0) | Material | 0,028 | N4 | N9 | column (100) |

2.4. Nodal supports

| Name | Node | System | Type | X | Z | Ry |
|------|------|--------|----------|-------|-------|-------|
| Sn1 | N9 | GCS | Standard | Rigid | Rigid | Rigid |

2.5. Materials

Steel EC3

| Name | ρ [kg/m ³] | E_{mod} [MPa] | μ | Limit inférieure [mm] | Limite supérieure [mm] | F_y [MPa] | F_u [MPa] | Colour |
|----------|--------------------------------|--------------------|--------------------|--------------------------|---------------------------|----------------|----------------|--------|
| | | G_{mod} [MPa] | α [m/mK] | | | | | |
| Material | 2700,00 | 7,2000e+04 | 0.3 | 0,0 | 40,0 | 235,0 | 360,0 | ■ |
| | | 2,7692e+04 | 0,01e-003 | 40,0 | 80,0 | 215,0 | 360,0 | |

2.6. Cross-sections

| CS2 | | |
|--|------------|------------|
| Type | Rectangle | |
| Detailed | 5,0; 10,0 | |
| Item material | Material | |
| A [m ²] | 5,0000e-05 | |
| A _y [m ²], A _z [m ²] | 4,1667e-05 | 4,1667e-05 |
| A _L [m ² /m], A _D [m ² /m] | 3,0000e-02 | 3,0000e-02 |
| c _{y,UCS} [mm], c _{z,UCS} [mm] | 5,0 | 2,5 |
| α [deg] | 0,00 | |
| I _y [m ⁴], I _z [m ⁴] | 1,0417e-10 | 4,1667e-10 |
| i _y [mm], i _z [mm] | 1,4 | 2,9 |
| W _{el,y} [m ³], W _{el,z} [m ³] | 4,1667e-08 | 8,3333e-08 |
| W _{pl,y} [m ³], W _{pl,z} [m ³] | 6,2500e-08 | 1,2500e-07 |
| M _{pl,y,+} [Nm], M _{pl,y,-} [Nm] | 14,69 | 14,69 |
| M _{pl,z,+} [Nm], M _{pl,z,-} [Nm] | 29,37 | 29,37 |
| d _y [mm], d _z [mm] | 0,0 | 0,0 |
| I _t [m ⁴], I _w [m ⁶] | 2,8591e-10 | 0,0000e+00 |
| β _y [mm], β _z [mm] | 0,0 | 0,0 |
| Picture | | |
| CS3 | | |
| Type | Rectangle | |
| Detailed | 3,0; 10,0 | |
| Item material | Material | |
| A [m ²] | 3,0000e-05 | |
| A _y [m ²], A _z [m ²] | 2,5000e-05 | 2,5000e-05 |
| A _L [m ² /m], A _D [m ² /m] | 2,6000e-02 | 2,6000e-02 |
| c _{y,UCS} [mm], c _{z,UCS} [mm] | 5,0 | 1,5 |
| α [deg] | 0,00 | |
| I _y [m ⁴], I _z [m ⁴] | 2,2500e-11 | 2,5000e-10 |
| i _y [mm], i _z [mm] | 0,9 | 2,9 |
| W _{el,y} [m ³], W _{el,z} [m ³] | 1,5000e-08 | 5,0000e-08 |
| W _{pl,y} [m ³], W _{pl,z} [m ³] | 2,2500e-08 | 7,5000e-08 |
| M _{pl,y,+} [Nm], M _{pl,y,-} [Nm] | 5,29 | 5,29 |
| M _{pl,z,+} [Nm], M _{pl,z,-} [Nm] | 17,63 | 17,63 |
| d _y [mm], d _z [mm] | 0,0 | 0,0 |
| I _t [m ⁴], I _w [m ⁶] | 7,2991e-11 | 0,0000e+00 |
| β _y [mm], β _z [mm] | 0,0 | 0,0 |
| Picture | | |

3. LOAD and MASS

3.1. Mass groups

| Name | Load case |
|------|--------------------|
| MG1 | LC1 - Poids propre |

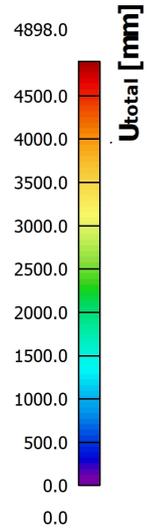
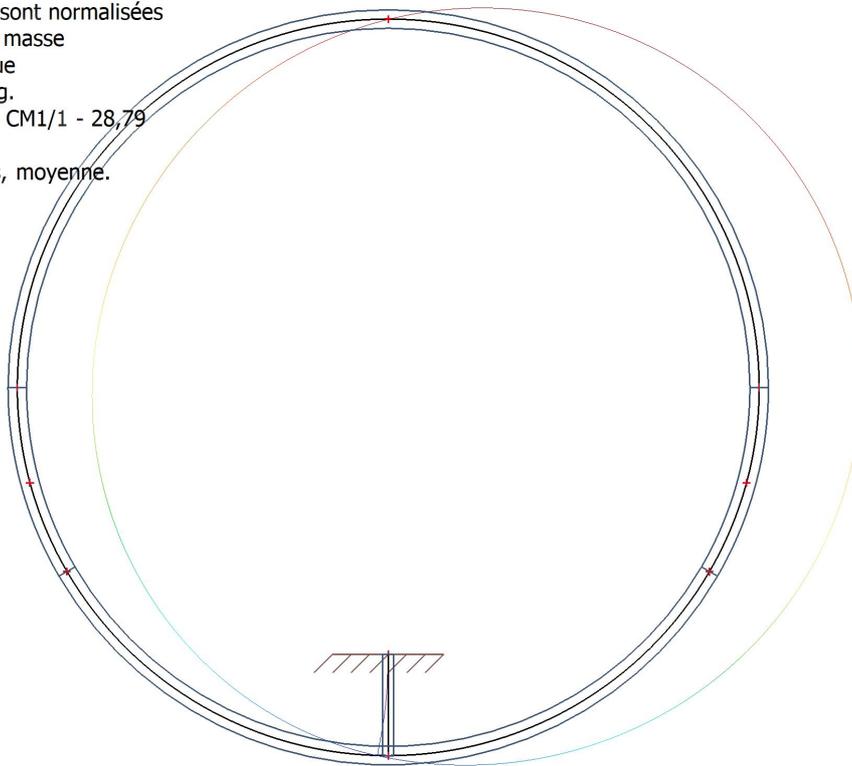
4. RESULTS

4.1. Eigen frequencies

| N | f [Hz] | ω [1/s] | ω^2 [1/s ²] | T [s] |
|-------------------------------|-----------|-------------------|-----------------------------------|----------|
| Mass combination : CM1 | | | | |
| 1 | 28,79 | 180,89 | 32720,84 | 0,03 |
| 2 | 189,06 | 1187,89 | 1411071,76 | 0,01 |
| 3 | 267,95 | 1683,53 | 2834278,93 | 0,00 |
| 4 | 637,78 | 4007,14 | 16057207,00 | 0,00 |
| 5 | 681,01 | 4278,81 | 18308240,59 | 0,00 |
| 6 | 1061,28 | 6668,04 | 44462754,18 | 0,00 |

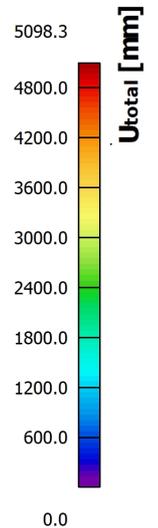
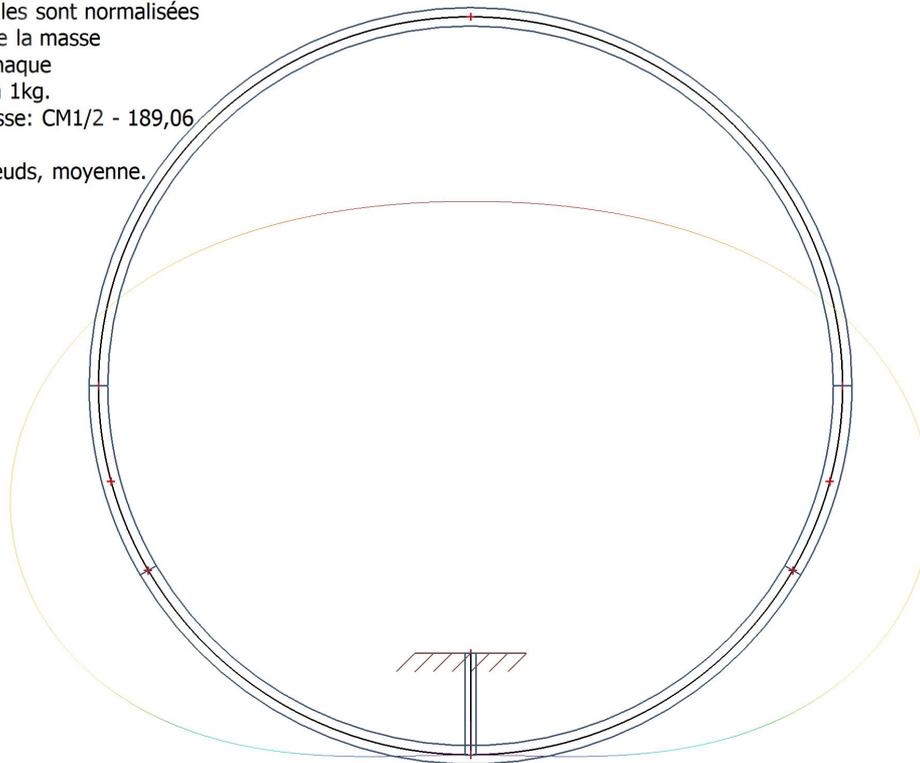
4.2. 3D displacement; U_{total}

Valeur: U_{total}
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/1 - 28,79
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



4.3. 3D displacement; U_{total}

Valeur: U_{total}
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/2 - 189,06
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



4.4. 3D displacement; U_{total}

Valeur: U_{total}

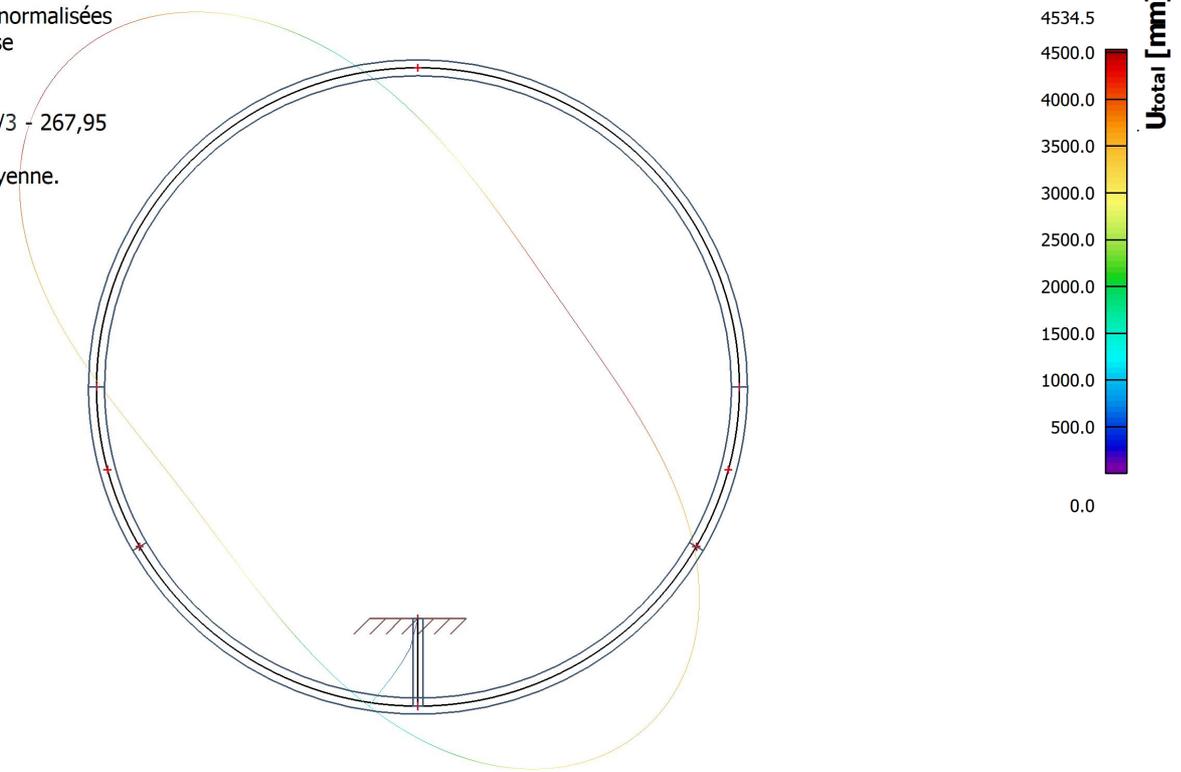
Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.

Combinaison masse: CM1/3 - 267,95

Sélection: Tout

Position: Aux noeuds, moyenne.

Système: Global



4.5. 3D displacement; U_{total}

Valeur: U_{total}

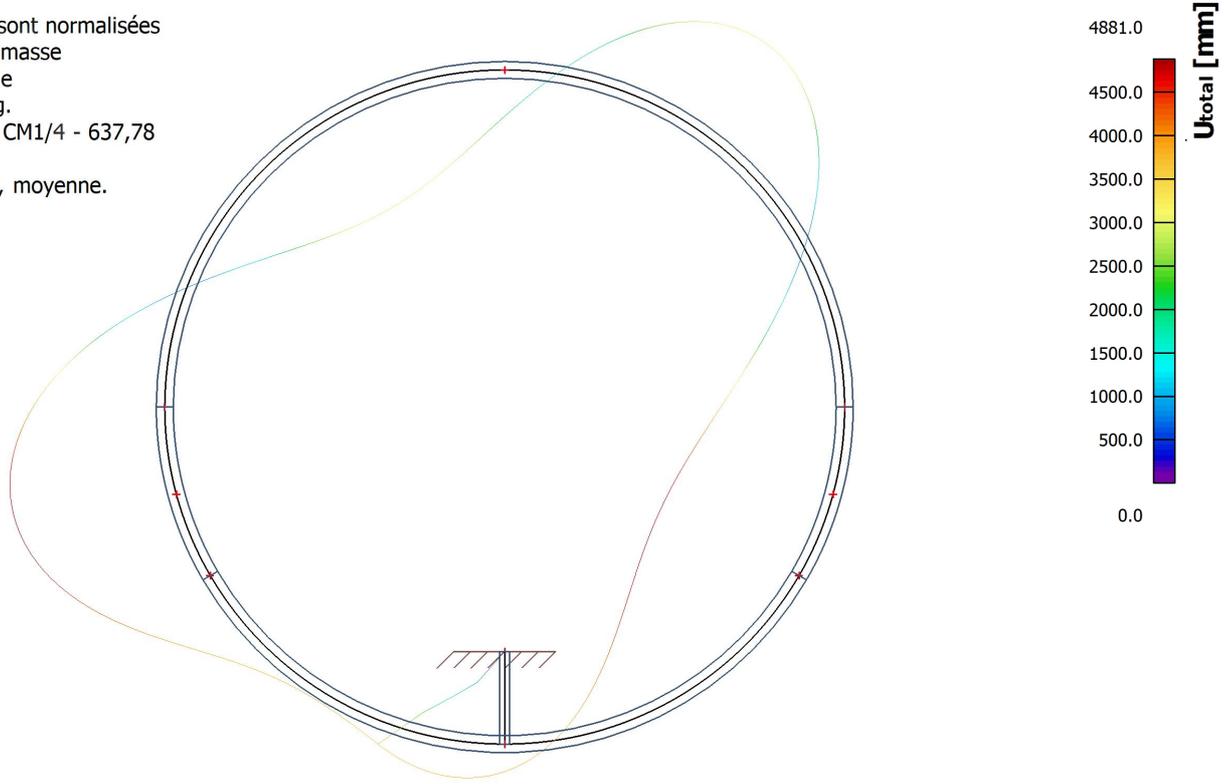
Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.

Combinaison masse: CM1/4 - 637,78

Sélection: Tout

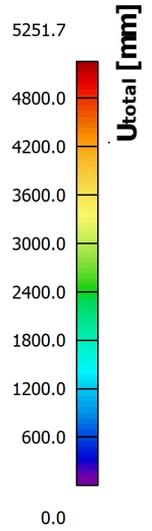
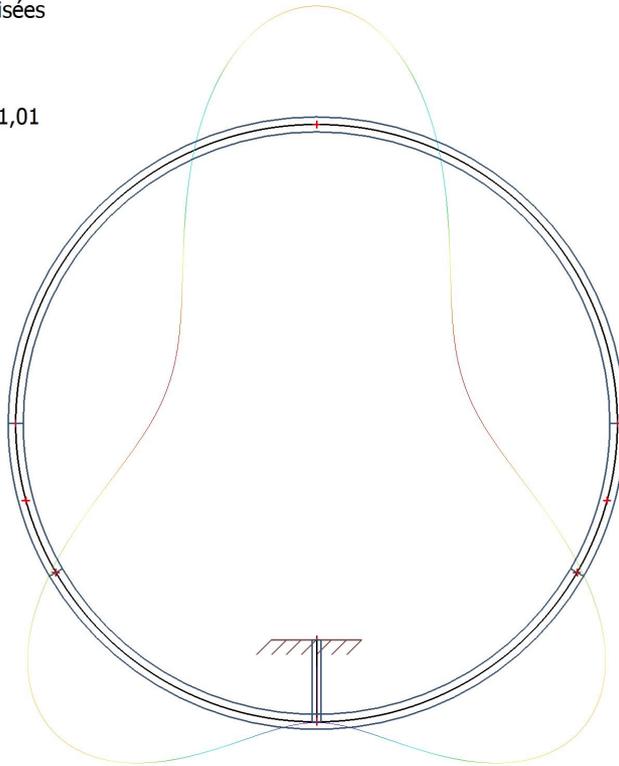
Position: Aux noeuds, moyenne.

Système: Global



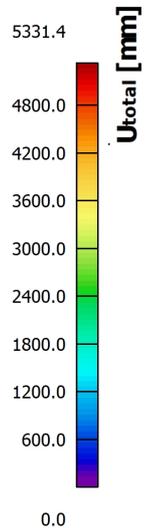
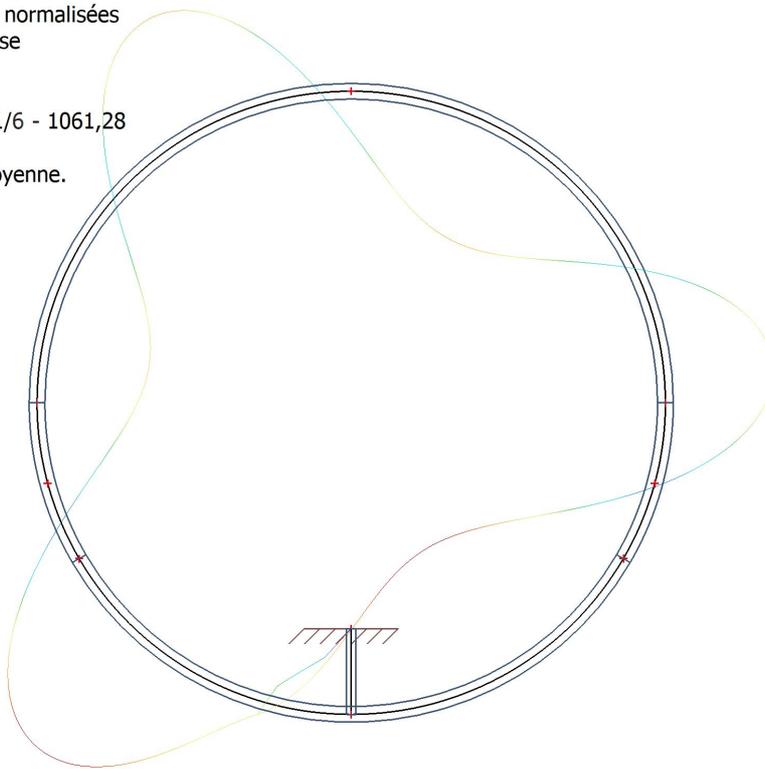
4.6. 3D displacement; U_{total}

Valeur: U_{total}
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/5 - 681,01
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



4.7. 3D displacement; U_{total}

Valeur: U_{total}
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/6 - 1061,28
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



5. EXPECTED AFNOR RESULTS

Eigenfrequencies:

f1 = 28.8 Hz

f2 = 189.3 Hz

f3 = 268.8 Hz

f4 = 641.0 Hz

f5 = 682.0 Hz

f6 = 1063.0 Hz

REFERENCE : "Guide de validation des progiciels de calcul de structures" AFNOR, 1990

1. TESTCASE DESCRIPTION

Modal analysis of pipes

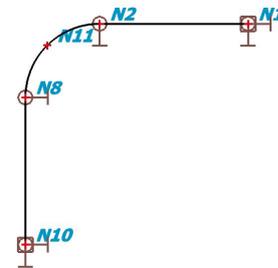
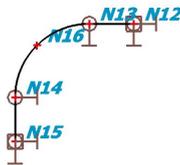
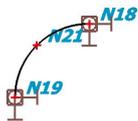
2. MODEL

2.1. Analysis model

Model 1

Model 2

Model 3



2.2. Nodes

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] | Member | Data |
|------|-------------|-------------|-------------|----------|------|
| N1 | 0,000 | 0,000 | 0,000 | B1 | Sn1 |
| N2 | 2,000 | 0,000 | 0,000 | B1 B5 | Sn3 |
| N8 | 3,000 | 0,000 | -1,000 | B5 B4 | Sn4 |
| N10 | 3,000 | 0,000 | -3,000 | B4 | Sn2 |
| N11 | 2,707 | 0,000 | -0,293 | B5 | |
| N12 | 7,400 | 0,000 | 0,000 | B6 | Sn5 |
| N13 | 8,000 | 0,000 | 0,000 | B6 B7 | Sn6 |

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] | Member | Data |
|------|-------------|-------------|-------------|----------|------|
| N14 | 9,000 | 0,000 | -1,000 | B7 B8 | Sn7 |
| N15 | 9,000 | 0,000 | -1,600 | B8 | Sn8 |
| N16 | 8,707 | 0,000 | -0,293 | B7 | |
| N18 | 13,000 | 0,000 | 0,000 | B10 | Sn10 |
| N19 | 14,000 | 0,000 | -1,000 | B10 | Sn11 |
| N21 | 13,707 | 0,000 | -0,293 | B10 | |

2.3. Members

| Name | Cross-section | Material | Length [m] | Beg. node | End node | Type |
|------|-----------------------|----------|------------|-----------|----------|-------------|
| B1 | CS1 - CHS (20,0; 2,0) | S 235 | 2,000 | N1 | N2 | general (0) |
| B5 | CS1 - CHS (20,0; 2,0) | S 235 | 1,571 | N2 | N8 | general (0) |
| B4 | CS1 - CHS (20,0; 2,0) | S 235 | 2,000 | N8 | N10 | general (0) |
| B6 | CS1 - CHS (20,0; 2,0) | S 235 | 0,600 | N12 | N13 | general (0) |
| B7 | CS1 - CHS (20,0; 2,0) | S 235 | 1,571 | N13 | N14 | general (0) |
| B8 | CS1 - CHS (20,0; 2,0) | S 235 | 0,600 | N14 | N15 | general (0) |
| B10 | CS1 - CHS (20,0; 2,0) | S 235 | 1,571 | N18 | N19 | general (0) |

2.4. Nodal supports

| Name | Node | System | Type | X | Y | Z | Rx | Ry | Rz |
|------|------|--------|----------|-------|-------|-------|-------|-------|-------|
| Sn1 | N1 | GCS | Standard | Rigid | Rigid | Rigid | Rigid | Rigid | Rigid |
| Sn2 | N10 | GCS | Standard | Rigid | Rigid | Rigid | Rigid | Rigid | Rigid |
| Sn3 | N2 | GCS | Standard | Free | Rigid | Rigid | Free | Free | Free |
| Sn4 | N8 | GCS | Standard | Rigid | Rigid | Free | Free | Free | Free |
| Sn5 | N12 | GCS | Standard | Rigid | Rigid | Rigid | Rigid | Rigid | Rigid |
| Sn6 | N13 | GCS | Standard | Free | Rigid | Rigid | Free | Free | Free |
| Sn7 | N14 | GCS | Standard | Rigid | Rigid | Free | Free | Free | Free |
| Sn8 | N15 | GCS | Standard | Rigid | Rigid | Rigid | Rigid | Rigid | Rigid |
| Sn10 | N18 | GCS | Standard | Rigid | Rigid | Rigid | Rigid | Rigid | Rigid |
| Sn11 | N19 | GCS | Standard | Rigid | Rigid | Rigid | Rigid | Rigid | Rigid |

2.5. Materials

Steel EC3

| Name | ρ [kg/m ³] | E_{mod} [MPa] | μ | Limit inférieure [mm] | Limite supérieure [mm] | F_y [MPa] | F_u [MPa] | Colour |
|-------|--------------------------------|--------------------|--------------------|--------------------------|---------------------------|----------------|----------------|---|
| | | G_{mod} [MPa] | α [m/mK] | | | | | |
| S 235 | 7850,00 | 2,1000e+05 | 0.3 | 0,0 | 40,0 | 235,0 | 360,0 |  |
| | | 8,0769e+04 | 0,01e-003 | 40,0 | 80,0 | 215,0 | 360,0 | |

2.6. Cross-sections

| CS1 | | |
|--|-----------------------------|------------|
| Type | CHS | |
| Detailed | 20,0; 2,0 | |
| Formcode | 3 - Circular hollow section | |
| Item material | S 235 | |
| A [m ²] | 1,1310e-04 | |
| A _y [m ²], A _z [m ²] | 7,2000e-05 | 7,2000e-05 |
| A _L [m ² /m], A _D [m ² /m] | 6,2829e-02 | 1,1309e-01 |
| c _{y,ucs} [mm], c _{z,ucs} [mm] | 10,0 | 10,0 |
| α [deg] | 0,00 | |
| I _y [m ⁴], I _z [m ⁴] | 4,6370e-09 | 4,6370e-09 |
| i _y [mm], i _z [mm] | 6,4 | 6,4 |
| W _{el,y} [m ³], W _{el,z} [m ³] | 4,6370e-07 | 4,6370e-07 |
| W _{pl,y} [m ³], W _{pl,z} [m ³] | 6,5067e-07 | 6,5067e-07 |
| M _{pl,y,+} [Nm], M _{pl,y,-} [Nm] | 152,86 | 152,86 |
| M _{pl,z,+} [Nm], M _{pl,z,-} [Nm] | 152,86 | 152,86 |
| d _y [mm], d _z [mm] | 0,0 | |
| I _t [m ⁴], I _w [m ⁶] | 9,1609e-09 | 1,0996e-45 |
| β _y [mm], β _z [mm] | 0,0 | |
| Picture | | |

3. LOAD and MASS

3.1. Mass groups

| Name | Load case |
|------|--------------------|
| MG1 | LC1 - Poids propre |

4. RESULTS

4.1. Eigen frequencies

| N | f [Hz] | ω [1/s] | ω^2 [1/s ²] | T [s] |
|-------------------------------|-----------|-------------------|-----------------------------------|----------|
| Mass combination : CM1 | | | | |
| 1 | 17,58 | 110,47 | 12203,53 | 0,06 |
| 2 | 24,33 | 152,87 | 23368,05 | 0,04 |
| 3 | 24,85 | 156,14 | 24380,00 | 0,04 |
| 4 | 26,61 | 167,18 | 27949,84 | 0,04 |
| 5 | 33,04 | 207,56 | 43081,63 | 0,03 |
| 6 | 34,71 | 218,09 | 47561,85 | 0,03 |
| 7 | 43,92 | 275,96 | 76152,13 | 0,02 |
| 8 | 67,00 | 420,97 | 177219,80 | 0,01 |
| 9 | 67,40 | 423,46 | 179318,51 | 0,01 |
| 10 | 74,10 | 465,54 | 216729,43 | 0,01 |
| 11 | 74,33 | 467,00 | 218087,11 | 0,01 |
| 12 | 93,77 | 589,14 | 347084,95 | 0,01 |
| 13 | 98,04 | 615,98 | 379435,01 | 0,01 |
| 14 | 98,24 | 617,27 | 381019,89 | 0,01 |
| 15 | 101,43 | 637,27 | 406112,56 | 0,01 |
| 16 | 118,96 | 747,42 | 558640,66 | 0,01 |
| 17 | 125,07 | 785,80 | 617476,18 | 0,01 |
| 18 | 142,48 | 895,18 | 801348,08 | 0,01 |
| 19 | 143,54 | 901,88 | 813393,30 | 0,01 |
| 20 | 151,92 | 954,49 | 911044,18 | 0,01 |
| 21 | 152,20 | 956,30 | 914515,77 | 0,01 |
| 22 | 182,37 | 1145,81 | 1312877,15 | 0,01 |
| 23 | 191,13 | 1200,87 | 1442097,36 | 0,01 |
| 24 | 192,92 | 1212,12 | 1469244,78 | 0,01 |
| 25 | 206,01 | 1294,34 | 1675326,10 | 0,00 |
| 26 | 224,55 | 1410,85 | 1990490,99 | 0,00 |

4.2. 3D displacement; U_{total}

Valeur: **U_{total}**

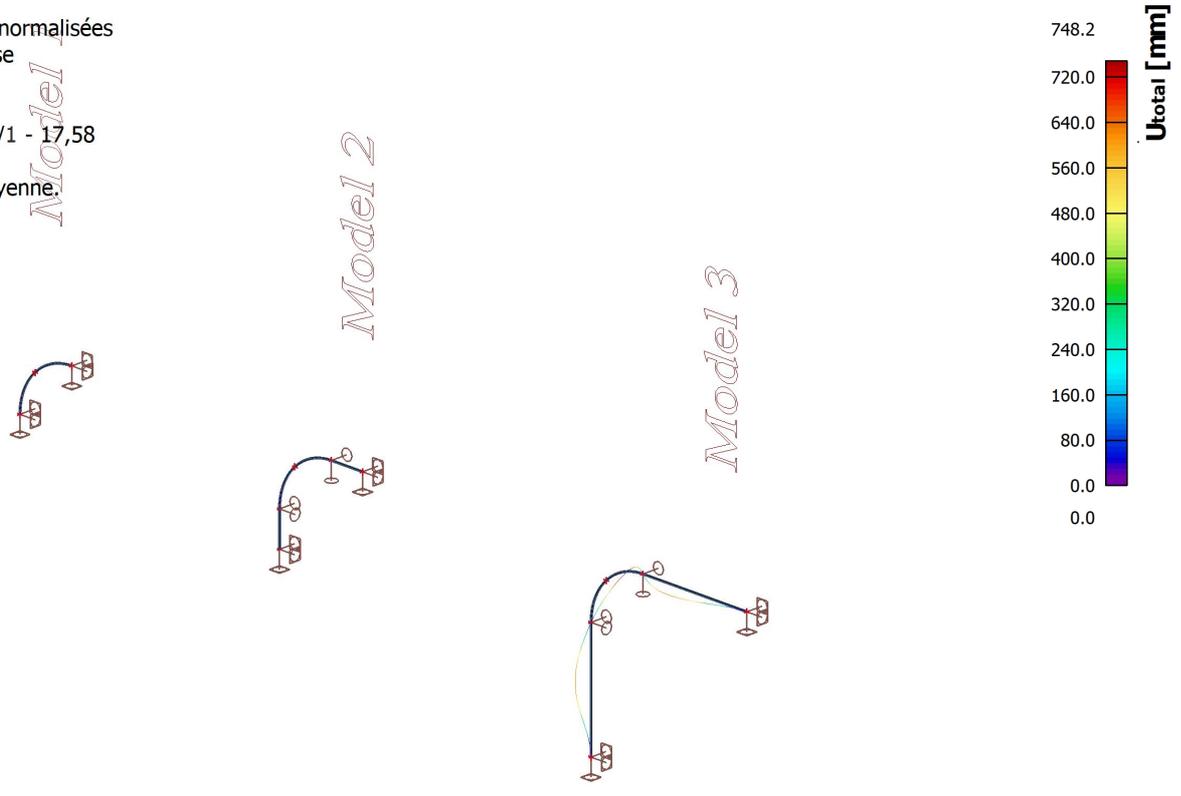
Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.

Combinaison masse: CM1/1 - 17,58

Sélection: Tout

Position: Aux noeuds, moyenne.

Système: Global



4.3. 3D displacement; U_{total}

Valeur: **U_{total}**

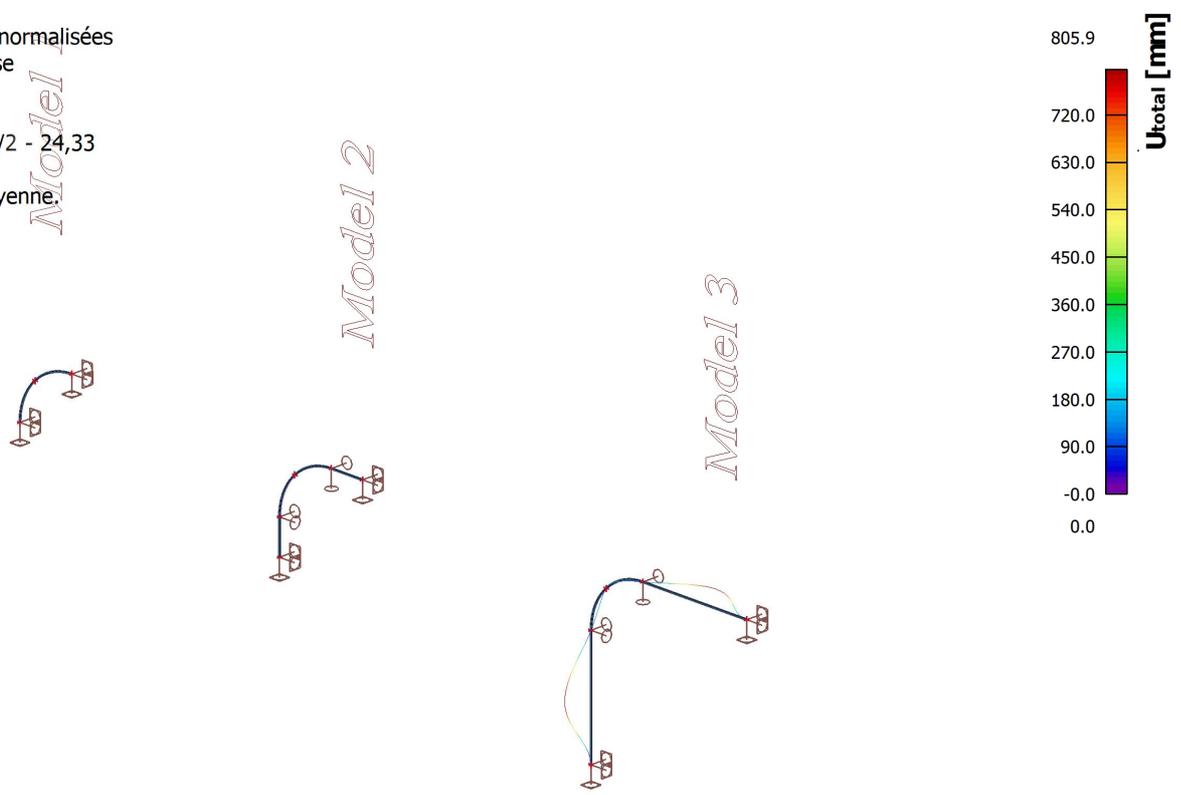
Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.

Combinaison masse: CM1/2 - 24,33

Sélection: Tout

Position: Aux noeuds, moyenne.

Système: Global



4.4. 3D displacement; U_{total}

Valeur: U_{total}

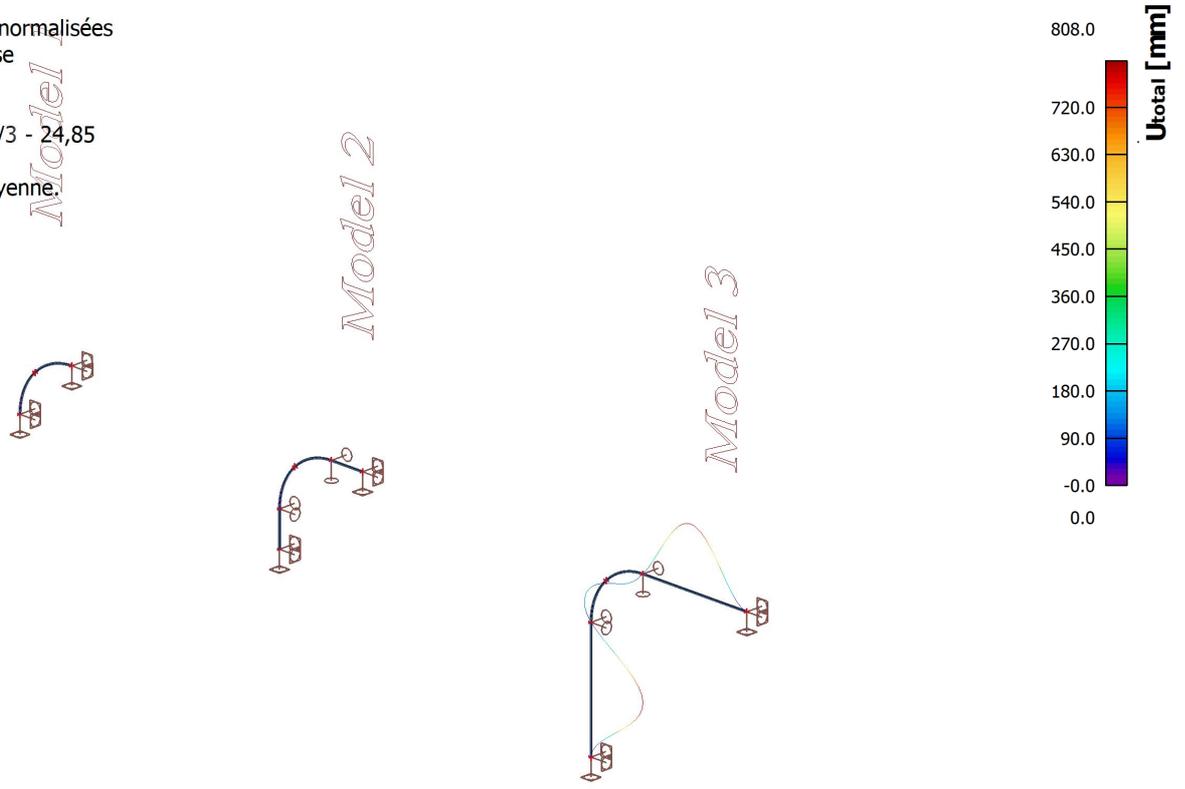
Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.

Combinaison masse: CM1/3 - 24,85

Sélection: Tout

Position: Aux noeuds, moyenne.

Système: Global



4.5. 3D displacement; U_{total}

Valeur: U_{total}

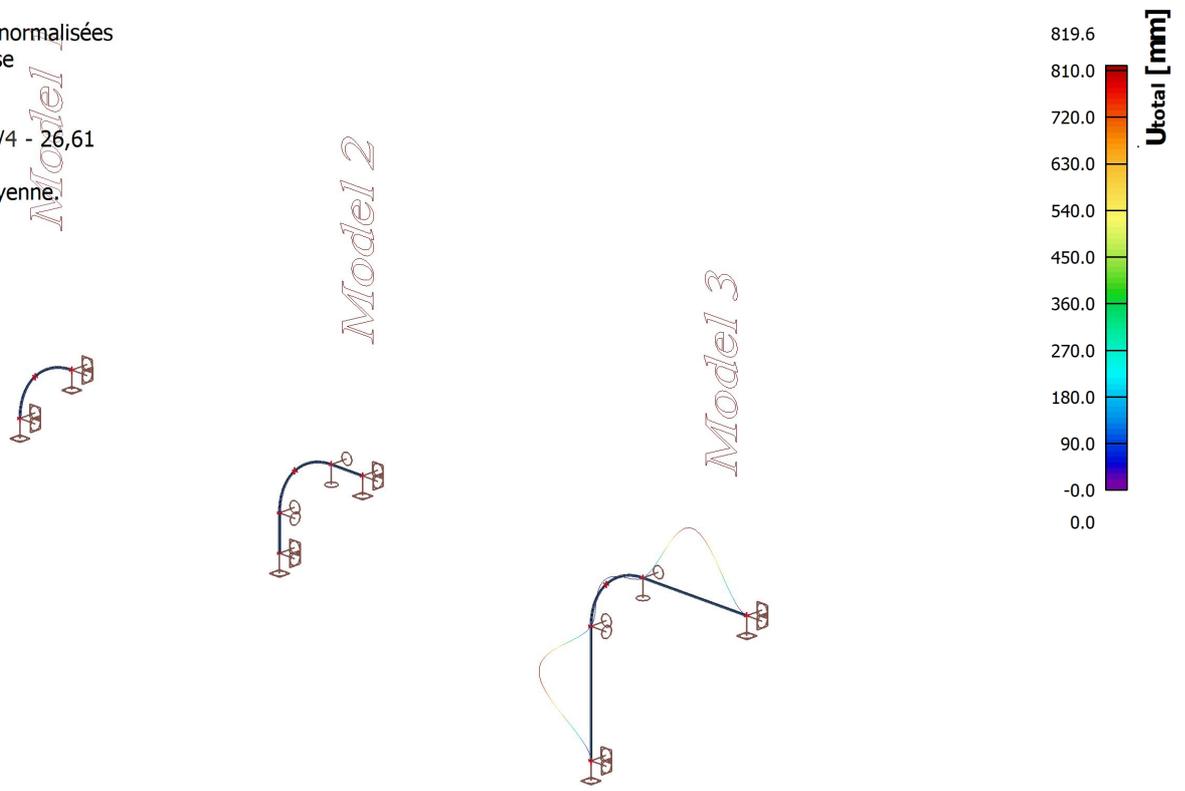
Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.

Combinaison masse: CM1/4 - 26,61

Sélection: Tout

Position: Aux noeuds, moyenne.

Système: Global



4.6. 3D displacement; U_{total}

Valeur: U_{total}

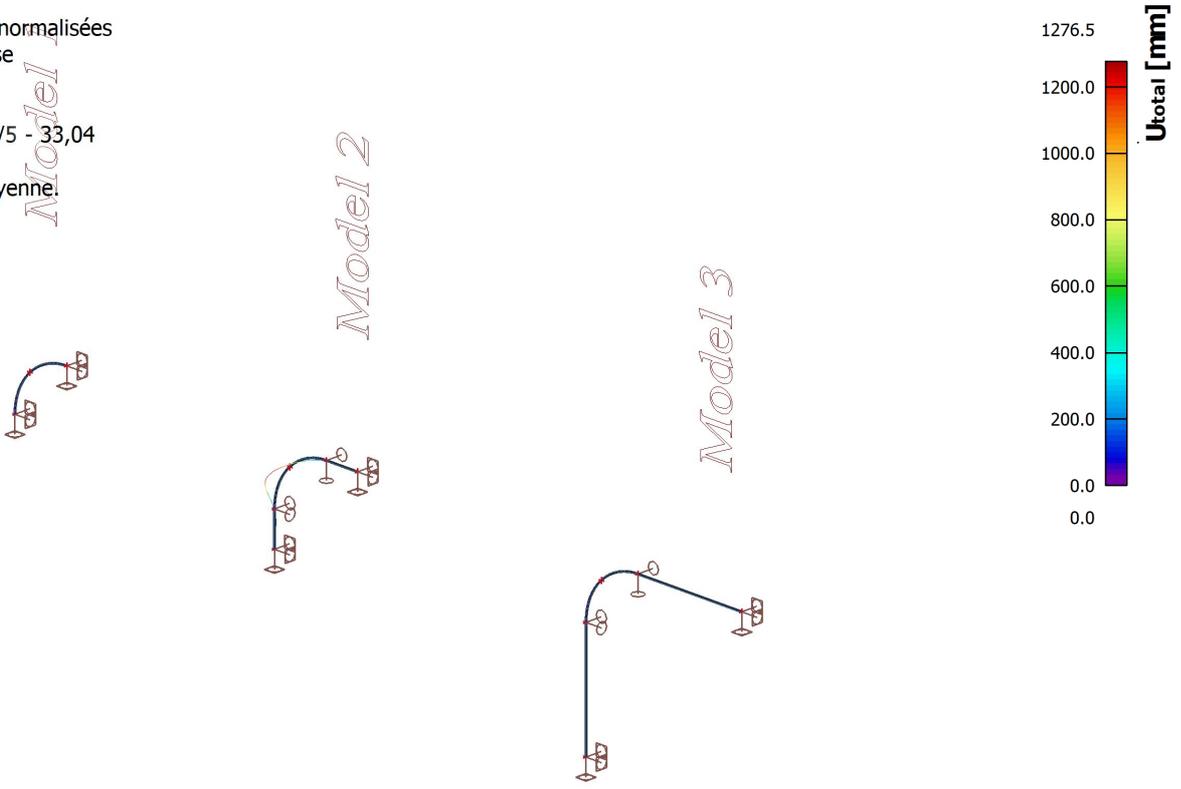
Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.

Combinaison masse: CM1/5 - 33,04

Sélection: Tout

Position: Aux noeuds, moyenne.

Système: Global



4.7. 3D displacement; U_{total}

Valeur: U_{total}

Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.

Combinaison masse: CM1/12 - 93,77

Sélection: Tout

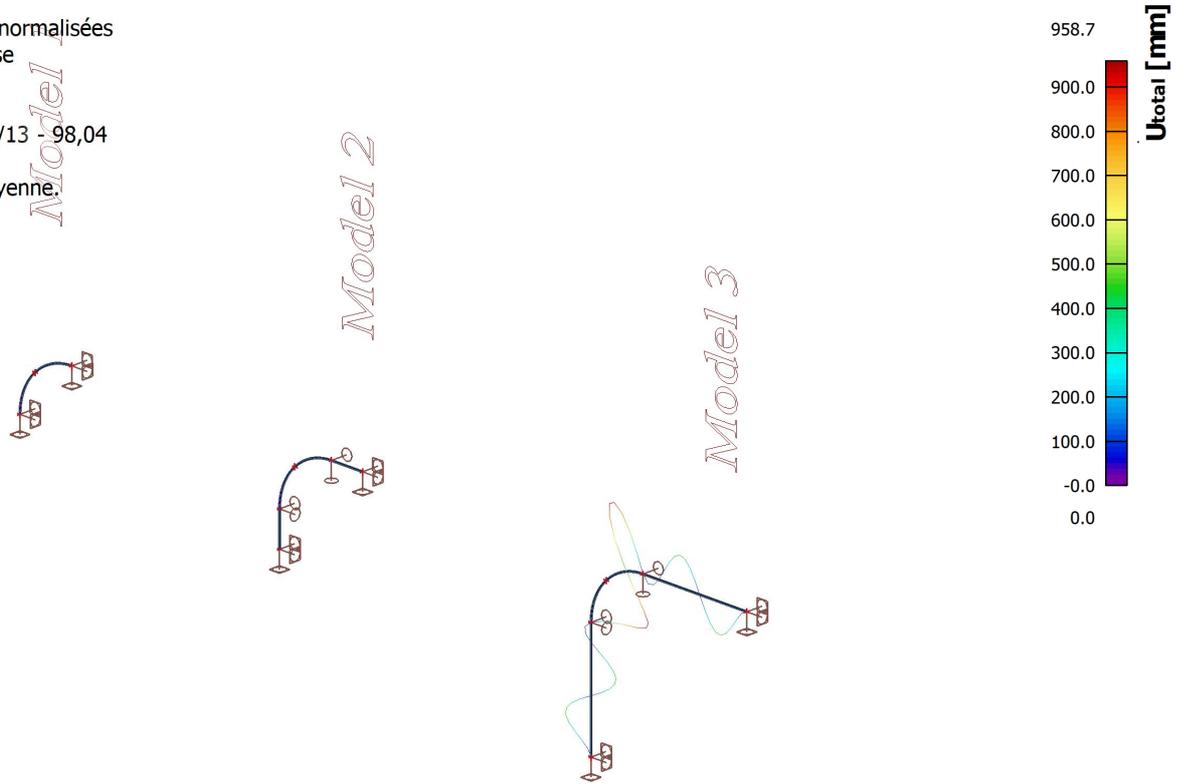
Position: Aux noeuds, moyenne.

Système: Global



4.8. 3D displacement; U_{total}

Valeur: U_{total}
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/13 - 98,04
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



4.9. 3D displacement; U_{total}

Valeur: U_{total}
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/22 - 182,37
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



4.10. 3D displacement; U_total

Valeur: U_{total}

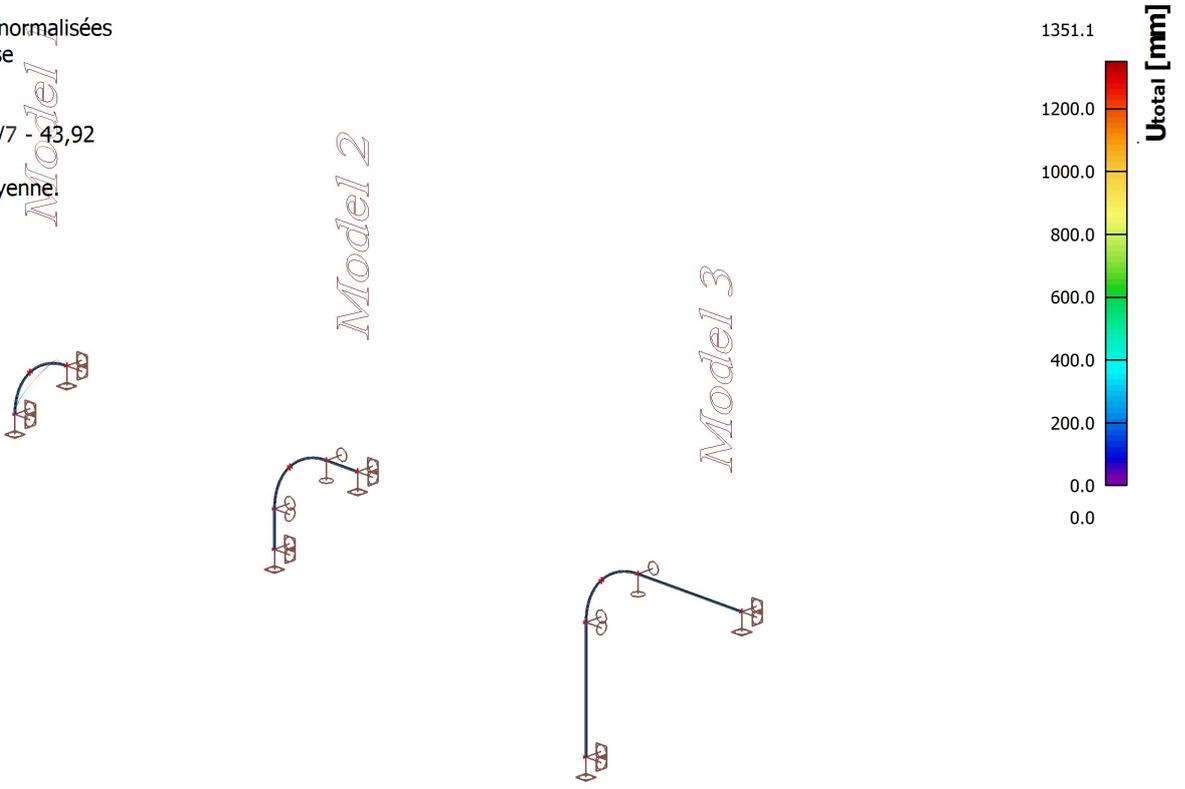
Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.

Combinaison masse: CM1/7 - 43,92

Sélection: Tout

Position: Aux noeuds, moyenne.

Système: Global



4.11. 3D displacement; U_total

Valeur: U_{total}

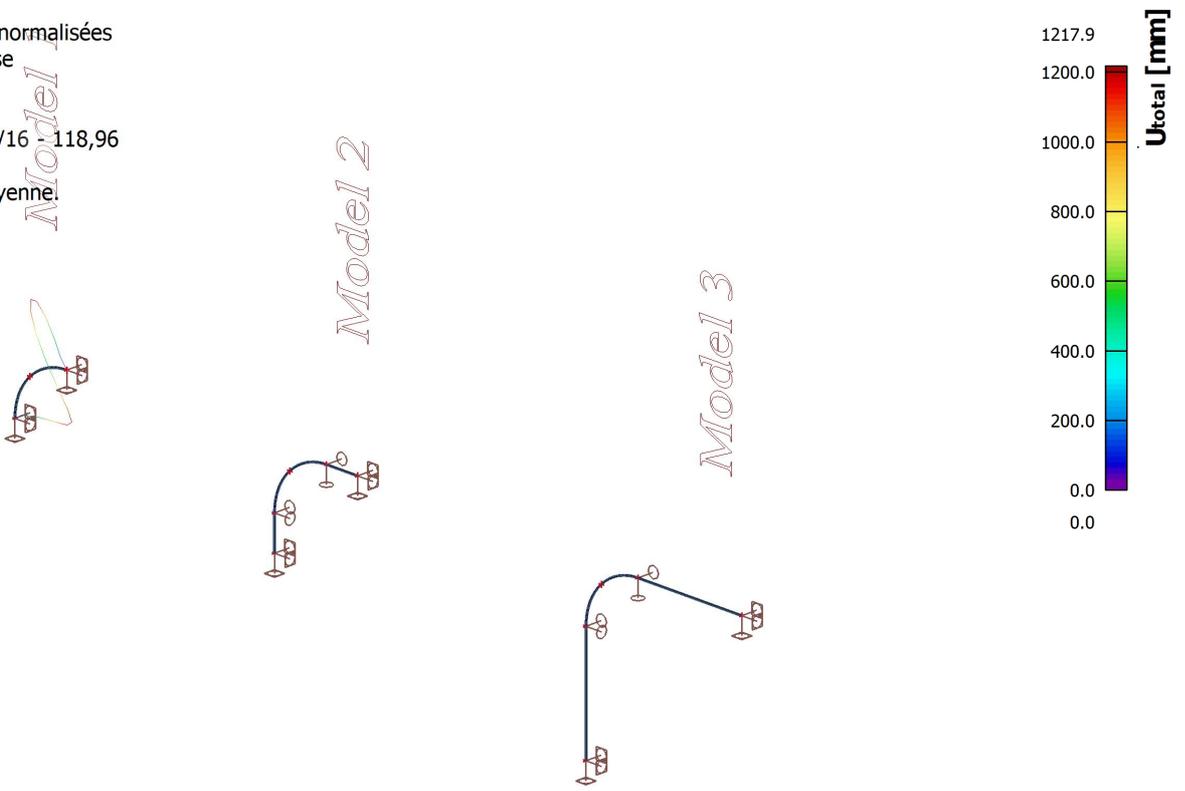
Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.

Combinaison masse: CM1/16 - 118,96

Sélection: Tout

Position: Aux noeuds, moyenne.

Système: Global



4.12. 3D displacement; U_total

Valeur: U_{total}

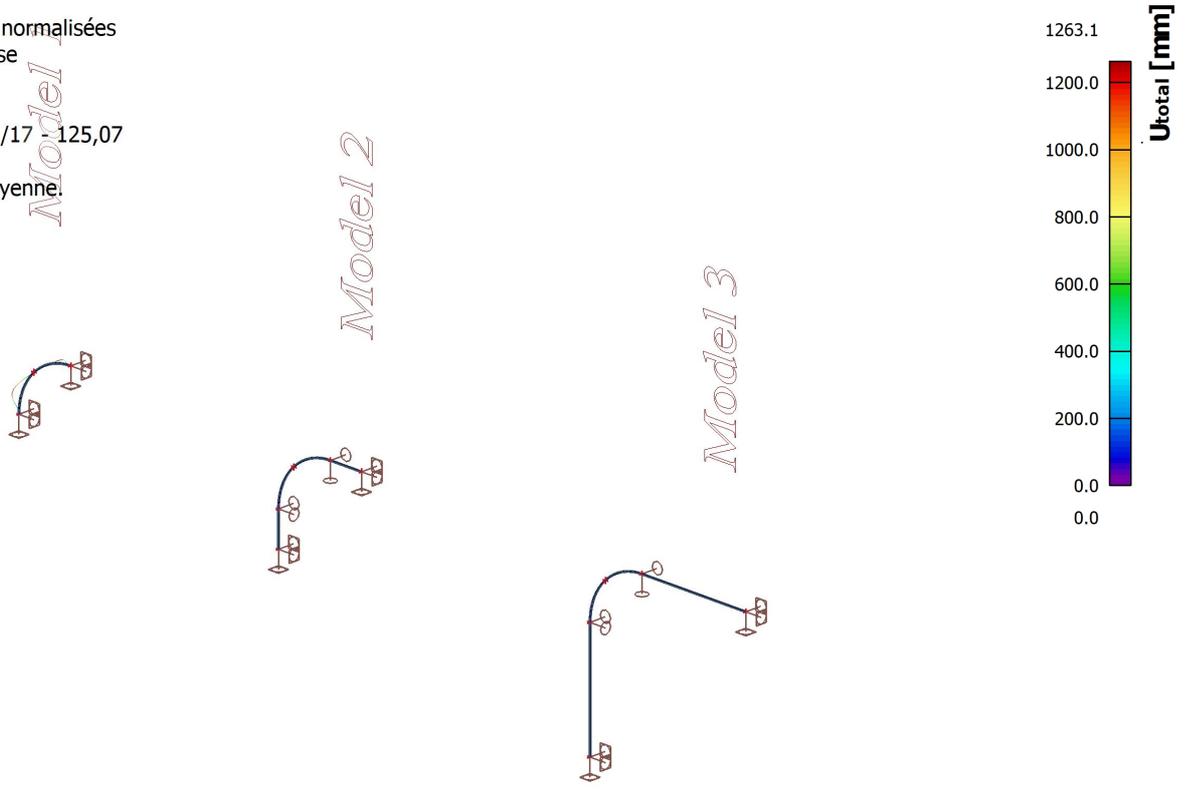
Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.

Combinaison masse: CM1/17 - 125,07

Sélection: Tout

Position: Aux noeuds, moyenne.

Système: Global



4.13. 3D displacement; U_total

Valeur: U_{total}

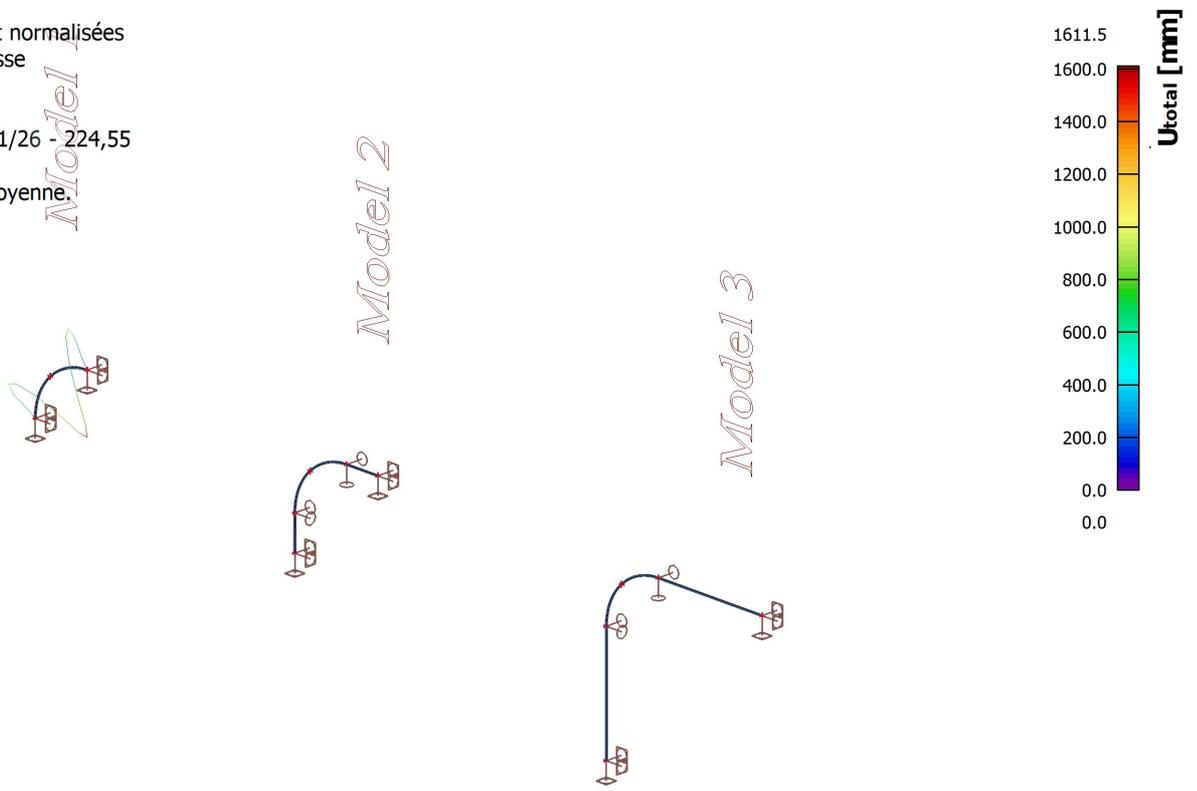
Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.

Combinaison masse: CM1/26 - 224,55

Sélection: Tout

Position: Aux noeuds, moyenne.

Système: Global



5. EXPECTED AFNOR RESULTS

Model 1:

Transversal mode 1 = 44.23 Hz

In-plane mode 1 = 119.0 Hz

Transversal mode 2 = 125.0 Hz

In-plane mode 2 = 227.0 Hz

Model 2:

Transversal mode 1 = 33.4 Hz

In-plane mode 1 = 94.0 Hz

Transversal mode 2 = 100.0Hz

In-plane mode 2 = 180.0 Hz

Model 3:

Transversal mode 1 = 17.9 Hz

Transversal mode 2 = 24.8 Hz

In-plane mode 1 = 25.3 Hz

In-plane mode 2 = 27.0 Hz

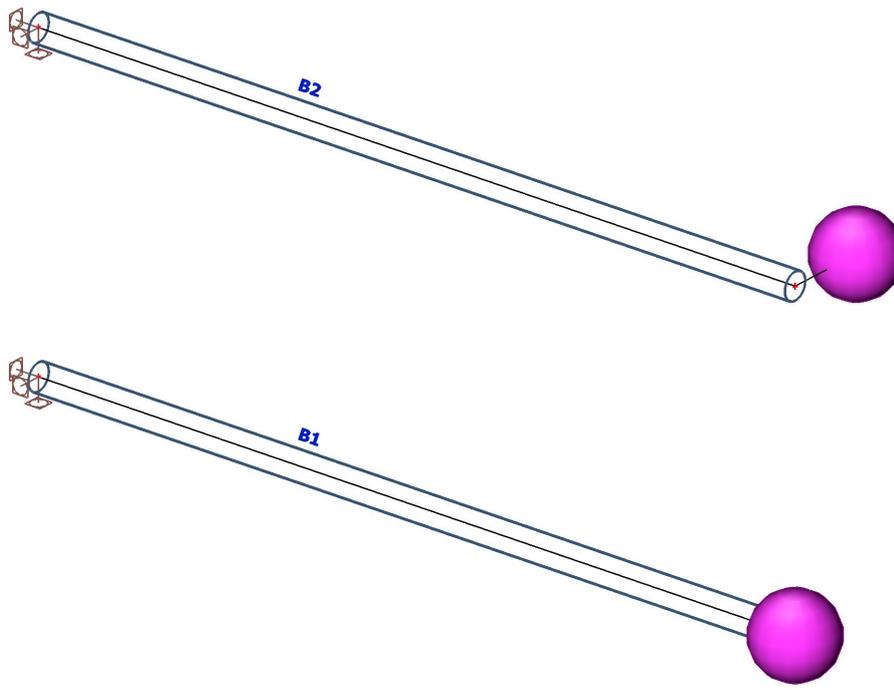
REFERENCE : "Guide de validation des progiciels de calcul de structures" AFNOR, 1990

1. TESTCASE DESCRIPTION

Modal analysis of a cantilever beam with mass at the extremity (with and without eccentricity) - Bending-torsion coupling

2. MODEL

2.1. Analysis model



2.2. Nodes

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] | Member | Data |
|------|-------------|-------------|-------------|--------|------|
| N1 | 0,048 | 0,000 | 0,000 | B1 | Sn1 |
| N2 | 10,048 | 0,000 | 0,000 | B1 | MN1 |
| N3 | 0,048 | 0,000 | 4,000 | B2 | Sn2 |

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] | Member | Data |
|------|-------------|-------------|-------------|--------|------|
| N4 | 10,048 | 0,000 | 4,000 | B2 | |
| | | | | B3 | |
| N5 | 10,048 | 1,000 | 4,000 | B3 | MN3 |

2.3. Members

| Name | Cross-section | Material | Length [m] | Beg. node | End node | Type |
|------|------------------------------|----------|------------|-----------|----------|-------------|
| B1 | CS1 - CHS (350; 15) | S 355 | 10,000 | N1 | N2 | general (0) |
| B2 | CS1 - CHS (350; 15) | S 355 | 10,000 | N3 | N4 | general (0) |
| B3 | CS2 - Rond plein (Numérique) | RIGID | 1,000 | N4 | N5 | general (0) |

2.4. Nodal supports

| Name | Node | System | Type | X | Y | Z | Rx | Ry | Rz |
|------|------|--------|----------|-------|-------|-------|-------|-------|-------|
| Sn1 | N1 | GCS | Standard | Rigid | Rigid | Rigid | Rigid | Rigid | Rigid |
| Sn2 | N3 | GCS | Standard | Rigid | Rigid | Rigid | Rigid | Rigid | Rigid |

2.5. Materials

Steel EC3

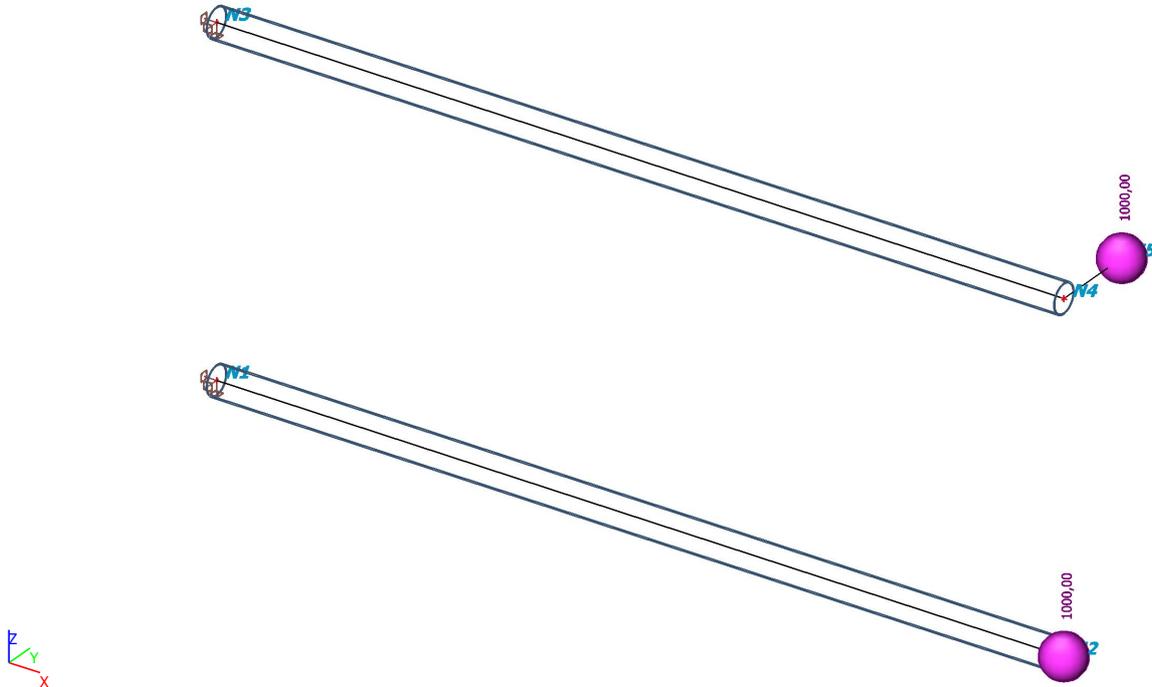
| Name | ρ [kg/m ³] | E_{mod} [MPa] | μ | Limite inférieure [mm] | Limite supérieure [mm] | F_y [MPa] | F_u [MPa] | Colour |
|-------|--------------------------------|--------------------|--------------------|---------------------------|---------------------------|----------------|----------------|--------|
| | | G_{mod} [MPa] | α [m/mK] | | | | | |
| S 355 | 7800,00 | 2,1000e+05 | 0.3 | 0 | 40 | 355,0 | 490,0 | ■ |
| | | 8,0769e+04 | 0,01e-003 | 40 | 80 | 335,0 | 470,0 | |
| RIGID | 0,00 | 3,0000e+10 | 0.25 | 0 | 40 | 235,0 | 360,0 | ■ |
| | | 1,2000e+10 | 0,01e-003 | 40 | 80 | 215,0 | 360,0 | |

2.6. Cross-sections

| CS1 | | |
|--|-----------------------------|-------------|
| Type | CHS | |
| Detailed | 350; 15 | |
| Formcode | 3 - Circular hollow section | |
| Item material | S 355 | |
| A [m ²] | 1,5787e-02 | |
| A _y [m ²], A _z [m ²] | 1,0050e-02 | 1,0050e-02 |
| A _L [m ² /m], A _D [m ² /m] | 1,0995e+00 | 2,1048e+00 |
| c _{y,UCS} [mm], c _{z,UCS} [mm] | 175 | 175 |
| α [deg] | 0,00 | |
| I _y [m ⁴], I _z [m ⁴] | 2,2190e-04 | 2,2190e-04 |
| i _y [mm], i _z [mm] | 119 | 119 |
| W _{el,y} [m ³], W _{el,z} [m ³] | 1,2680e-03 | 1,2680e-03 |
| W _{pl,y} [m ³], W _{pl,z} [m ³] | 1,6845e-03 | 1,6845e-03 |
| M _{pl,y,+} [Nm], M _{pl,y,-} [Nm] | 597815,36 | 597815,36 |
| M _{pl,z,+} [Nm], M _{pl,z,-} [Nm] | 597815,36 | 597815,36 |
| d _y [mm], d _z [mm] | 0 | 0 |
| I _t [m ⁴], I _w [m ⁶] | 4,4291e-04 | 6,6891e-39 |
| β_y [mm], β_z [mm] | 0 | 0 |
| Picture | | |
| CS2 | | |
| Type | Rond plein | |
| Detailed | Numerical | |
| A [m ²] | 7,8540e-01 | |
| A _y [m ²], A _z [m ²] | 6,7325e-01 | 6,7325e-01 |
| A _L [m ² /m], A _D [m ² /m] | 3,1414e+00 | 3,1414e+00 |
| c _{y,UCS} [mm], c _{z,UCS} [mm] | 500 | 500 |
| α [deg] | 0,00 | |
| I _y [m ⁴], I _z [m ⁴] | 4,9087e-02 | 4,9087e-02 |
| i _y [mm], i _z [mm] | 250 | 250 |
| W _{el,y} [m ³], W _{el,z} [m ³] | 9,8175e-02 | 9,8175e-02 |
| W _{pl,y} [m ³], W _{pl,z} [m ³] | 1,6667e-01 | 1,6667e-01 |
| M _{pl,y,+} [Nm], M _{pl,y,-} [Nm] | 39154737,03 | 39154737,03 |
| M _{pl,z,+} [Nm], M _{pl,z,-} [Nm] | 39154737,03 | 39154737,03 |
| d _y [mm], d _z [mm] | 0 | 0 |
| I _t [m ⁴], I _w [m ⁶] | 9,8109e-02 | 2,2156e-13 |
| β_y [mm], β_z [mm] | 0 | 0 |

3. LOAD and MASS

3.1. LC1 / Tot. value



3.2. Nodal mass

| Name | Mass group | M [kg] | Imx [kgm ²] | Koeff mx | Imy [kgm ²] | Koeff my | Imz [kgm ²] | Koeff mz | Node |
|------|------------|---------|-------------------------|----------|-------------------------|----------|-------------------------|----------|------|
| MN1 | MG1 | 1000,00 | 0,00 | 1 | 0,00 | 1 | 0,00 | 1 | N2 |
| MN3 | MG1 | 1000,00 | 0,00 | 1 | 0,00 | 1 | 0,00 | 1 | N5 |

| Explanations of symbols | |
|-------------------------|----------------------|
| Node | (10,048;0,000;0,000) |

3.3. Mass groups

| Name |
|------|
| MG1 |

4. RESULTS

4.1. Eigen frequencies

| N | f [Hz] | ω [1/s] | ω^2 [1/s ²] | T [s] |
|-------------------------------|-----------|-------------------|-----------------------------------|----------|
| Mass combination : CM1 | | | | |
| 1 | 1,62 | 10,17 | 103,42 | 0,62 |
| 2 | 1,64 | 10,31 | 106,38 | 0,61 |
| 3 | 1,66 | 10,40 | 108,18 | 0,60 |
| 4 | 1,66 | 10,40 | 108,18 | 0,60 |
| 5 | 13,45 | 84,53 | 7145,34 | 0,07 |
| 6 | 13,59 | 85,36 | 7285,82 | 0,07 |
| 7 | 16,07 | 100,94 | 10189,89 | 0,06 |
| 8 | 16,07 | 100,95 | 10189,90 | 0,06 |
| 9 | 28,86 | 181,32 | 32875,63 | 0,03 |
| 10 | 31,95 | 200,75 | 40299,19 | 0,03 |
| 11 | 49,98 | 314,01 | 98600,86 | 0,02 |
| 12 | 49,98 | 314,01 | 98600,96 | 0,02 |
| 13 | 61,49 | 386,37 | 149279,13 | 0,02 |
| 14 | 63,87 | 401,31 | 161053,68 | 0,02 |
| 15 | 76,47 | 480,46 | 230843,32 | 0,01 |
| 16 | 80,37 | 504,95 | 254969,74 | 0,01 |
| 17 | 103,00 | 647,15 | 418798,87 | 0,01 |
| 18 | 103,00 | 647,15 | 418799,29 | 0,01 |

4.2. 3D displacement; Beam B1

Valeur: U_{total}

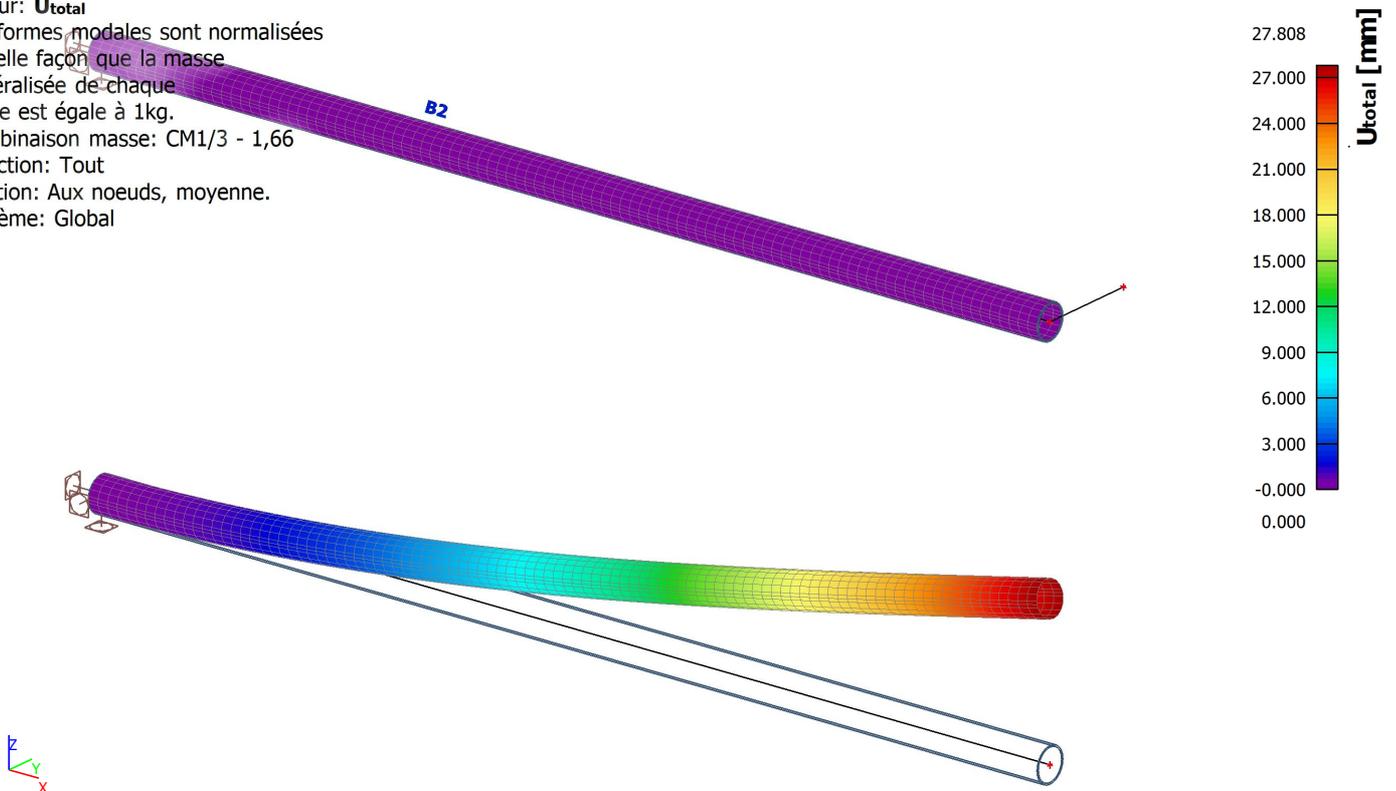
Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.

Combinaison masse: CM1/3 - 1,66

Sélection: Tout

Position: Aux noeuds, moyenne.

Système: Global



4.3. 3D displacement; Beam B1

Valeur: U_{total}

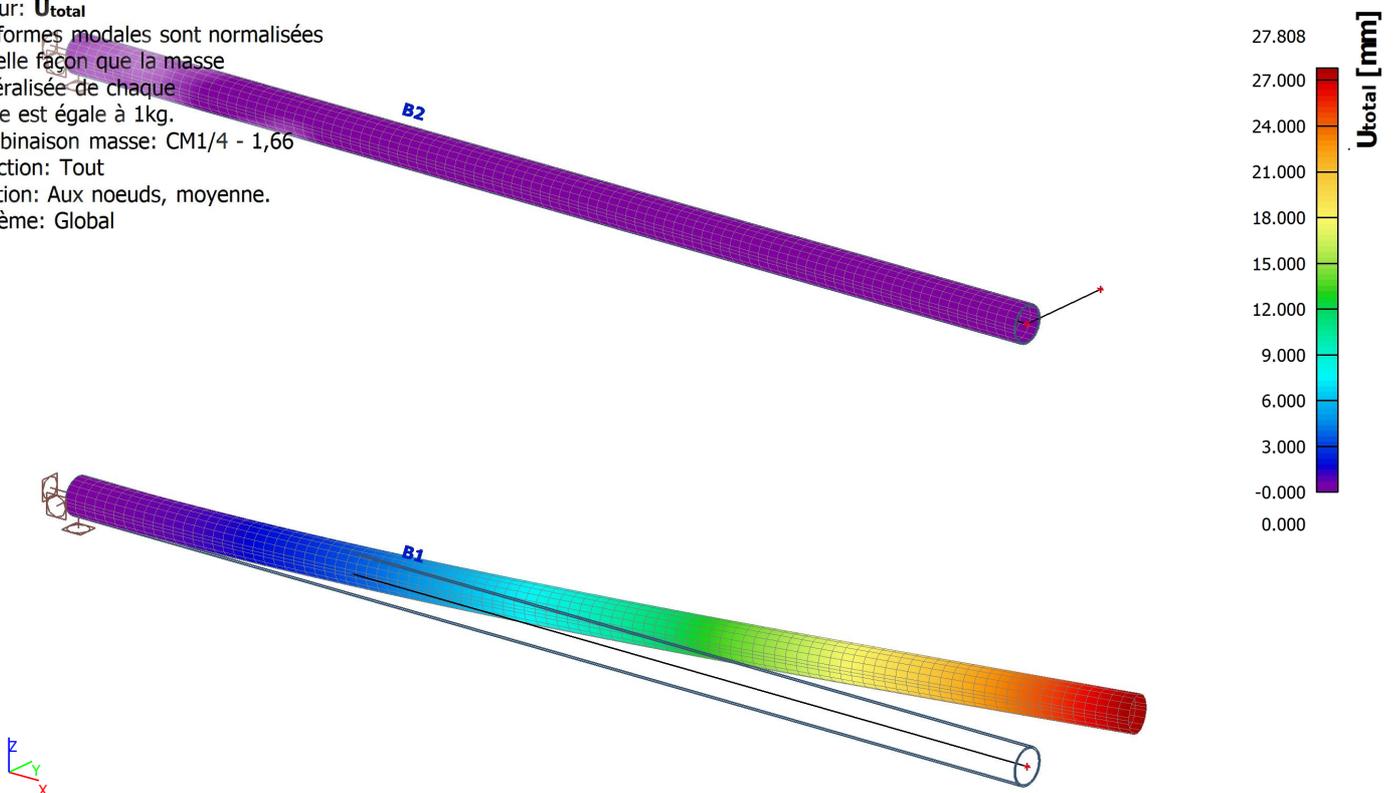
Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.

Combinaison masse: CM1/4 - 1,66

Sélection: Tout

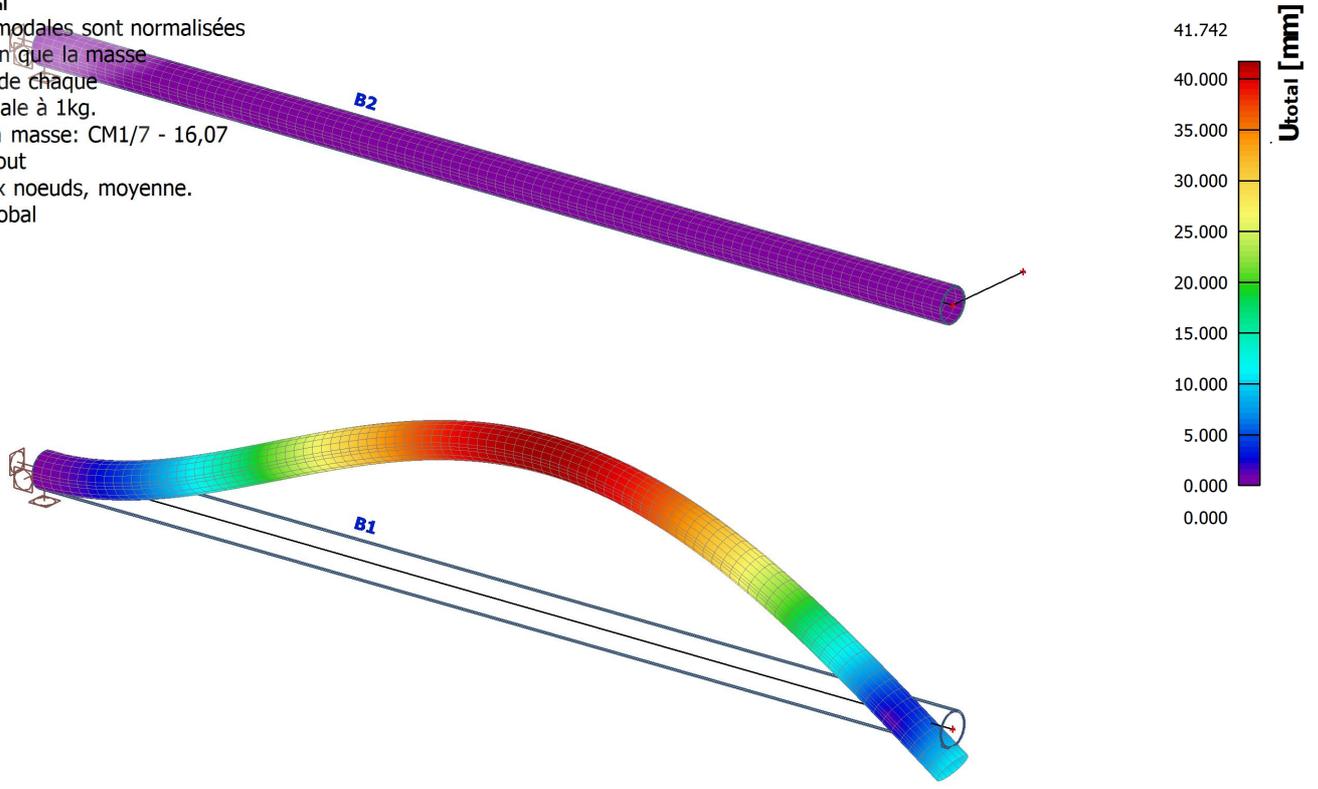
Position: Aux noeuds, moyenne.

Système: Global



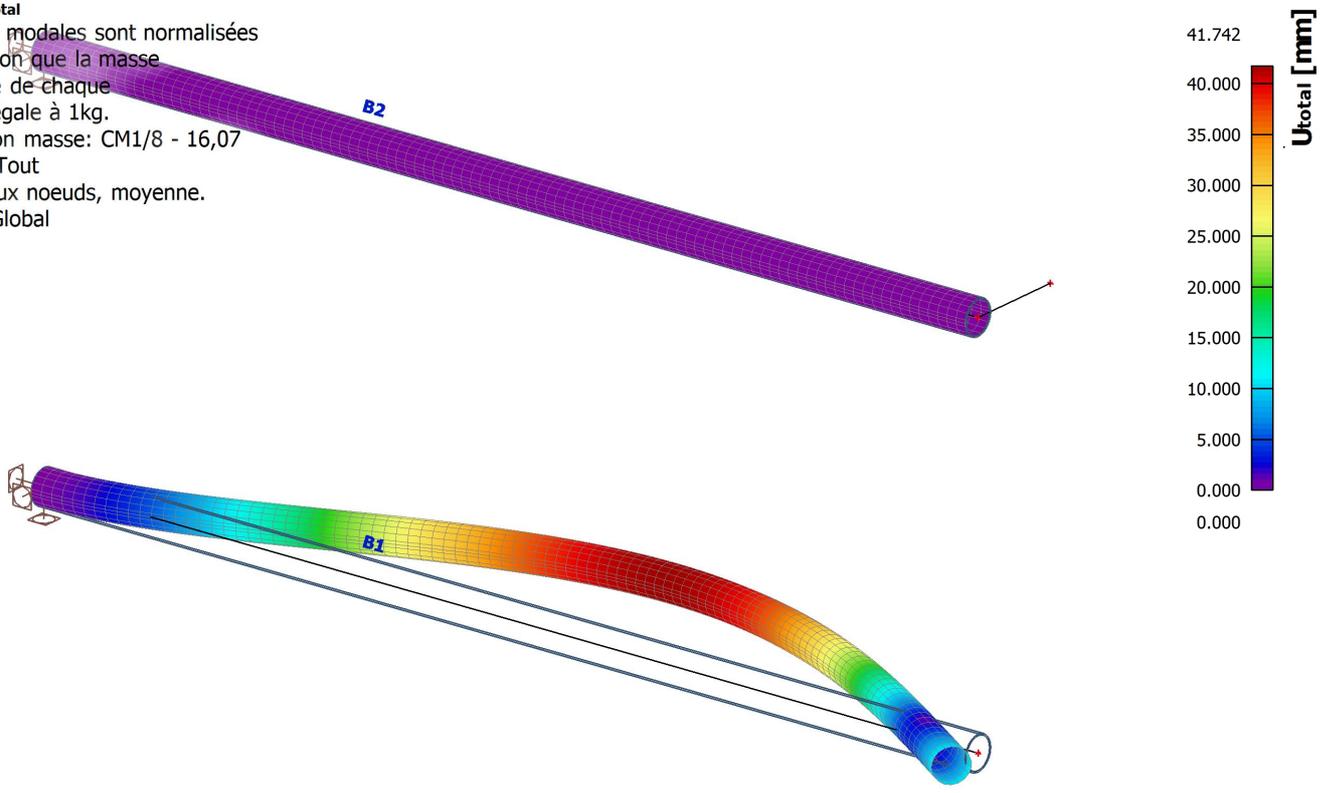
4.4. 3D displacement; Beam B1

Valeur: U_{total}
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/7 - 16,07
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



4.5. 3D displacement; Beam B1

Valeur: U_{total}
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/8 - 16,07
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



4.6. 3D displacement; Beam B1

Valeur: U_{total}

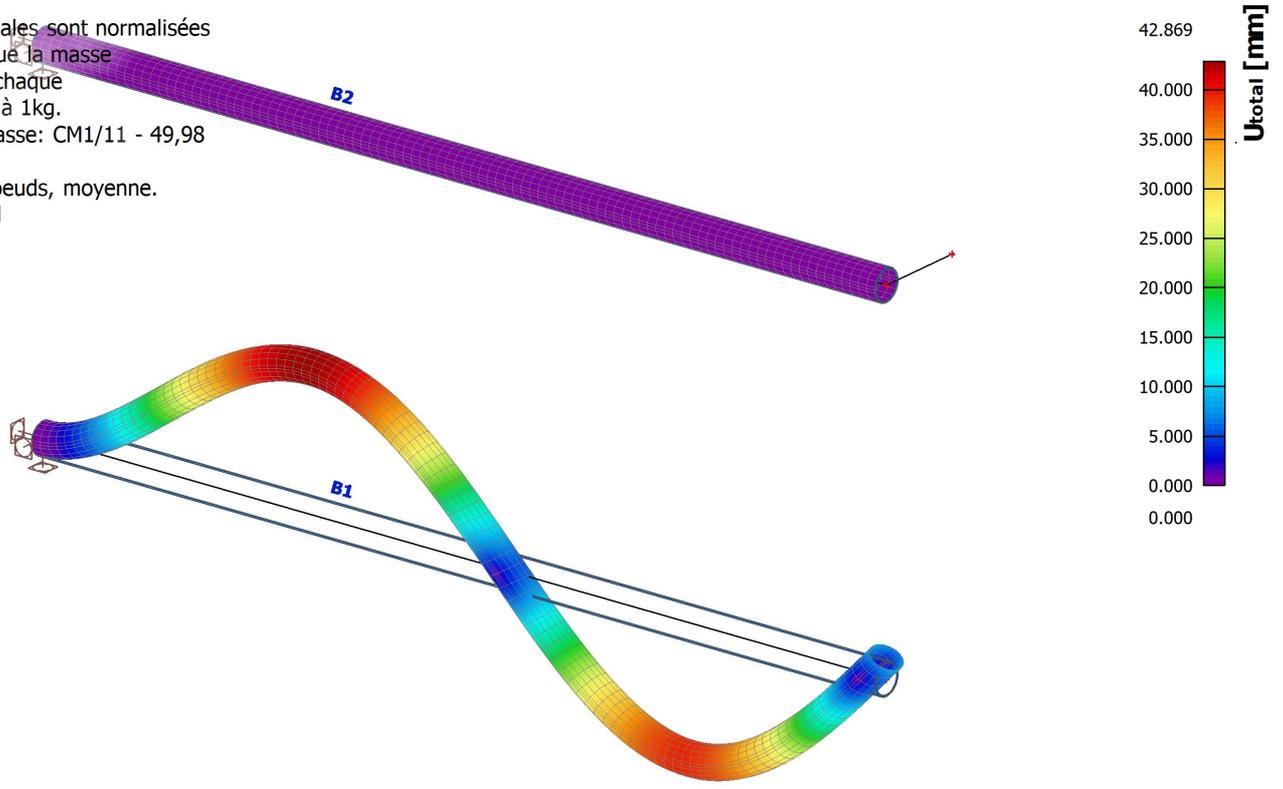
Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.

Combinaison masse: CM1/11 - 49,98

Sélection: Tout

Position: Aux noeuds, moyenne.

Système: Global



4.7. 3D displacement; Beam B1

Valeur: U_{total}

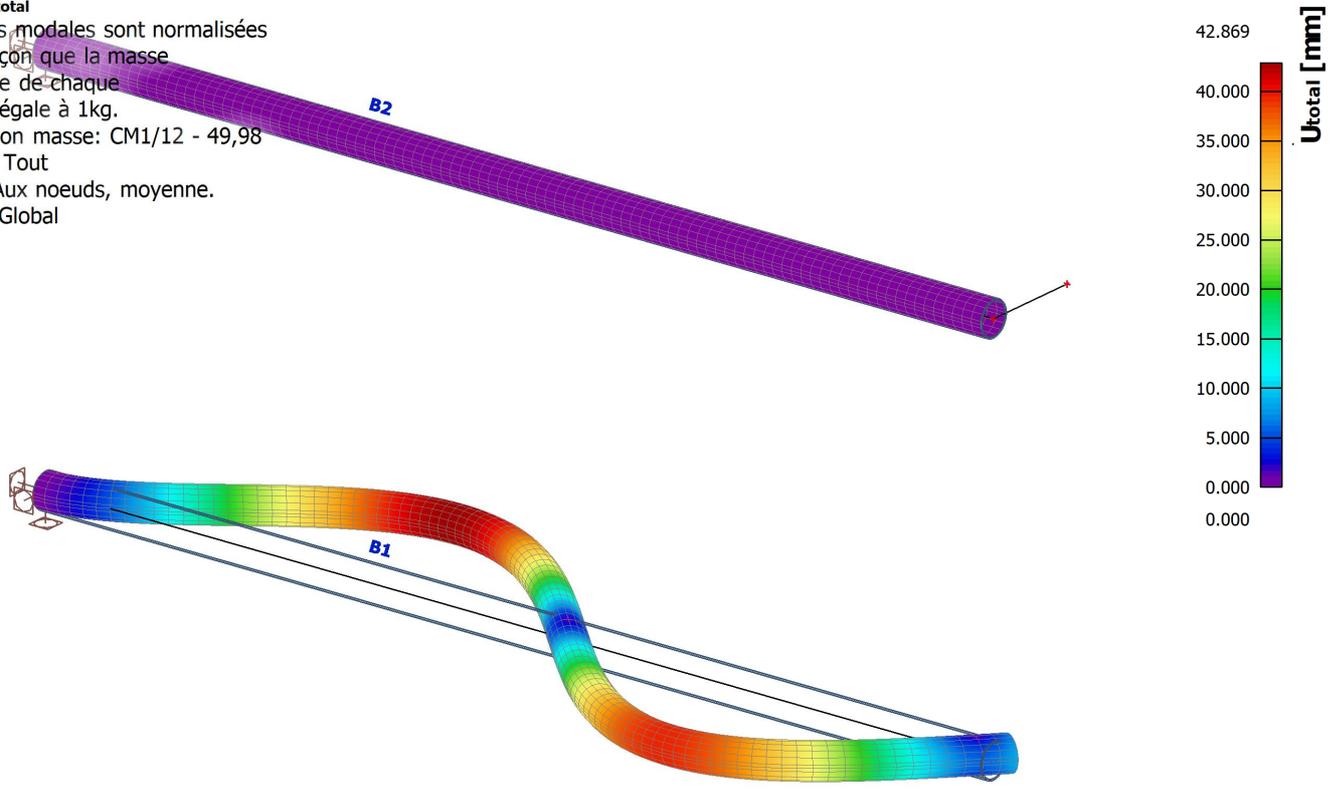
Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.

Combinaison masse: CM1/12 - 49,98

Sélection: Tout

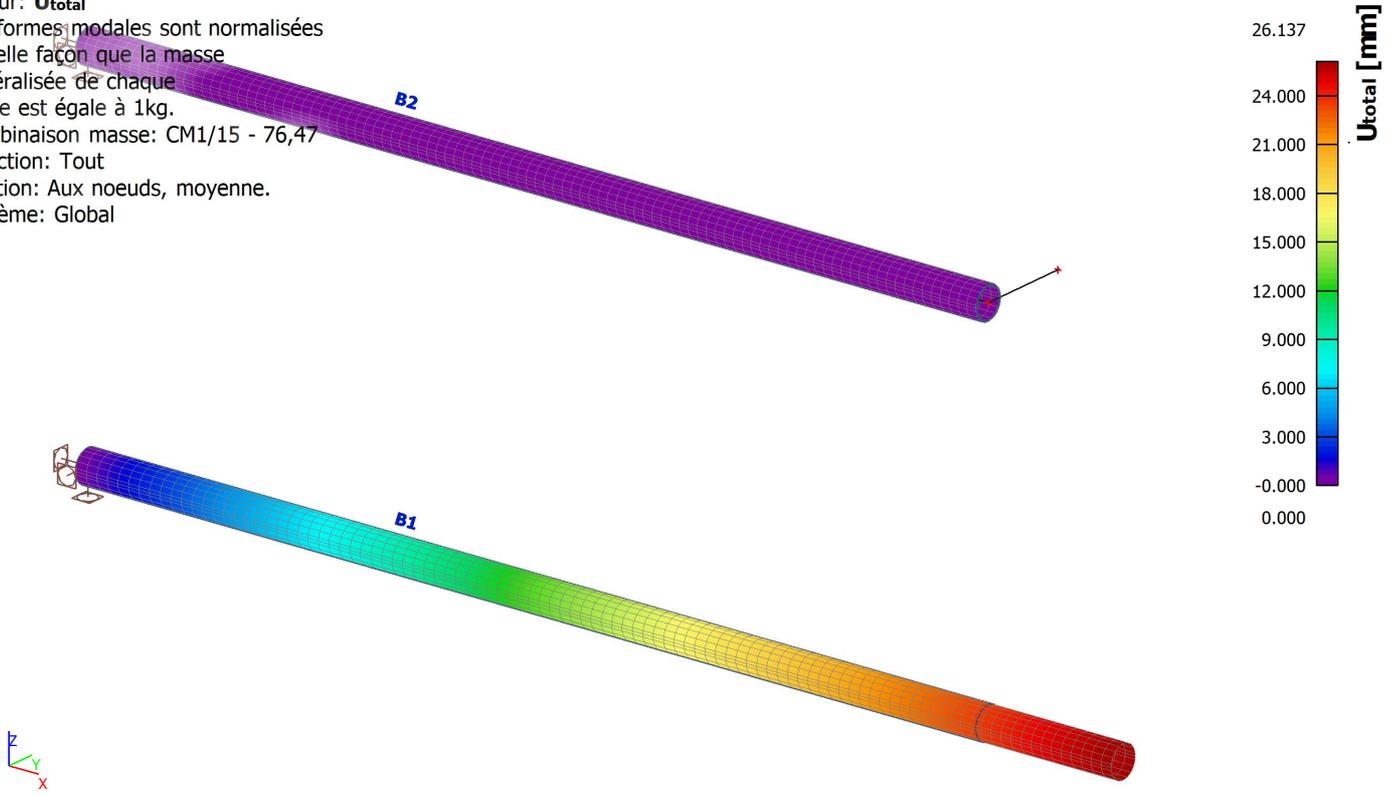
Position: Aux noeuds, moyenne.

Système: Global



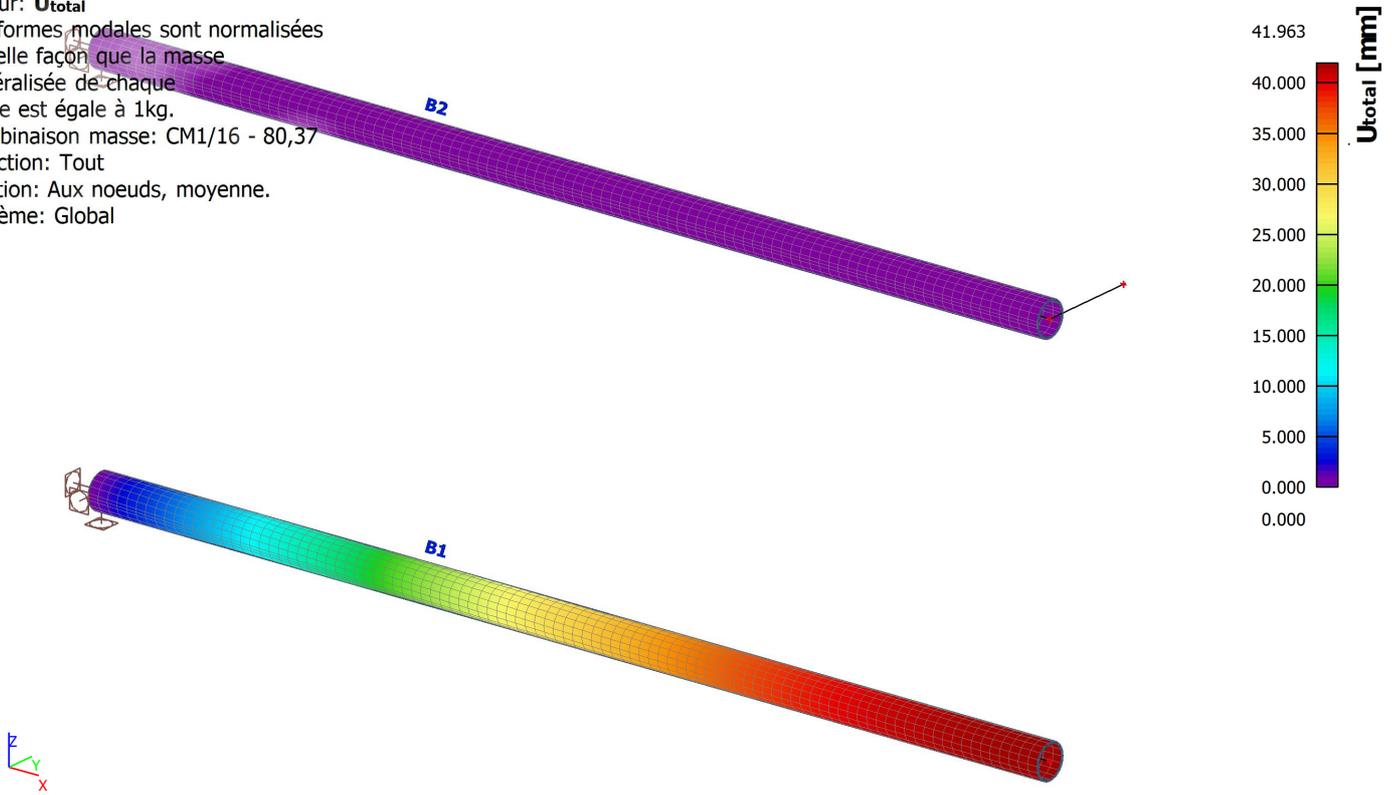
4.8. 3D displacement; Beam B1

Valeur: U_{total}
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/15 - 76,47
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



4.9. 3D displacement; Beam B1

Valeur: U_{total}
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/16 - 80,37
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



4.10. 3D displacement; Beam B1

Valeur: U_{total}

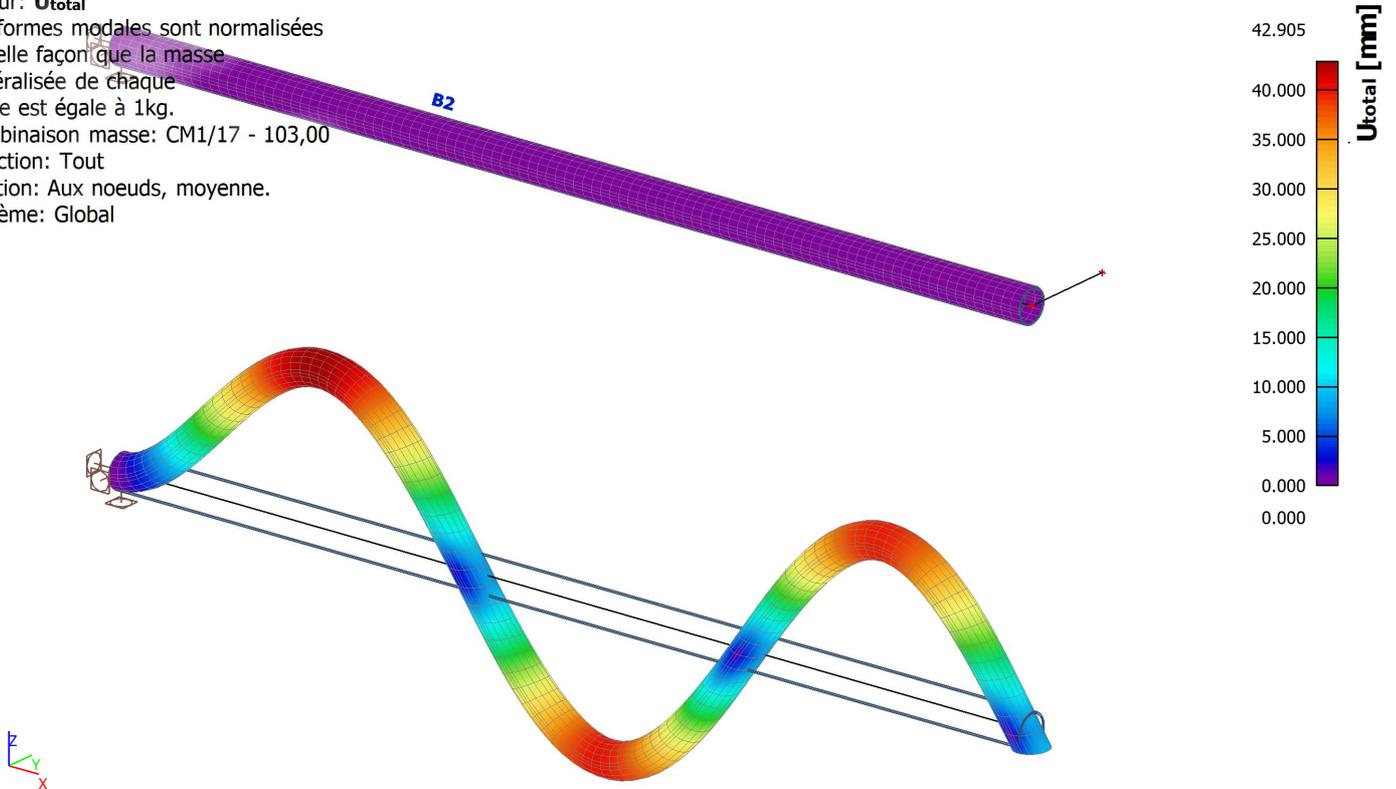
Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.

Combinaison masse: CM1/17 - 103,00

Sélection: Tout

Position: Aux noeuds, moyenne.

Système: Global



4.11. 3D displacement; Beam B1

Valeur: U_{total}

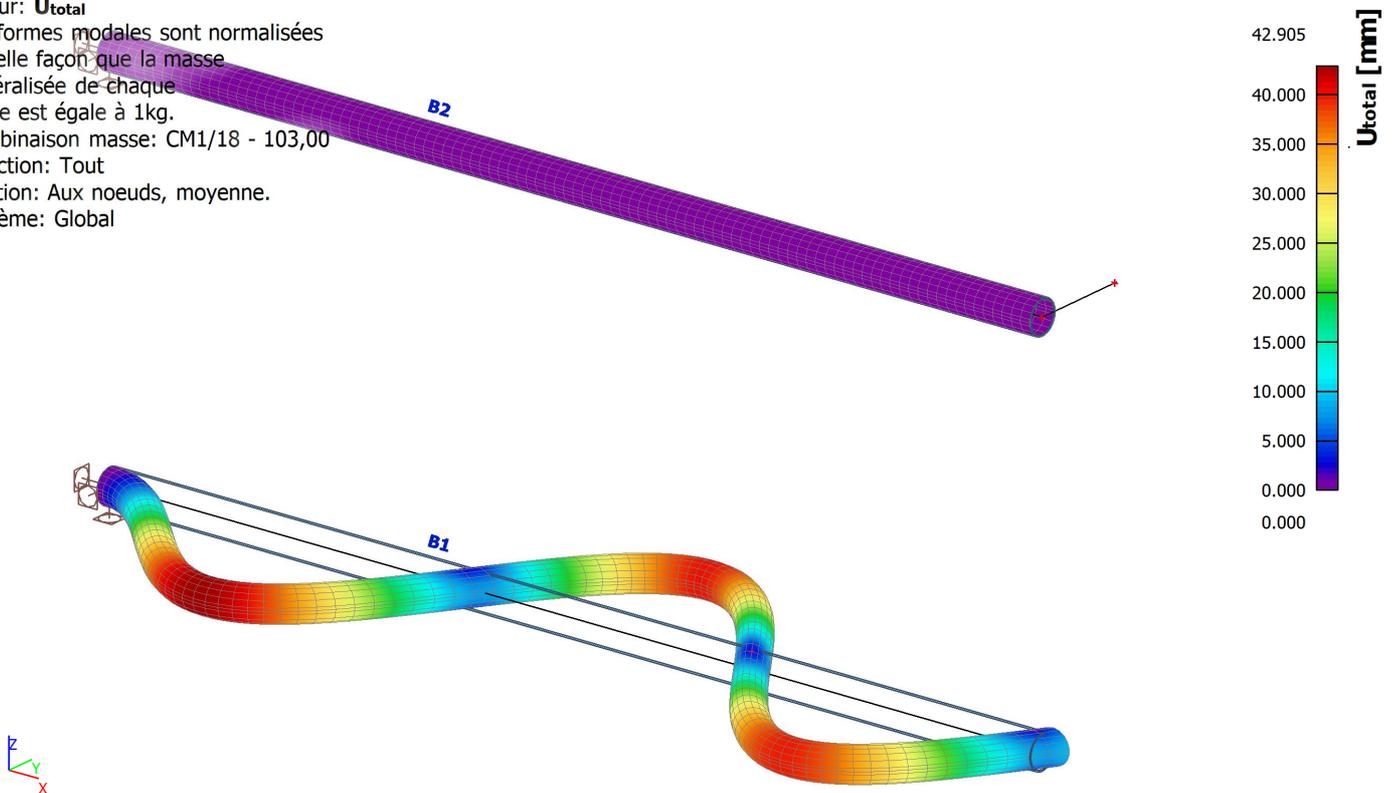
Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.

Combinaison masse: CM1/18 - 103,00

Sélection: Tout

Position: Aux noeuds, moyenne.

Système: Global



4.12. 3D displacement; Beam B2

Valeur: U_{total}

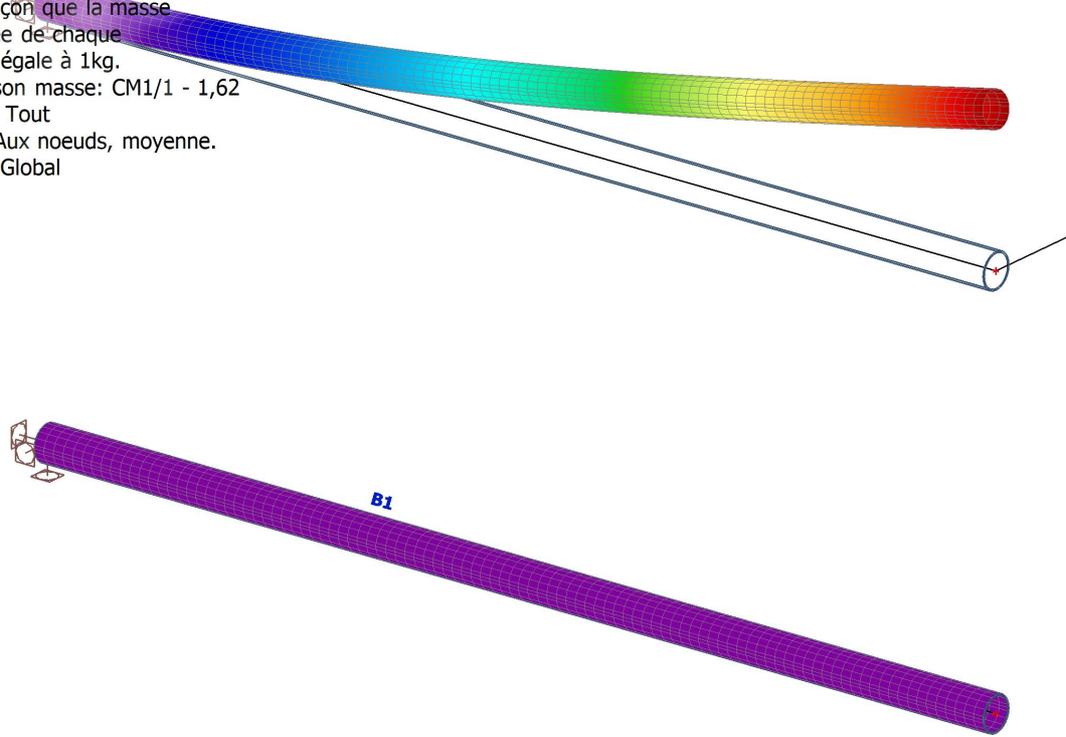
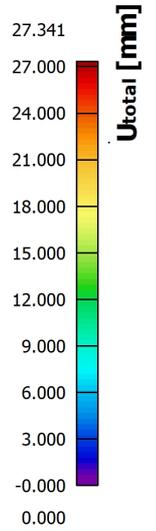
Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.

Combinaison masse: CM1/1 - 1,62

Sélection: Tout

Position: Aux noeuds, moyenne.

Système: Global



4.13. 3D displacement; Beam B2

Valeur: U_{total}

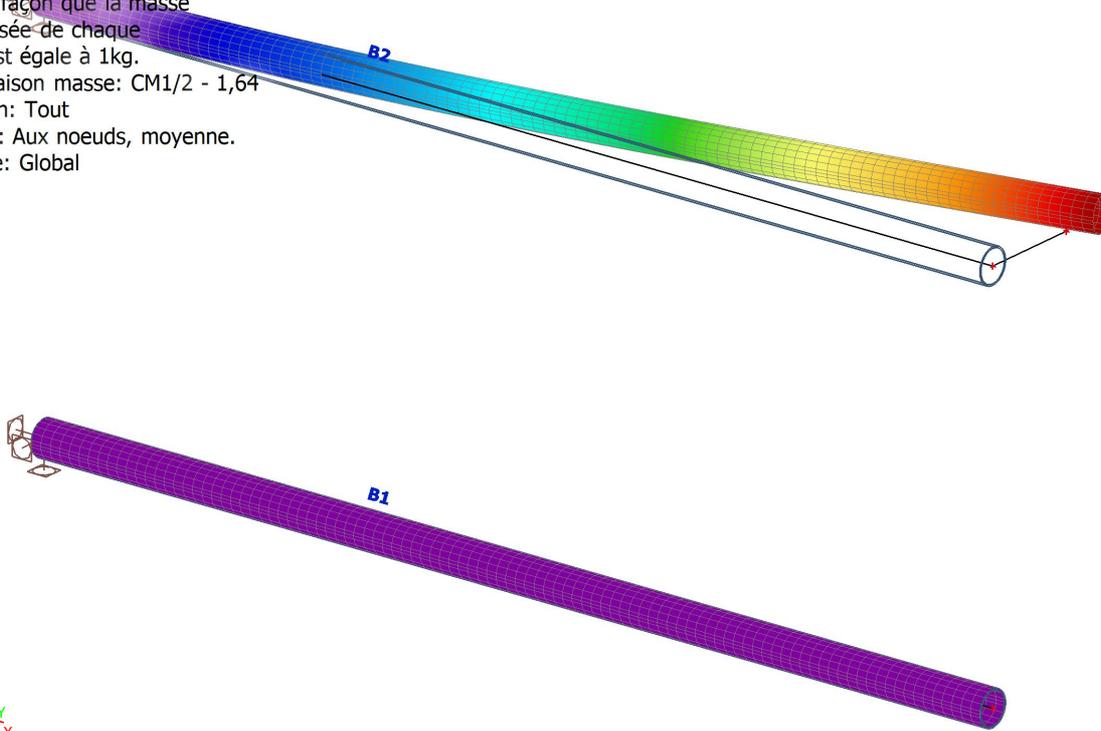
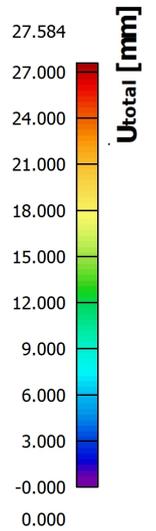
Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.

Combinaison masse: CM1/2 - 1,64

Sélection: Tout

Position: Aux noeuds, moyenne.

Système: Global



4.14. 3D displacement; Beam B2

Valeur: U_{total}

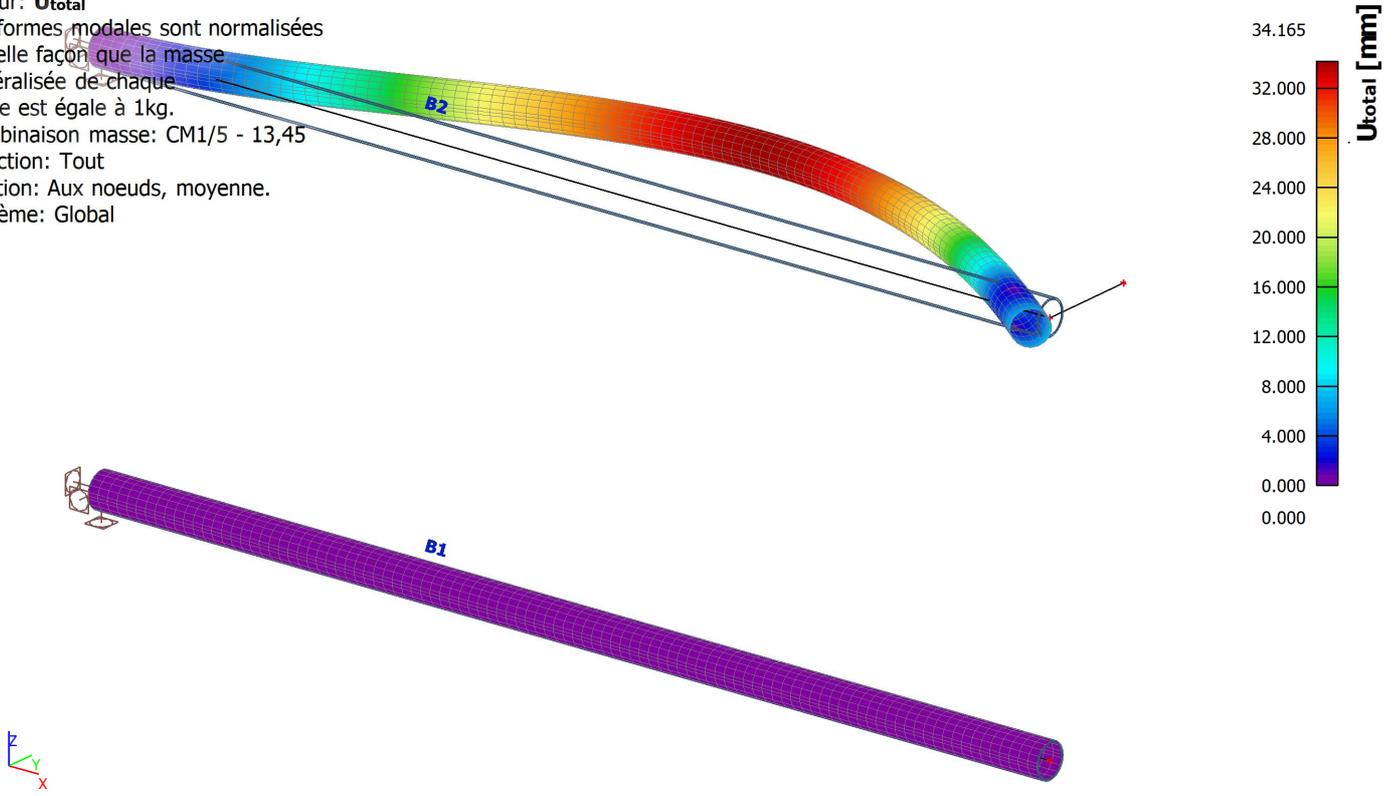
Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.

Combinaison masse: CM1/5 - 13,45

Sélection: Tout

Position: Aux noeuds, moyenne.

Système: Global



4.15. 3D displacement; Beam B2

Valeur: U_{total}

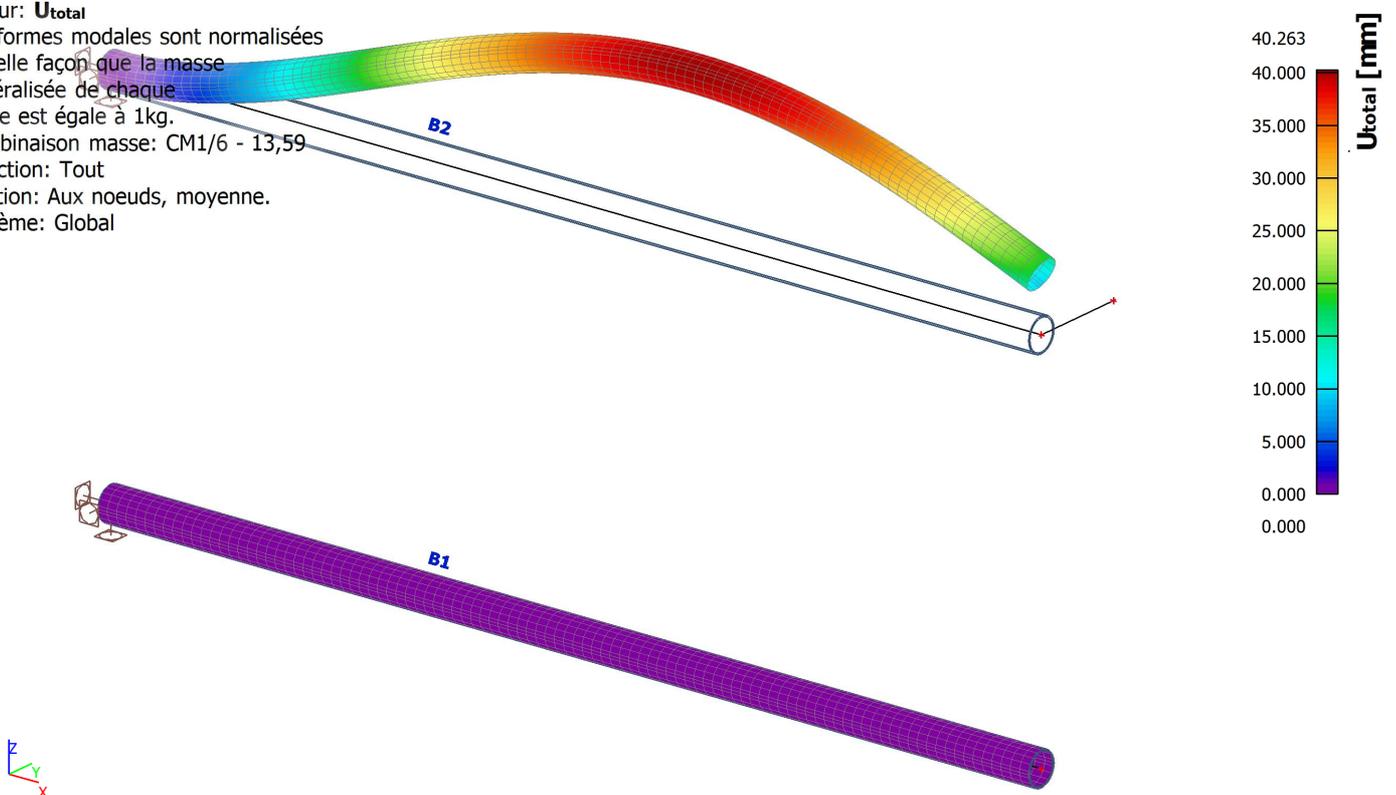
Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.

Combinaison masse: CM1/6 - 13,59

Sélection: Tout

Position: Aux noeuds, moyenne.

Système: Global



4.16. 3D displacement; Beam B2

Valeur: U_{total}

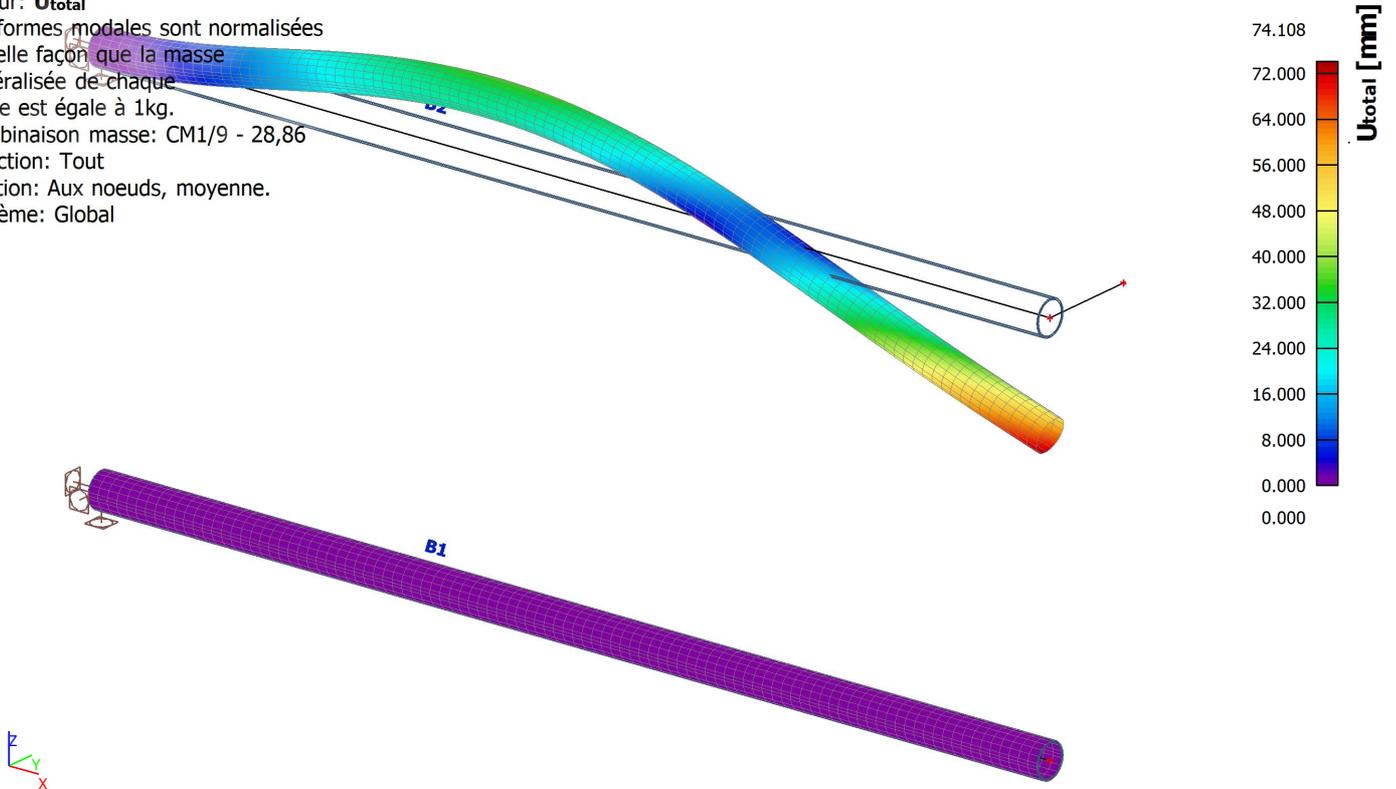
Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.

Combinaison masse: CM1/9 - 28,86

Sélection: Tout

Position: Aux noeuds, moyenne.

Système: Global



4.17. 3D displacement; Beam B2

Valeur: U_{total}

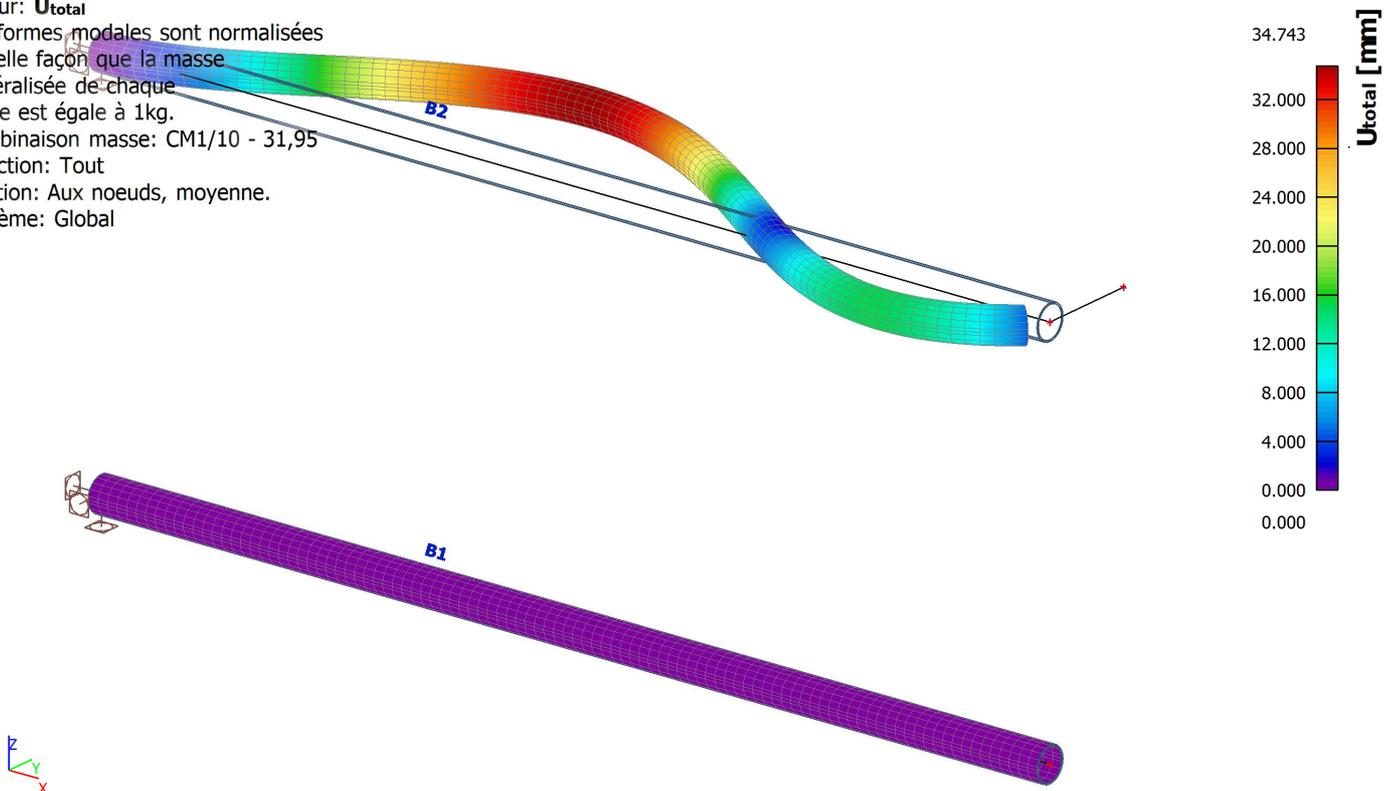
Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.

Combinaison masse: CM1/10 - 31,95

Sélection: Tout

Position: Aux noeuds, moyenne.

Système: Global



4.18. 3D displacement; Beam B2

Valeur: U_{total}

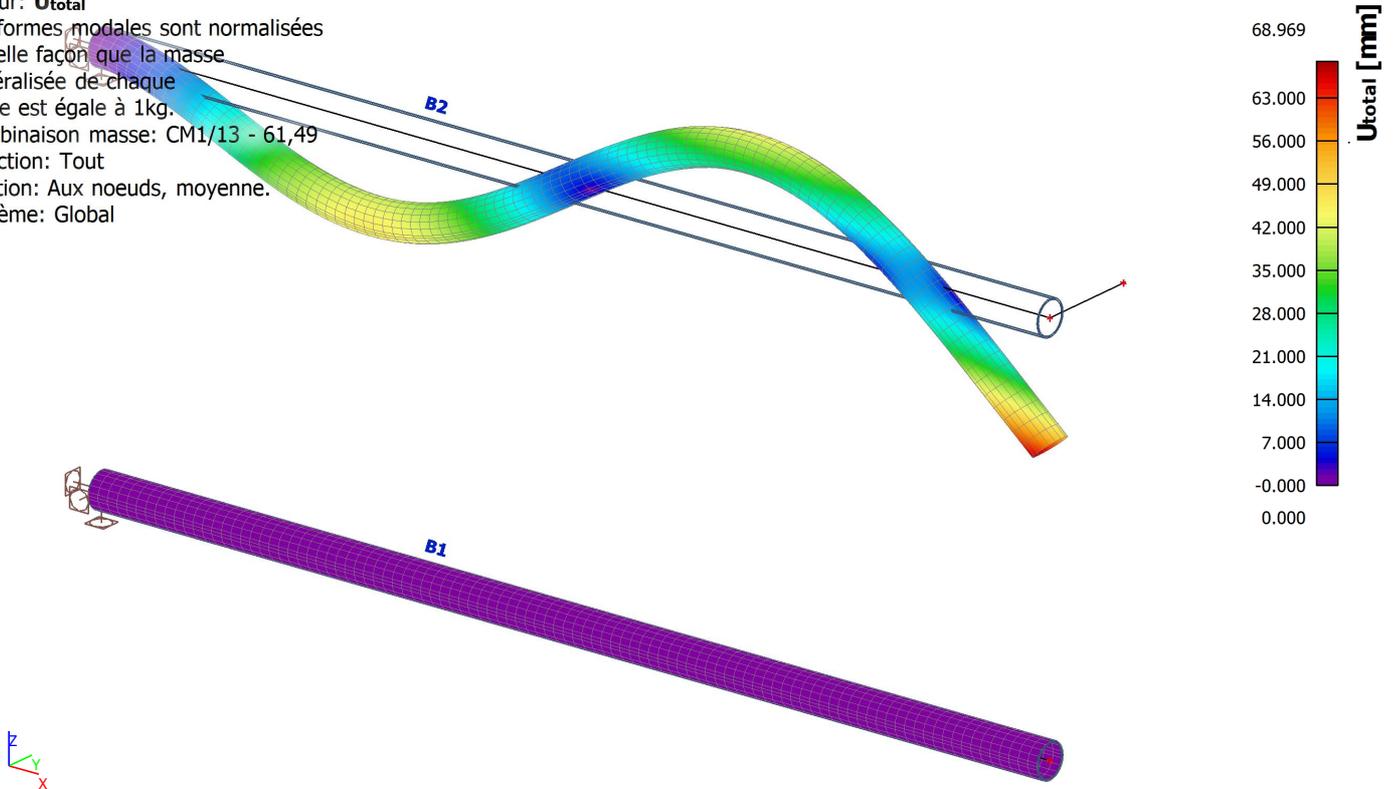
Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.

Combinaison masse: CM1/13 - 61,49

Sélection: Tout

Position: Aux noeuds, moyenne.

Système: Global



4.19. 3D displacement; Beam B2

Valeur: U_{total}

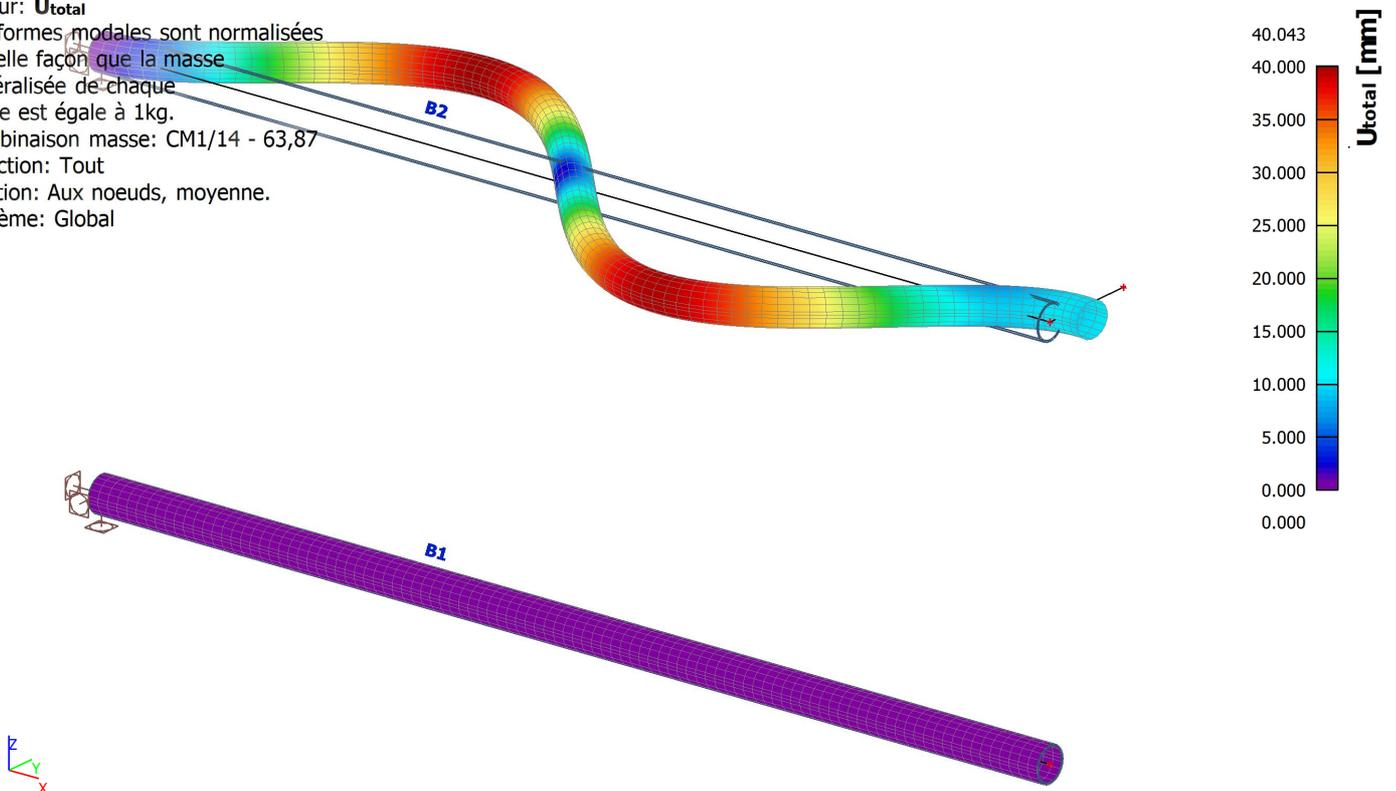
Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.

Combinaison masse: CM1/14 - 63,87

Sélection: Tout

Position: Aux noeuds, moyenne.

Système: Global



5. EXPECTED AFNOR RESULTS

Beam B1 (no eccentric mass):

Bendings 1 & 2 = 1.65 Hz

Bendings 3 & 4 = 16.07 Hz

Bendings 5 & 6 = 50.02 Hz

Tension 1 = 76.47 Hz

Torsion 1 = 80.47 Hz

Bendings 7 & 8 = 103.20

Beam B2 (with eccentric mass):

Bending + Torsion = 1.636 Hz

Bending + Tension = 1.642 Hz

Bending + Tension = 13.46 Hz

Bending + Torsion = 13.59 Hz

Bending + Torsion = 28.90 Hz

Bending + Tension = 31.96 Hz

Bending + Torsion = 61.61 Hz

Bending + Tension = 63.93 Hz

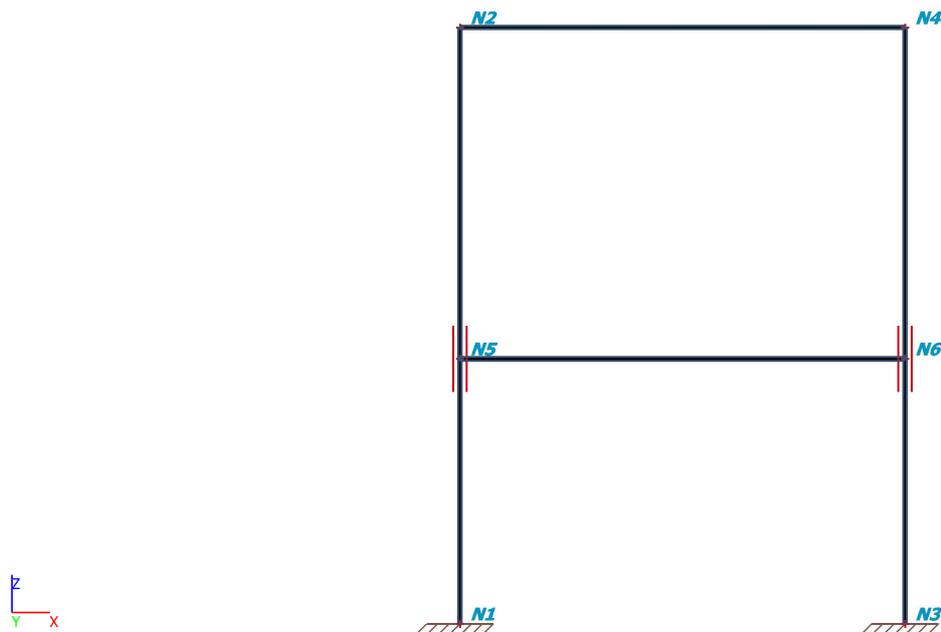
REFERENCE : "Guide de validation des progiciels de calcul de structures" AFNOR, 1990

1. TESTCASE DESCRIPTION

Modal analysis of a symmetric portal frame

2. MODEL

2.1. Analysis model



2.2. Nodes

| Name | Coord X [m] | Coord Z [m] | Member | Data |
|------|-------------|-------------|----------|------|
| N1 | -0,300 | 0,000 | B1 | Sn1 |
| N2 | -0,300 | 0,810 | B1 B3 | |
| N3 | 0,300 | 0,000 | B2 | Sn2 |

| Name | Coord X [m] | Coord Z [m] | Member | Data |
|------|-------------|-------------|----------|------|
| N4 | 0,300 | 0,810 | B2 B3 | |
| N5 | -0,300 | 0,360 | B1 B4 | |
| N6 | 0,300 | 0,360 | B2 B4 | |

2.3. Members

| Name | Cross-section | Material | Length [m] | Beg. node | End node | Type |
|------|---------------------------------------|----------|------------|-----------|----------|--------------|
| B1 | CS1 - Rectangulaire plein (4,8; 29,0) | S 235 | 0,810 | N1 | N2 | column (100) |
| B2 | CS1 - Rectangulaire plein (4,8; 29,0) | S 235 | 0,810 | N3 | N4 | column (100) |
| B3 | CS1 - Rectangulaire plein (4,8; 29,0) | S 235 | 0,600 | N2 | N4 | beam (80) |
| B4 | CS1 - Rectangulaire plein (4,8; 29,0) | S 235 | 0,600 | N5 | N6 | beam (80) |

2.4. Nodal supports

| Name | Node | System | Type | X | Z | Ry |
|------|------|--------|----------|-------|-------|-------|
| Sn1 | N1 | GCS | Standard | Rigid | Rigid | Rigid |
| Sn2 | N3 | GCS | Standard | Rigid | Rigid | Rigid |

2.5. Materials

Steel EC3

| Name | ρ [kg/m ³] | E_{mod} [MPa] | μ | Limit inférieure [mm] | Limite supérieure [mm] | F_y [MPa] | F_u [MPa] | Colour |
|-------|--------------------------------|--------------------|--------------------|--------------------------|---------------------------|----------------|----------------|--------|
| | | G_{mod} [MPa] | α [m/mK] | | | | | |
| S 235 | 7850,00 | 2,1000e+05 | 0.3 | 0,0 | 40,0 | 235,0 | 360,0 | ■ |
| | | 8,0769e+04 | 0,01e-003 | 40,0 | 80,0 | 215,0 | 360,0 | |

2.6. Cross-sections

| CS1 | | |
|--|------------------------------|------------|
| Type | Rectangulaire plein | |
| Detailed | 4,8; 29,0 | |
| Formcode | 7 - Full rectangular section | |
| Item material | S 235 | |
| A [m ²] | 1,3920e-04 | |
| A _y [m ²], A _z [m ²] | 1,1600e-04 | 1,1600e-04 |
| A _L [m ² /m], A _D [m ² /m] | 6,7600e-02 | 6,7600e-02 |
| C _{y,UCS} [mm], C _{z,UCS} [mm] | 14,5 | 2,4 |
| α [deg] | 0,00 | |
| I _y [m ⁴], I _z [m ⁴] | 2,6726e-10 | 9,7556e-09 |
| i _y [mm], i _z [mm] | 1,4 | 8,4 |
| W _{el,y} [m ³], W _{el,z} [m ³] | 1,1136e-07 | 6,7280e-07 |
| W _{pl,y} [m ³], W _{pl,z} [m ³] | 1,6704e-07 | 1,0092e-06 |
| M _{pl,y,+} [Nm], M _{pl,y,-} [Nm] | 39,25 | 39,25 |
| M _{pl,z,+} [Nm], M _{pl,z,-} [Nm] | 237,16 | 237,16 |
| d _y [mm], d _z [mm] | 0,0 | |
| I _t [m ⁴], I _w [m ⁶] | 9,5758e-10 | 0,0000e+00 |
| β_y [mm], β_z [mm] | 0,0 | |
| Picture | | |

3. LOAD and MASS

3.1. Mass groups

| Name | Load case |
|------|-------------------|
| MG1 | LC1 - Self weight |

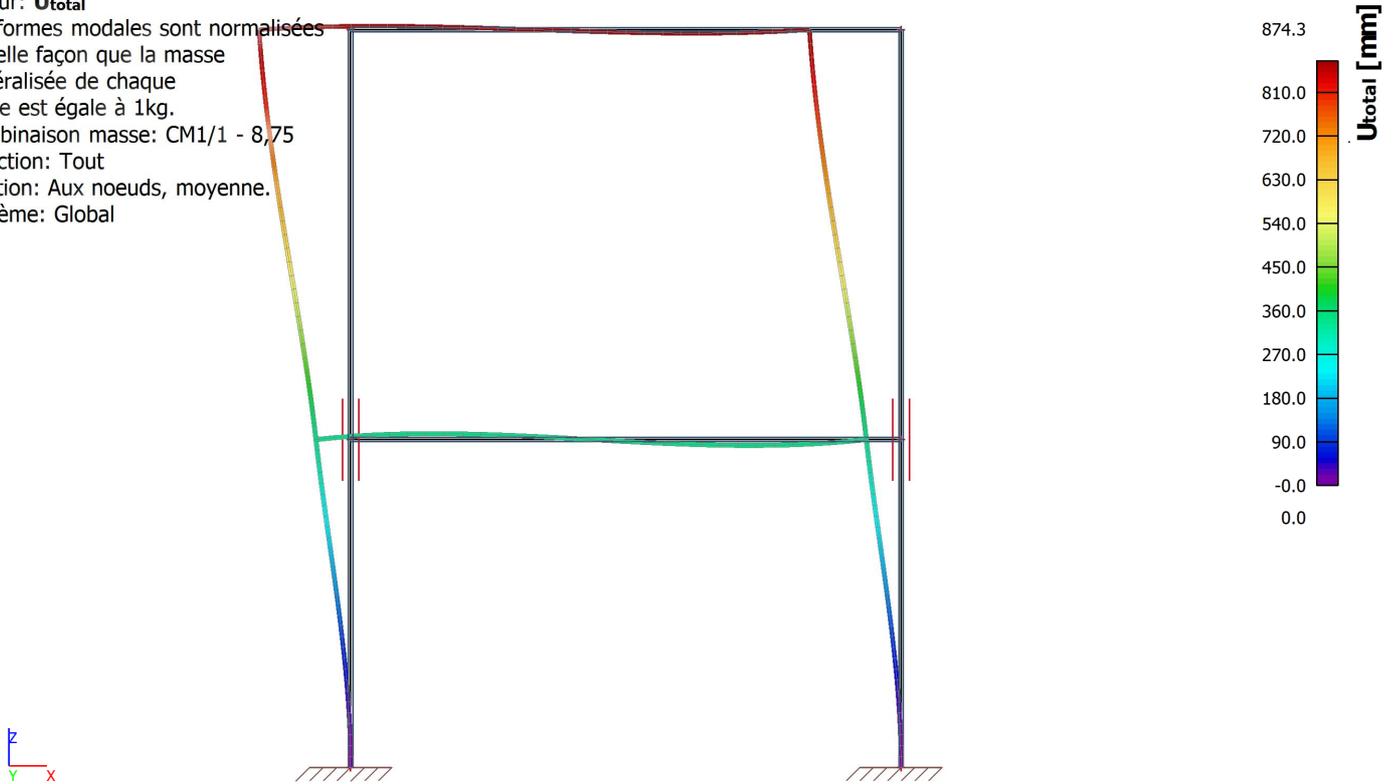
4. RESULTS

4.1. Eigen frequencies

| N | f [Hz] | ω [1/s] | ω^2 [1/s ²] | T [s] |
|-------------------------------|-----------|-------------------|-----------------------------------|----------|
| Mass combination : CM1 | | | | |
| 1 | 8,75 | 55,00 | 3024,66 | 0,11 |
| 2 | 29,34 | 184,37 | 33993,26 | 0,03 |
| 3 | 43,71 | 274,61 | 75412,58 | 0,02 |
| 4 | 56,12 | 352,61 | 124331,60 | 0,02 |
| 5 | 95,86 | 602,30 | 362770,46 | 0,01 |
| 6 | 102,37 | 643,18 | 413685,92 | 0,01 |
| 7 | 146,64 | 921,34 | 848863,44 | 0,01 |
| 8 | 174,39 | 1095,67 | 1200500,42 | 0,01 |
| 9 | 178,36 | 1120,61 | 1255760,55 | 0,01 |
| 10 | 205,58 | 1291,65 | 1668361,32 | 0,00 |
| 11 | 265,81 | 1670,09 | 2789205,97 | 0,00 |
| 12 | 319,35 | 2006,47 | 4025929,16 | 0,00 |
| 13 | 334,36 | 2100,79 | 4413307,87 | 0,00 |

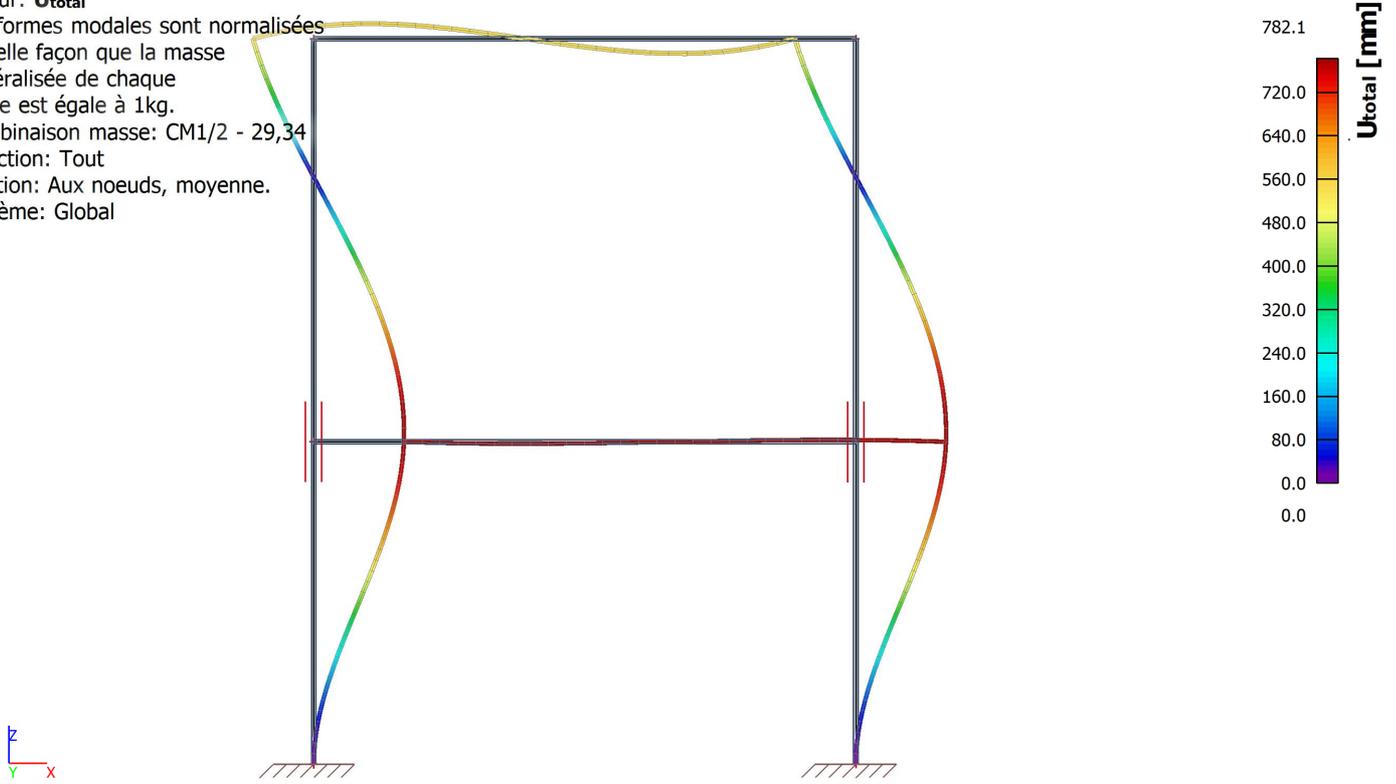
4.2. 3D displacement; U_{total}

Valeur: **U_{total}**
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/1 - 8,75
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



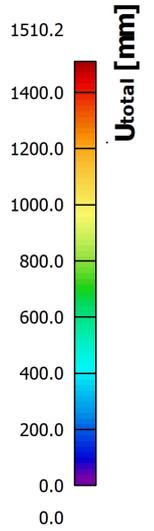
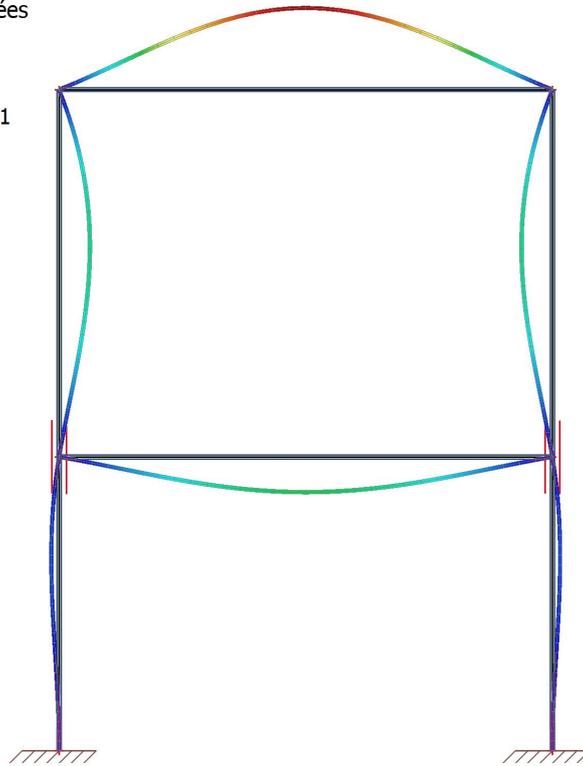
4.3. 3D displacement; U_{total}

Valeur: **U_{total}**
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/2 - 29,34
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



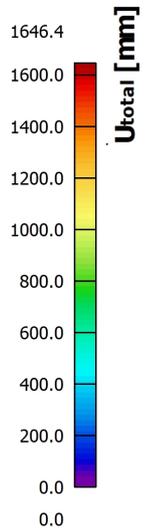
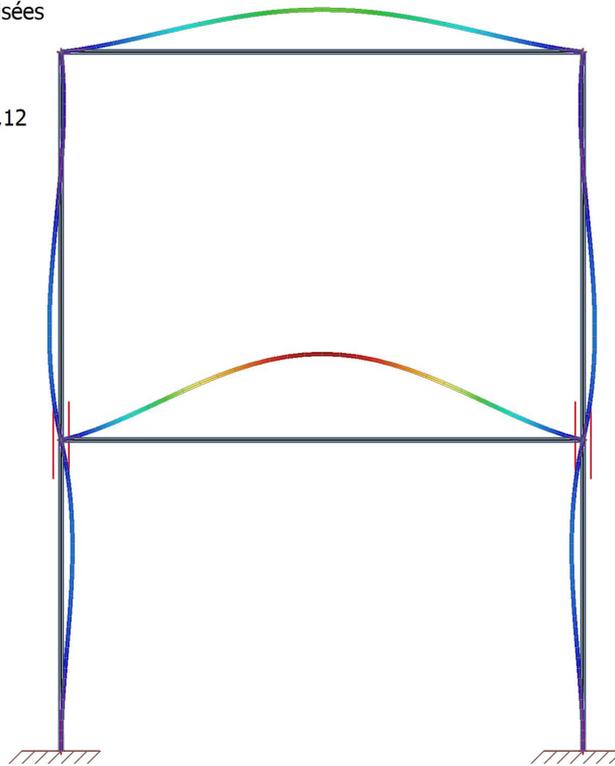
4.4. 3D displacement; U_{total}

Valeur: **U_{total}**
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/3 - 43,71
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



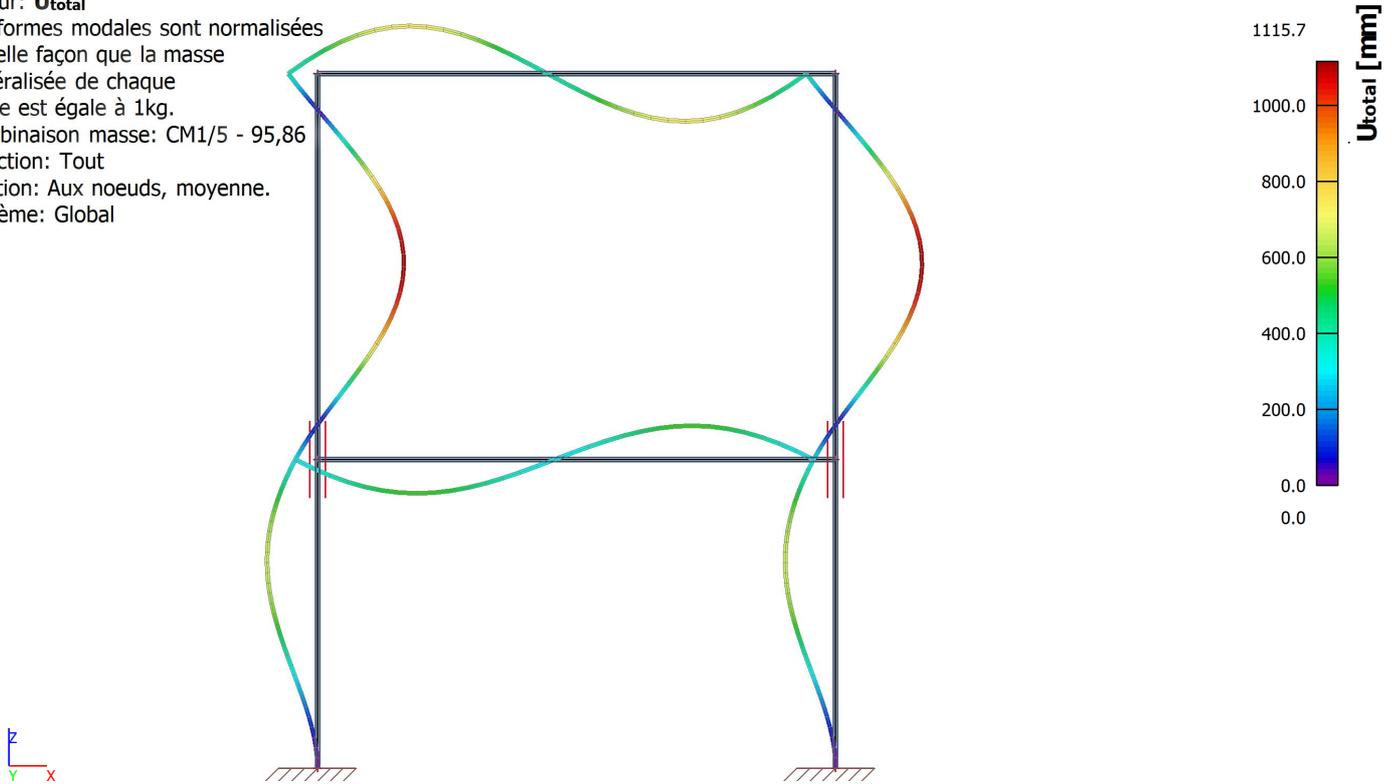
4.5. 3D displacement; U_{total}

Valeur: **U_{total}**
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/4 - 56,12
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



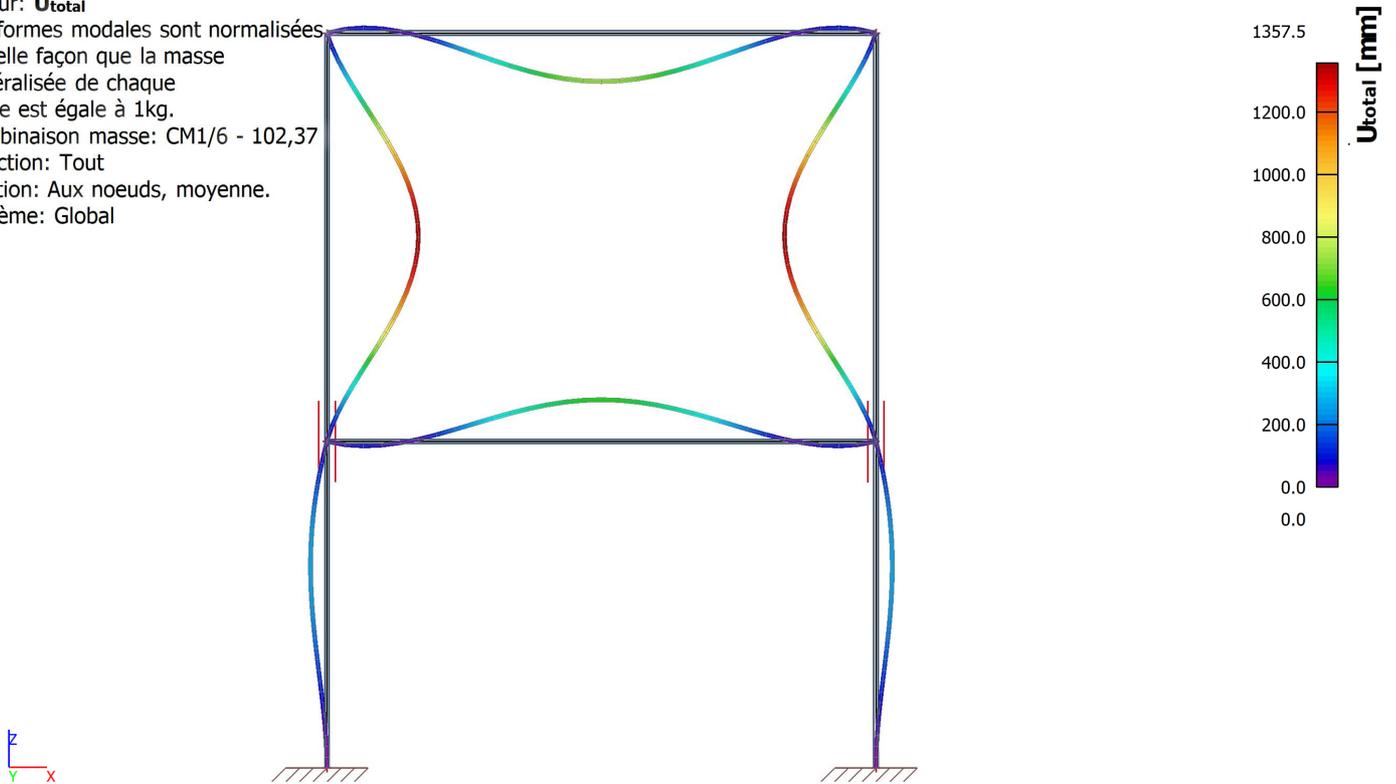
4.6. 3D displacement; U_{total}

Valeur: **U_{total}**
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/5 - 95,86
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



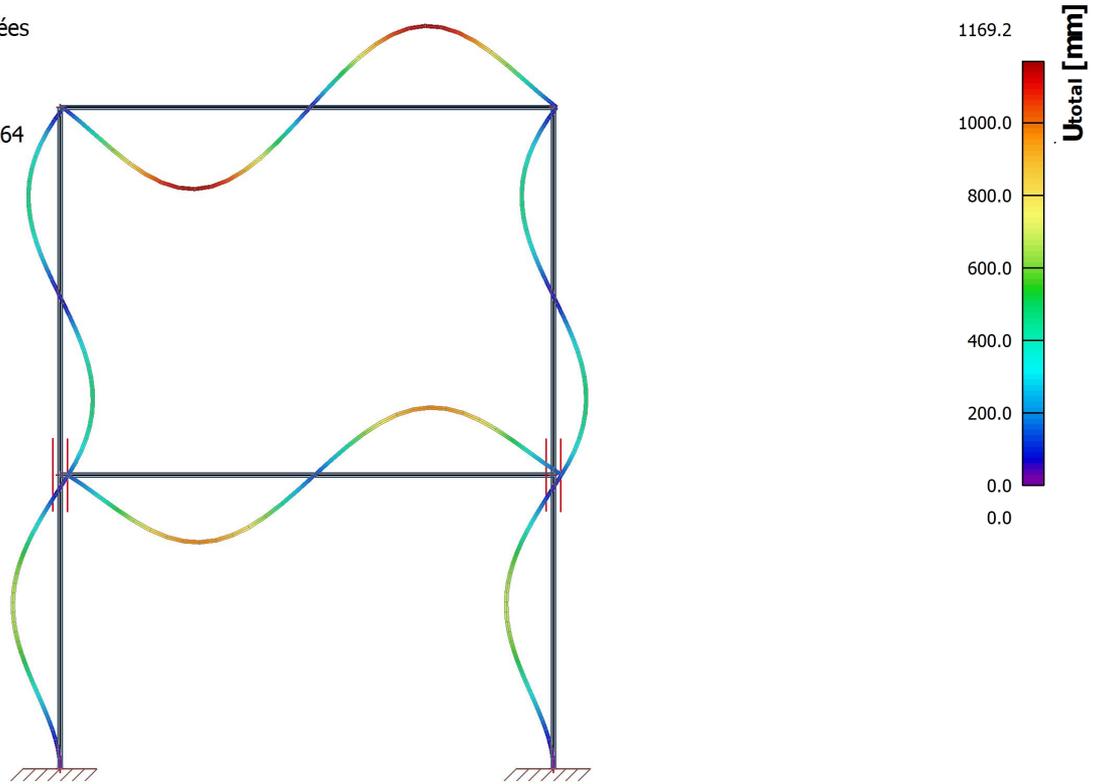
4.7. 3D displacement; U_{total}

Valeur: **U_{total}**
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/6 - 102,37
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



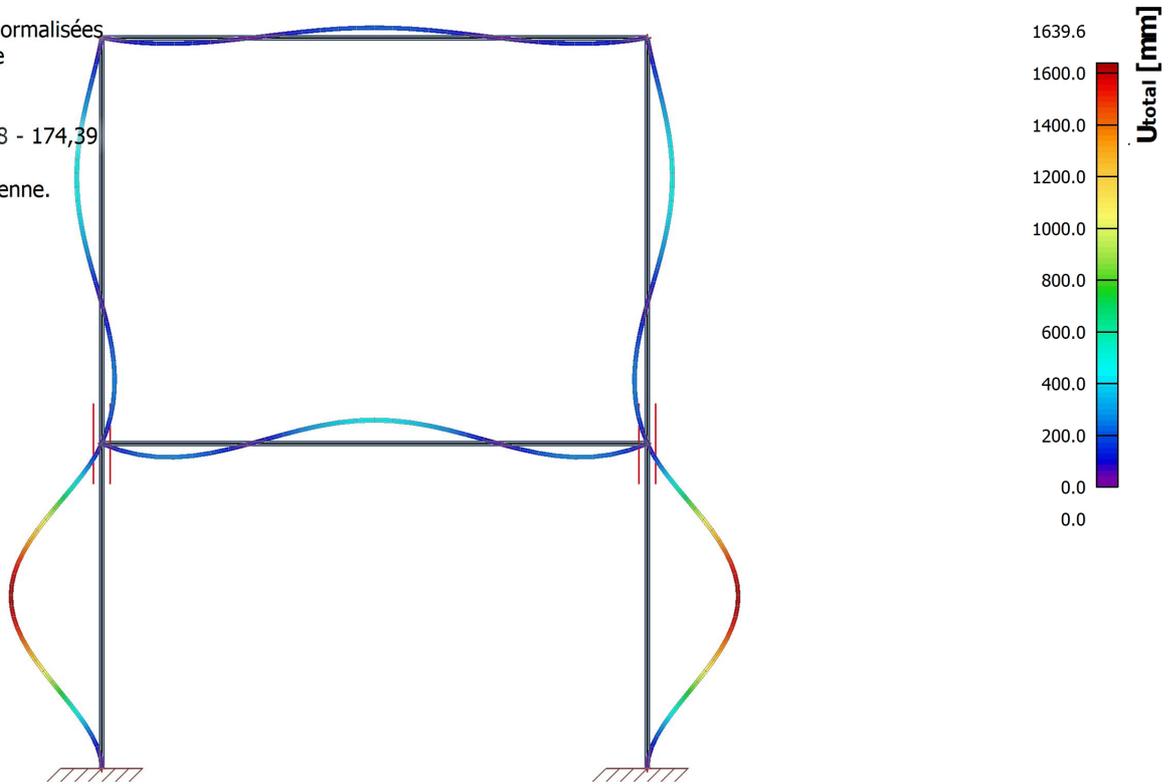
4.8. 3D displacement; U_{total}

Valeur: **U_{total}**
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/7 - 146,64
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



4.9. 3D displacement; U_{total}

Valeur: **U_{total}**
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/8 - 174,39
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



4.10. 3D displacement; U_{total}

Valeur: **U_{total}**

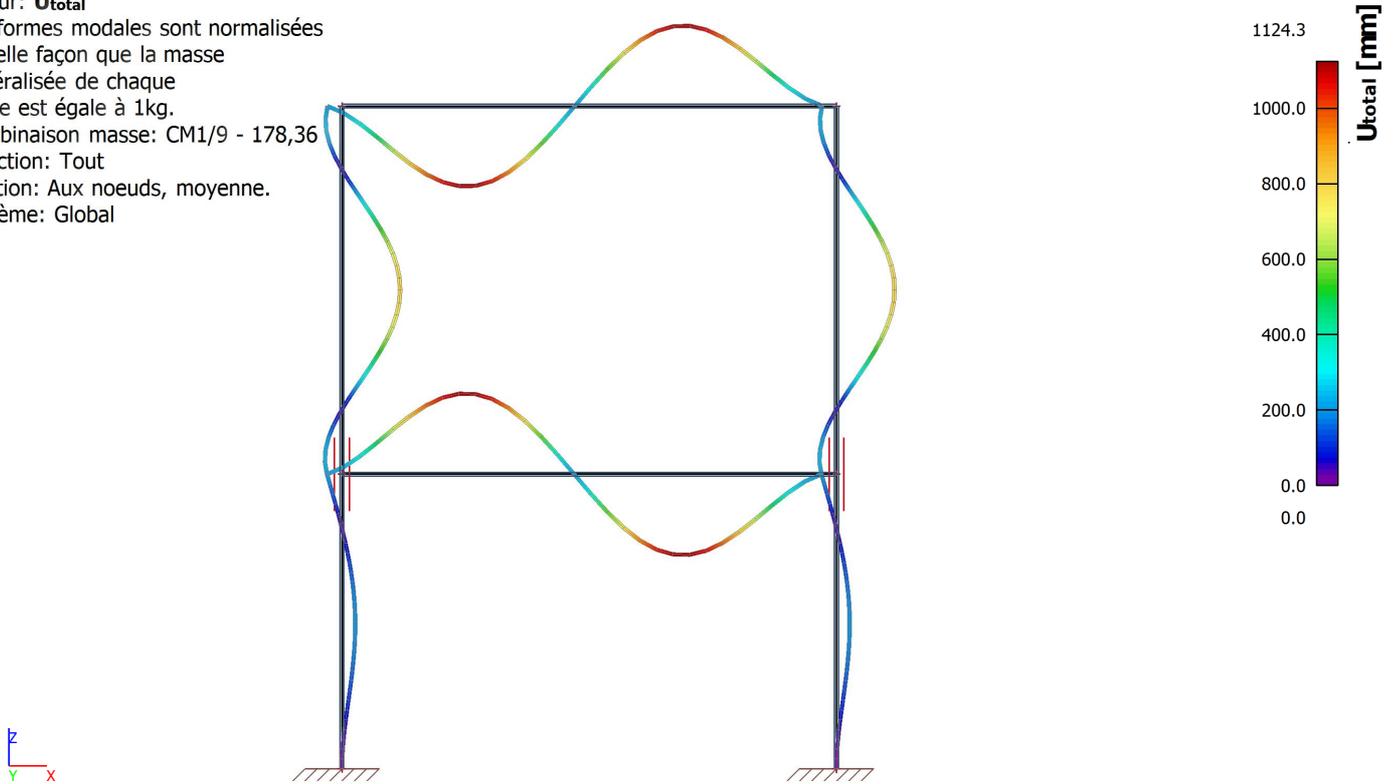
Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.

Combinaison masse: CM1/9 - 178,36

Sélection: Tout

Position: Aux noeuds, moyenne.

Système: Global



4.11. 3D displacement; U_{total}

Valeur: **U_{total}**

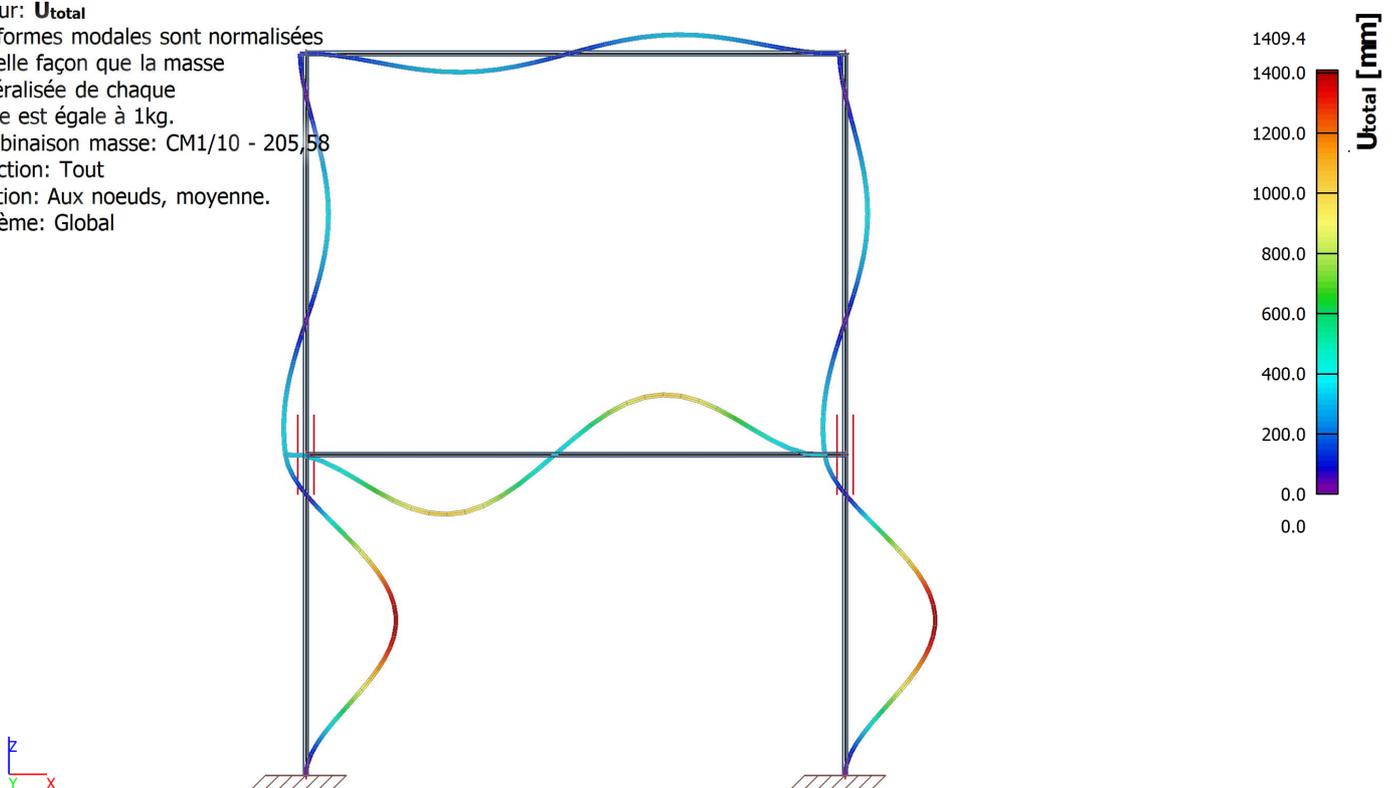
Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.

Combinaison masse: CM1/10 - 205,58

Sélection: Tout

Position: Aux noeuds, moyenne.

Système: Global



4.12. 3D displacement; U_{total}

Valeur: **U_{total}**

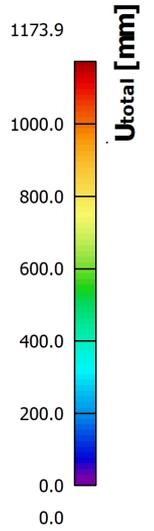
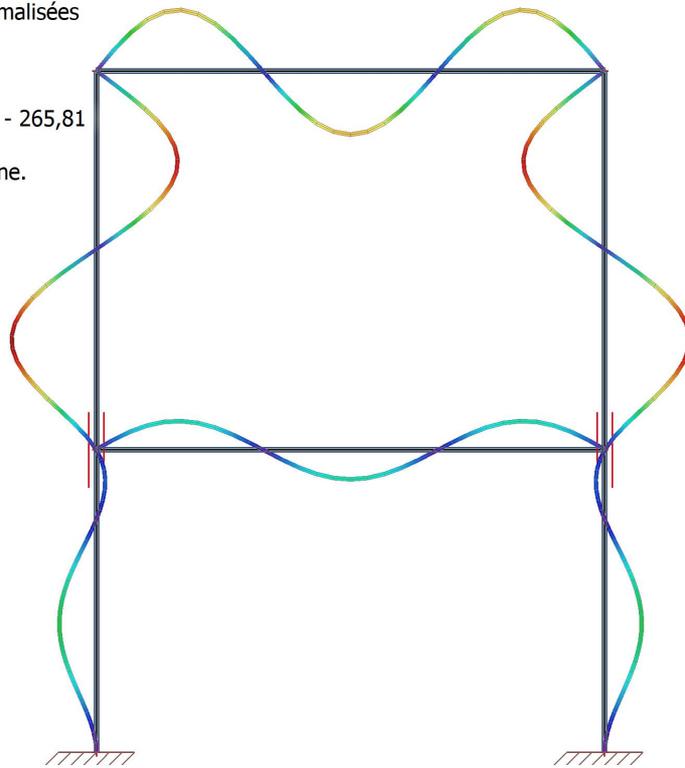
Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.

Combinaison masse: CM1/11 - 265,81

Sélection: Tout

Position: Aux noeuds, moyenne.

Système: Global



4.13. 3D displacement; U_{total}

Valeur: **U_{total}**

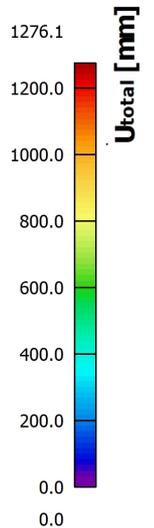
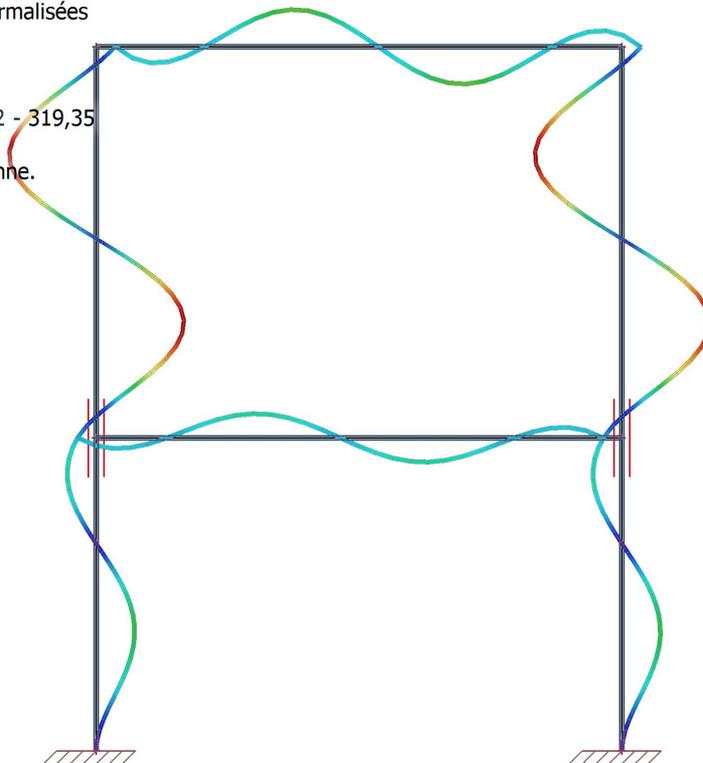
Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.

Combinaison masse: CM1/12 - 319,35

Sélection: Tout

Position: Aux noeuds, moyenne.

Système: Global



4.14. 3D displacement; U_total

Valeur: **U_{total}**

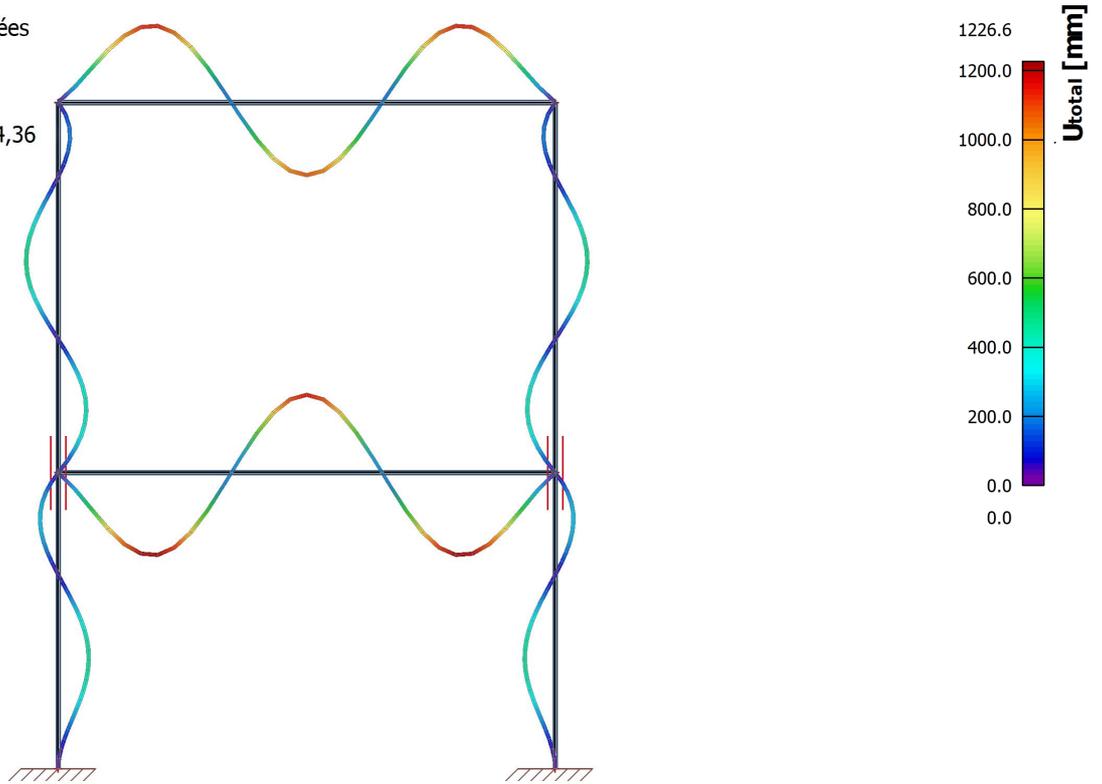
Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.

Combinaison masse: CM1/13 - 334,36

Sélection: Tout

Position: Aux noeuds, moyenne.

Système: Global



5. EXPECTED AFNOR RESULTS

Eigenfrequencies:

f1 = 8.8 Hz

f2 = 29.4 Hz

f3 = 43.8 Hz

f4 = 56.3 Hz

f5 = 96.2 Hz

f6 = 102.6 Hz

f7 = 147.1 Hz

f8 = 174.8 Hz

f9 = 178.8 Hz

f10 = 206.0 Hz

f11 = 266.4 Hz

f12 = 320.0 Hz

f13 = 335.0 Hz

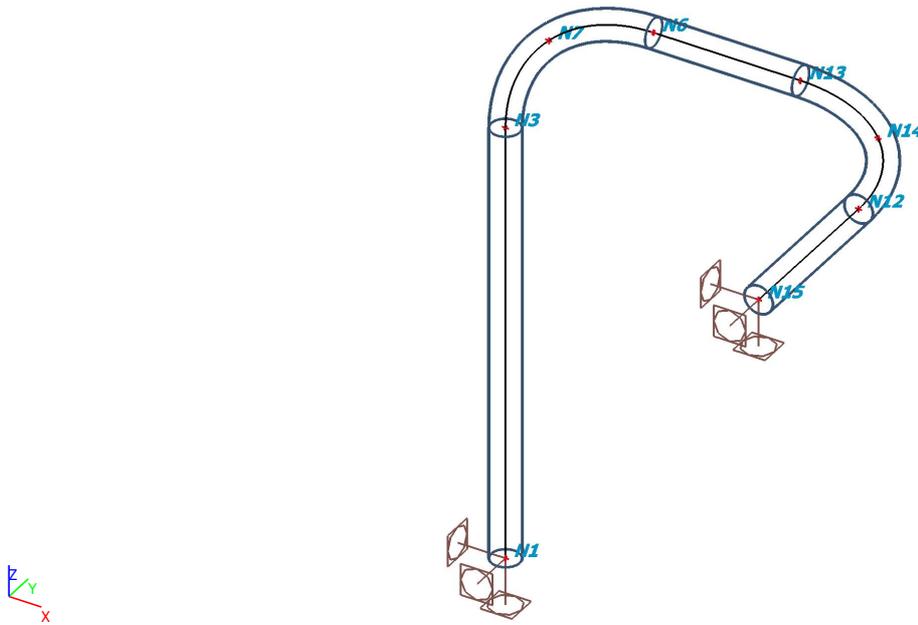
REFERENCE : "Guide de validation des progiciels de calcul de structures" AFNOR, 1990

1. TESTCASE DESCRIPTION

Hovgaard problem - Modal analysis of a pipe

2. MODEL

2.1. Analysis model



2.2. Nodes

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] | Member | Data |
|------|-------------|-------------|-------------|----------|------|
| N1 | -2,750 | 0,000 | -3,690 | B1 | Sn2 |
| N3 | -2,750 | 0,000 | -0,922 | B1 B5 | |
| N6 | -1,828 | 0,000 | 0,000 | B3 B5 | |
| N7 | -2,480 | 0,000 | -0,270 | B5 | |

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] | Member | Data |
|------|-------------|-------------|-------------|----------|------|
| N12 | 0,000 | -0,922 | 0,000 | B7 B9 | |
| N13 | -0,914 | 0,000 | 0,000 | B3 B9 | |
| N14 | -0,267 | -0,273 | 0,000 | B9 | |
| N15 | 0,000 | -1,960 | 0,000 | B7 | Sn1 |

2.3. Members

| Name | Cross-section | Material | Length [m] | Beg. node | End node | Type |
|------|-------------------------|----------|------------|-----------|----------|--------------|
| B1 | CS1 - Tube (185,0; 6,1) | Material | 2,768 | N1 | N3 | column (100) |
| B3 | CS1 - Tube (185,0; 6,1) | Material | 0,914 | N6 | N13 | beam (80) |
| B5 | CS1 - Tube (185,0; 6,1) | Material | 1,448 | N6 | N3 | beam (80) |
| B7 | CS1 - Tube (185,0; 6,1) | Material | 1,038 | N12 | N15 | beam (80) |
| B9 | CS1 - Tube (185,0; 6,1) | Material | 1,440 | N12 | N13 | beam (80) |

2.4. Nodal supports

| Name | Node | System | Type | X | Y | Z | Rx | Ry | Rz |
|------|------|--------|----------|-------|-------|-------|-------|-------|-------|
| Sn1 | N15 | GCS | Standard | Rigid | Rigid | Rigid | Rigid | Rigid | Rigid |
| Sn2 | N1 | GCS | Standard | Rigid | Rigid | Rigid | Rigid | Rigid | Rigid |

2.5. Materials

Steel EC3

| Name | ρ [kg/m ³] | E_{mod} [MPa] | μ | Limite inférieure [mm] | Limite supérieure [mm] | F_y [MPa] | F_u [MPa] | Colour |
|----------|--------------------------------|--------------------|--------------------|---------------------------|---------------------------|----------------|----------------|--------|
| | | G_{mod} [MPa] | α [m/mK] | | | | | |
| Material | 13404,11 | 1,6580e+05 | 0.3 | 0,0 | 40,0 | 235,0 | 360,0 | ■ |
| | | 6,3769e+04 | 0,01e-003 | 40,0 | 80,0 | 215,0 | 360,0 | |

2.6. Cross-sections

| CS1 | | |
|--|------------|------------|
| Type | Tube | |
| Detailed | 185,0; 6,1 | |
| Item material | Material | |
| A [m ²] | 3,4392e-03 | |
| A _y [m ²], A _z [m ²] | 2,1895e-03 | 2,1895e-03 |
| A _L [m ² /m], A _D [m ² /m] | 5,8117e-01 | 1,1239e+00 |
| c _{y,UCS} [mm], c _{z,UCS} [mm] | 92,5 | 92,5 |
| α [deg] | 0,00 | |
| I _y [m ⁴], I _z [m ⁴] | 1,3772e-05 | 1,3772e-05 |
| i _y [mm], i _z [mm] | 63,3 | 63,3 |
| W _{el,y} [m ³], W _{el,z} [m ³] | 1,4889e-04 | 1,4889e-04 |
| W _{pl,y} [m ³], W _{pl,z} [m ³] | 1,9590e-04 | 1,9590e-04 |
| M _{pl,y,+} [Nm], M _{pl,y,-} [Nm] | 46023,54 | 46023,54 |
| M _{pl,z,+} [Nm], M _{pl,z,-} [Nm] | 46023,54 | 46023,54 |
| d _y [mm], d _z [mm] | 0,0 | 0,0 |
| I _t [m ⁴], I _w [m ⁶] | 2,7512e-05 | 0,0000e+00 |
| β_y [mm], β_z [mm] | 0,0 | 0,0 |
| Picture | | |

3. LOAD and MASS

3.1. Mass groups

| Name | Load case |
|------|--------------------|
| MG1 | LC1 - Poids propre |

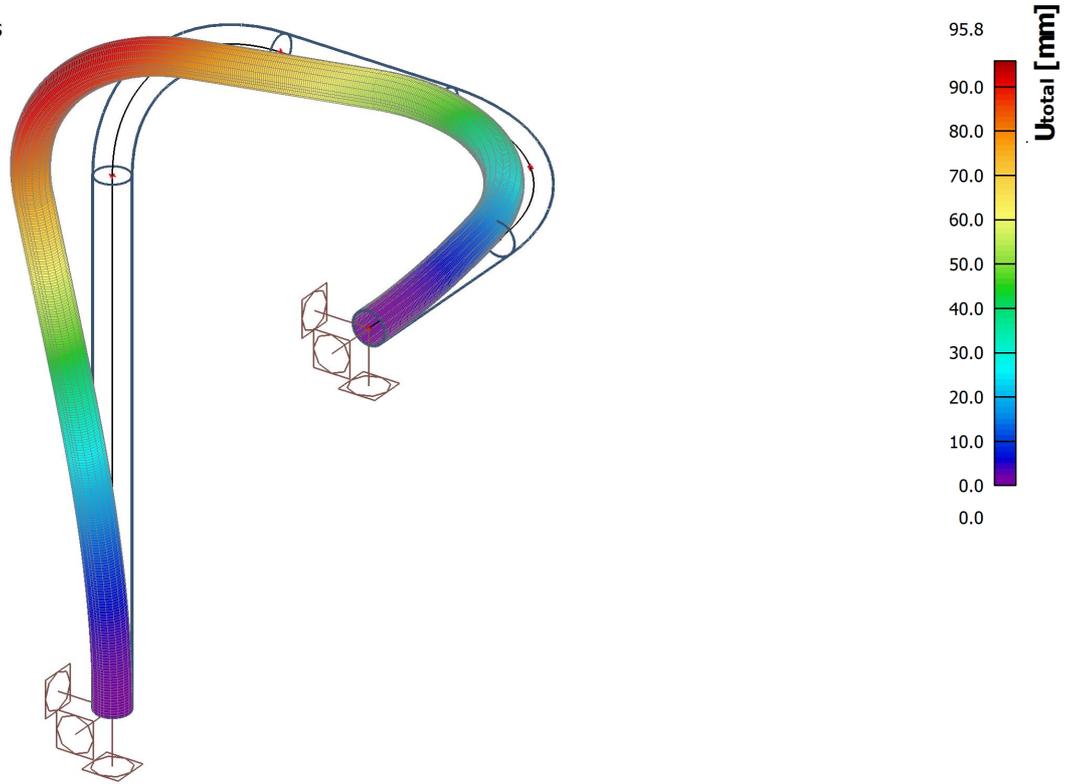
4. RESULTS

4.1. Eigen frequencies

| N | f [Hz] | ω [1/s] | ω^2 [1/s ²] | T [s] |
|-------------------------------|-----------|-------------------|-----------------------------------|----------|
| Mass combination : CM1 | | | | |
| 1 | 11,20 | 70,34 | 4948,03 | 0,09 |
| 2 | 23,02 | 144,64 | 20920,07 | 0,04 |
| 3 | 27,99 | 175,85 | 30924,81 | 0,04 |
| 4 | 52,66 | 330,85 | 109460,61 | 0,02 |
| 5 | 57,91 | 363,87 | 132399,78 | 0,02 |
| 6 | 92,77 | 582,84 | 339707,56 | 0,01 |
| 7 | 97,27 | 611,14 | 373492,37 | 0,01 |
| 8 | 149,03 | 936,35 | 876746,12 | 0,01 |
| 9 | 152,80 | 960,07 | 921737,82 | 0,01 |

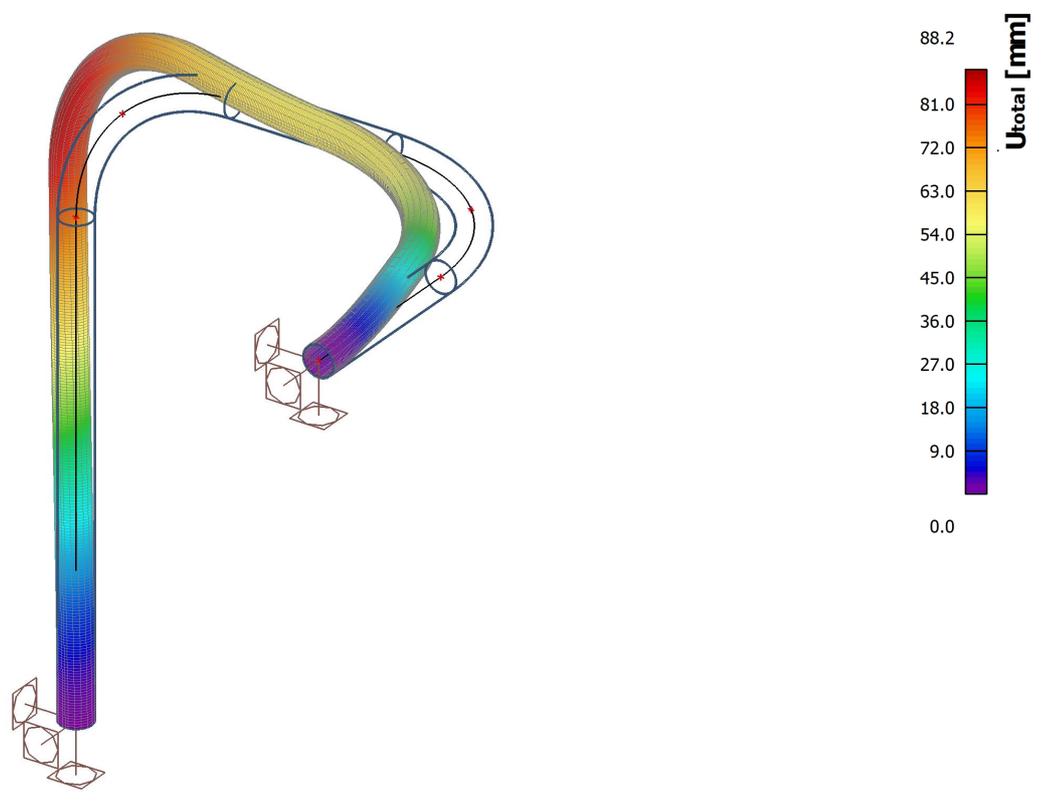
4.2. 3D displacement; U_{total}

Valeur: **U_{total}**
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/1 - 11,20
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



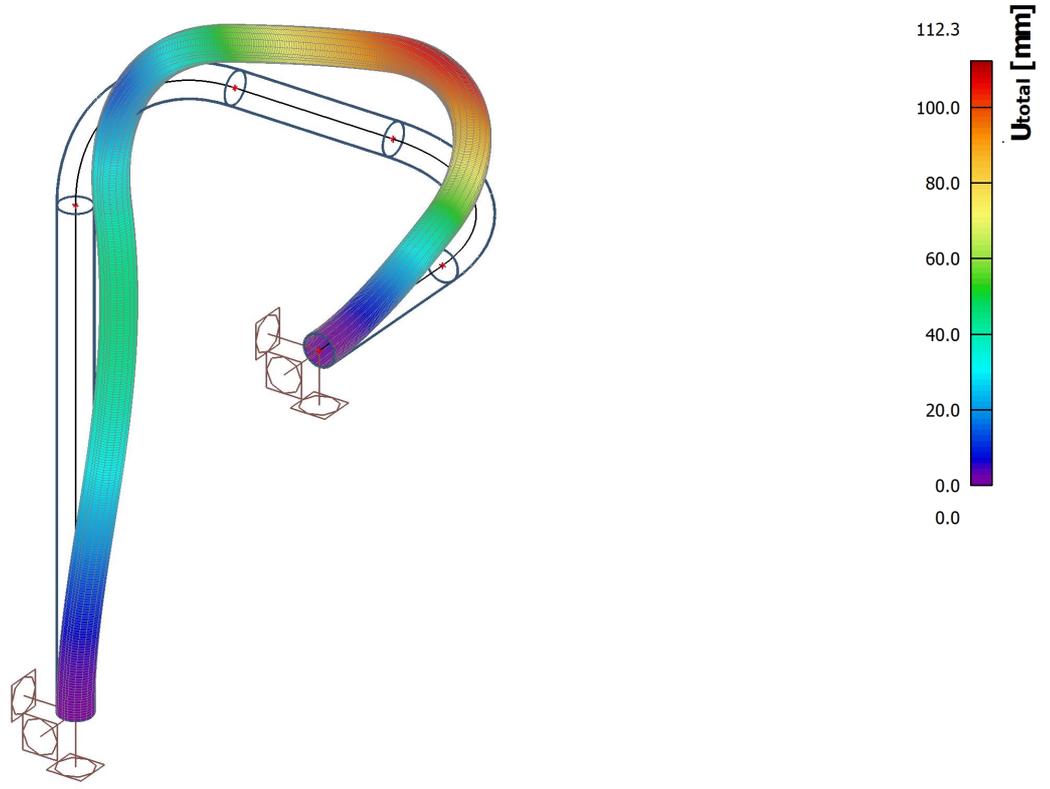
4.3. 3D displacement; U_{total}

Valeur: **U_{total}**
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/2 - 23,02
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



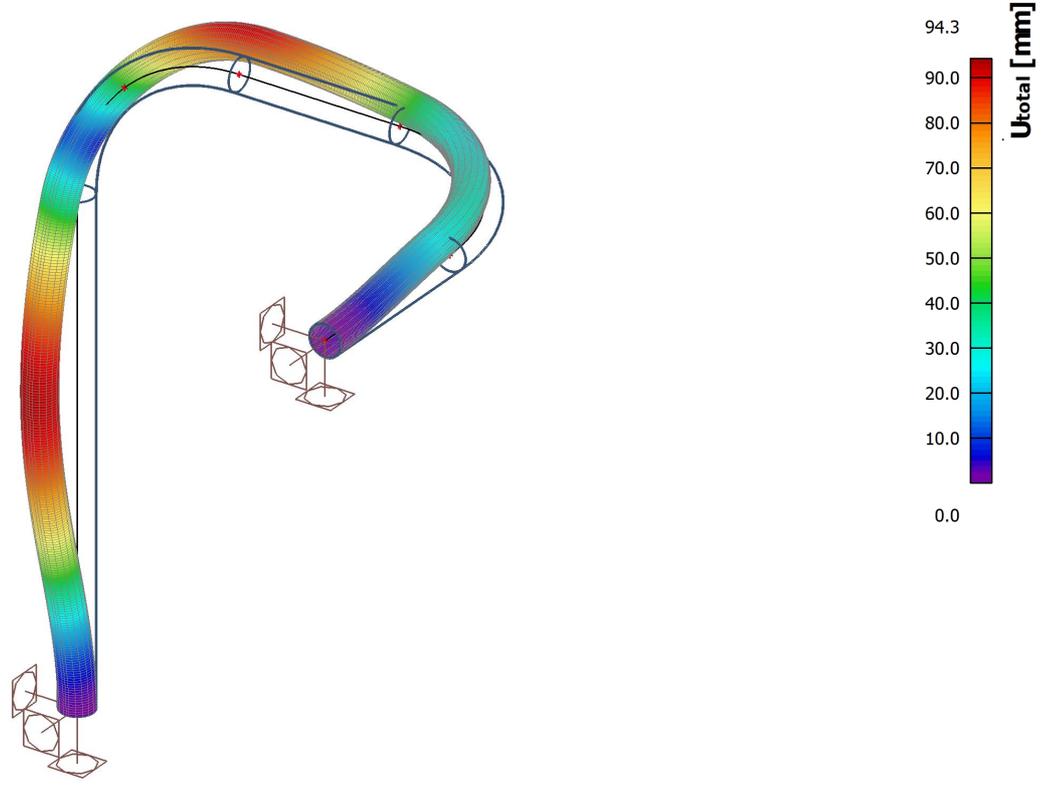
4.4. 3D displacement; U_{total}

Valeur: **U_{total}**
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/3 - 27,99
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



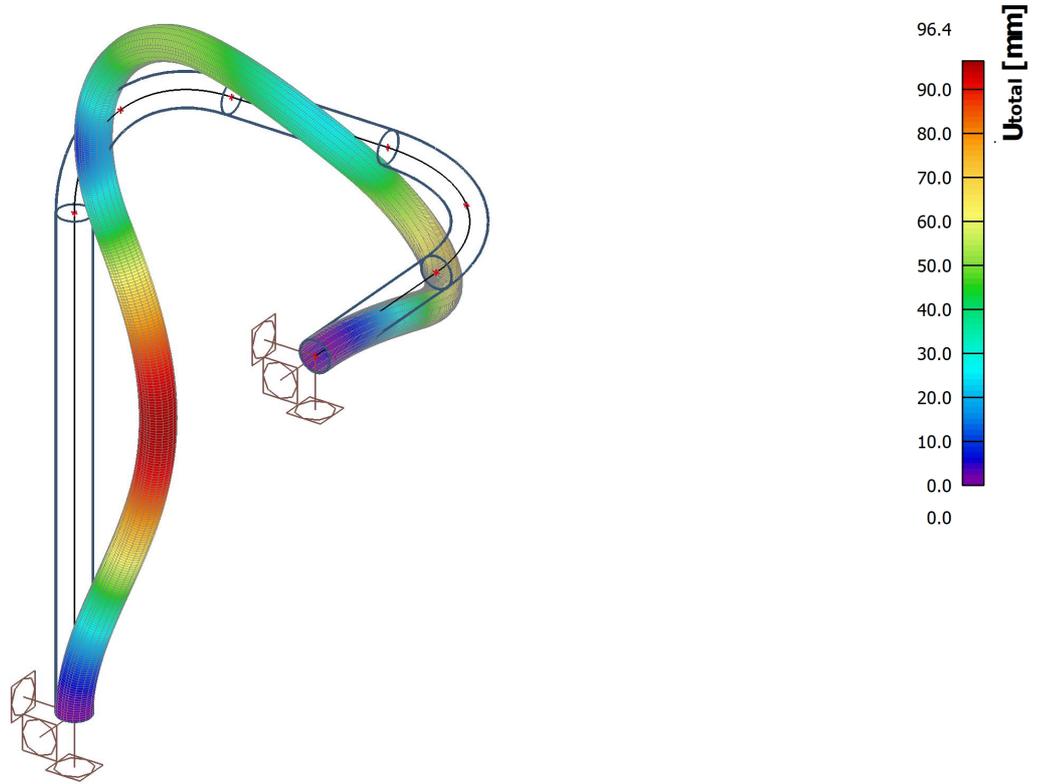
4.5. 3D displacement; U_{total}

Valeur: **U_{total}**
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/4 - 52,66
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



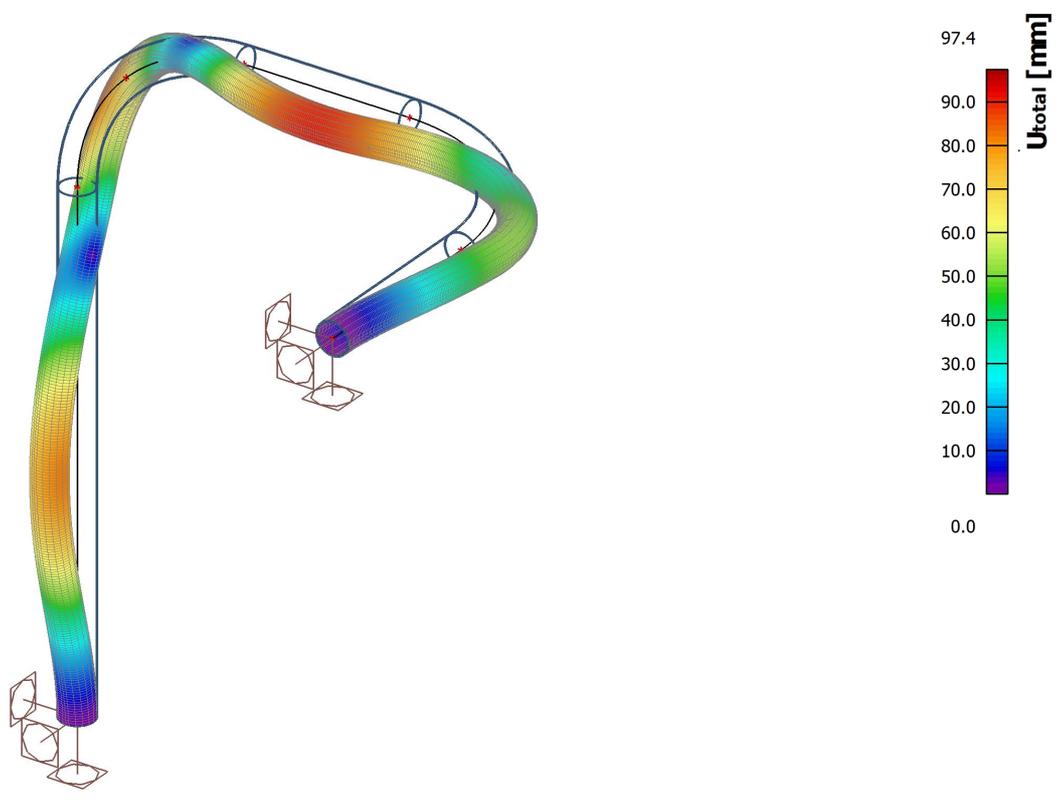
4.6. 3D displacement; U_{total}

Valeur: **U_{total}**
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/5 - 57,91
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



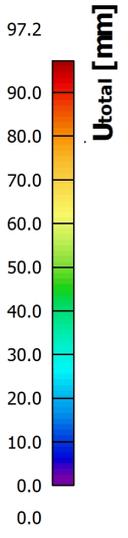
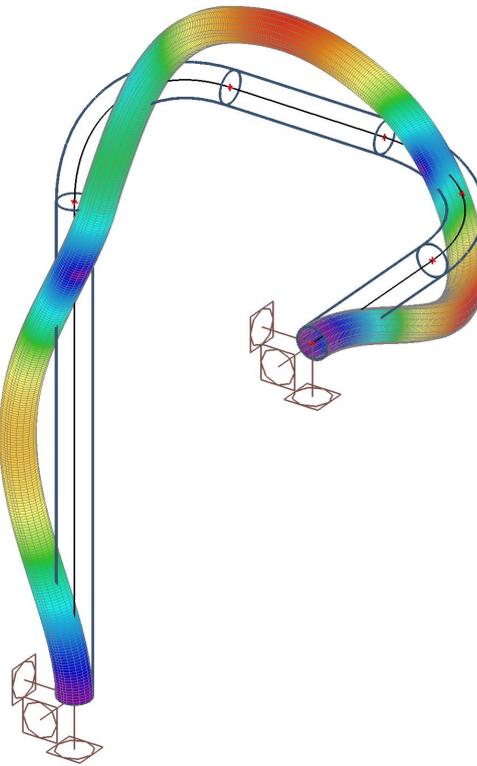
4.7. 3D displacement; U_{total}

Valeur: **U_{total}**
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/6 - 92,77
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



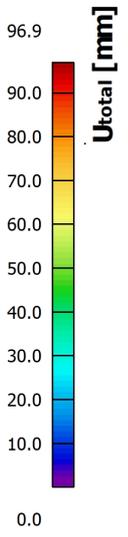
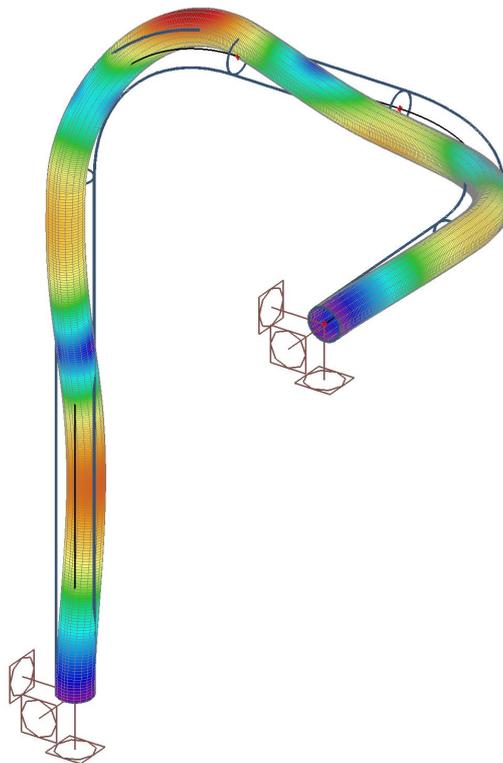
4.8. 3D displacement; U_{total}

Valeur: **U_{total}**
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/7 - 97,27
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



4.9. 3D displacement; U_{total}

Valeur: **U_{total}**
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/8 - 149,03
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



4.10. 3D displacement; U_total

Valeur: **U_{total}**

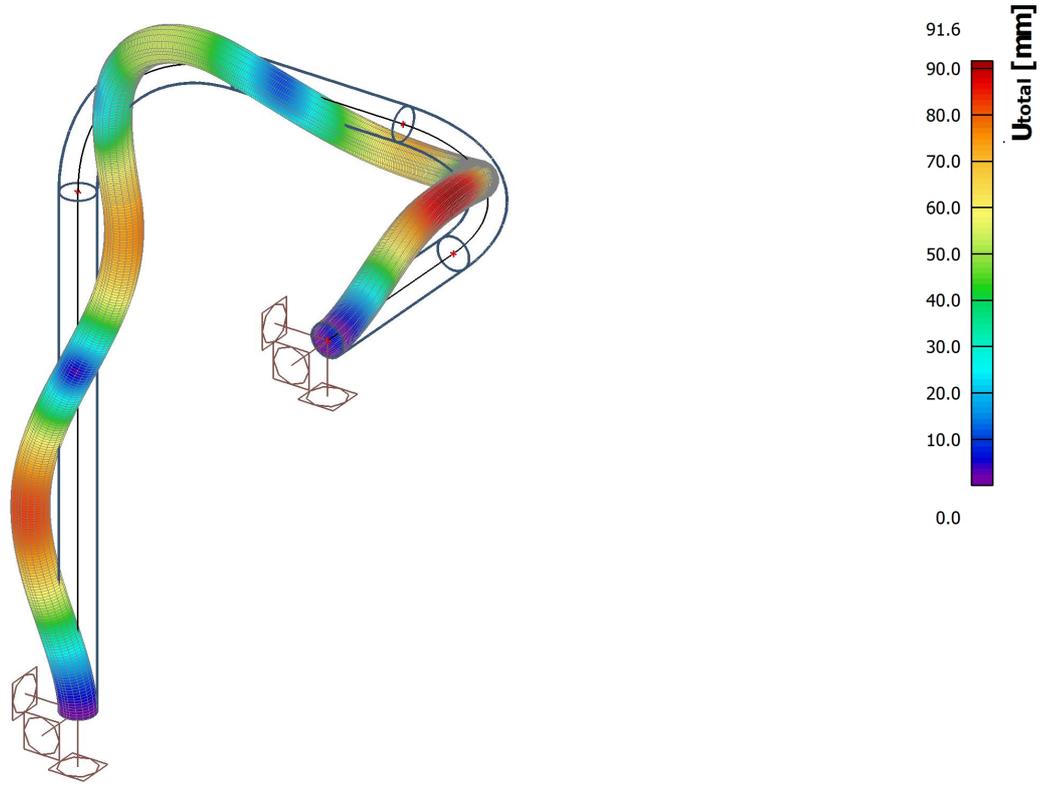
Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.

Combinaison masse: CM1/9 - 152,80

Sélection: Tout

Position: Aux noeuds, moyenne.

Système: Global



5. EXPECTED AFNOR RESULTS

Eigenfrequencies:

f1 = 10.18 Hz

f2 = 19.54 Hz

f3 = 25.47 Hz

f4 = 48.09 Hz

f5 = 52.96 Hz

f6 = 75.94 Hz

f7 = 80.11 Hz

f8 = 122.34 Hz

f9 = 123.15Hz

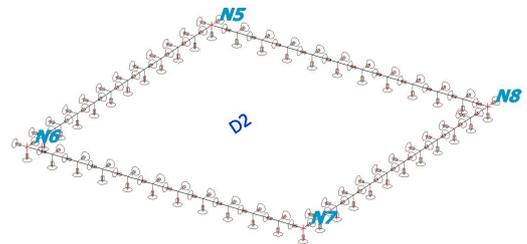
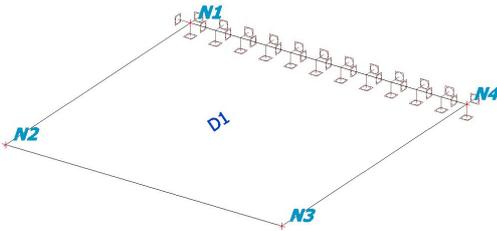
REFERENCE : "Guide de validation des progiciels de calcul de structures" AFNOR, 1990

1. TESTCASE DESCRIPTION

Modal analysis of a cantilever and a free plate

2. MODEL

2.1. Analysis model



2.2. Nodes

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] |
|------|-------------|-------------|-------------|
| N1 | 0,000 | 0,000 | 0,000 |
| N2 | 1,000 | 0,000 | 0,000 |
| N3 | 1,000 | 1,000 | 0,000 |

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] |
|------|-------------|-------------|-------------|
| N4 | 0,000 | 1,000 | 0,000 |
| N5 | 0,000 | 3,000 | 0,000 |
| N6 | 1,000 | 3,000 | 0,000 |

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] |
|------|-------------|-------------|-------------|
| N7 | 1,000 | 4,000 | 0,000 |
| N8 | 0,000 | 4,000 | 0,000 |

2.3. 2D members

| Name | Layer | Type | Element type | Material | Thickness type | Th. [mm] |
|------|---------|------------|--------------|----------|----------------|----------|
| D1 | Calque1 | dalle (90) | Standard | S 235 | constant | 10,0 |
| D2 | Calque1 | dalle (90) | Standard | S 235 | constant | 10,0 |

2.4. Supports on 2D member edge

| Name | 2D member | Orig | Pos x ₁ | X | Y | Z | Rx | Ry | Rz | Stiffness X [MN/m ²] |
|------|-----------|--------------------|--------------------|----------|----------|----------|-------|-------|-------|--|
| | Edge | Coor | Pos x ₂ | | | | | | | Stiffness Y [MN/m ²] |
| | | | | | | | | | | Stiffness Z [MN/m ²] |
| Sle1 | D1 4 | From start Rela | 0.000 1.000 | Rigid | Rigid | Rigid | Rigid | Rigid | Rigid | |
| Sle2 | D2 4 | From start Rela | 0.000 1.000 | Flexible | Flexible | Flexible | Free | Free | Free | 1,0000e-06 1,0000e-06 1,0000e-06 |
| Sle3 | D2 1 | From start Rela | 0.000 1.000 | Flexible | Flexible | Flexible | Free | Free | Free | 1,0000e-06 1,0000e-06 1,0000e-06 |
| Sle4 | D2 2 | From start Rela | 0.000 1.000 | Flexible | Flexible | Flexible | Free | Free | Free | 1,0000e-06 1,0000e-06 1,0000e-06 |
| Sle5 | D2 3 | From start Rela | 0.000 1.000 | Flexible | Flexible | Flexible | Free | Free | Free | 1,0000e-06 1,0000e-06 1,0000e-06 |

2.5. Materials

Steel EC3

| Name | ρ [kg/m ³] | E _{mod} [MPa] | μ | Limit inférieure [mm] | Limite supérieure [mm] | F _y [MPa] | F _u [MPa] | Colour |
|-------|---------------------------|---------------------------|-------------|--------------------------|---------------------------|-------------------------|-------------------------|--------|
| | | G _{mod} [MPa] | α [m/mK] | | | | | |
| S 235 | 7850,00 | 2,1000e+05 | 0.3 | 0,0 | 40,0 | 235,0 | 360,0 | ■ |
| | | 8,0769e+04 | 0,01e-003 | 40,0 | 80,0 | 215,0 | 360,0 | |

3. LOAD and MASS

3.1. Mass groups

| Name | Load case |
|------|--------------------|
| MG1 | LC1 - Poids propre |

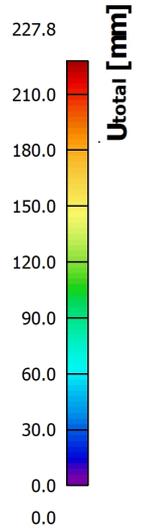
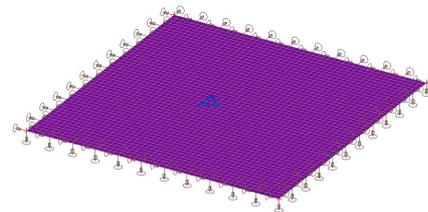
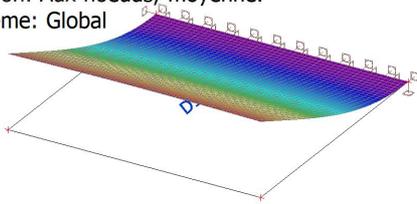
4. RESULTS

4.1. Eigen frequencies

| N | f [Hz] | ω [1/s] | ω^2 [1/s ²] | T [s] |
|-------------------------------|-----------|-------------------|-----------------------------------|----------|
| Mass combination : CM1 | | | | |
| 1 | 0,04 | 0,23 | 0,05 | 27,83 |
| 2 | 0,04 | 0,23 | 0,05 | 27,83 |
| 3 | 0,04 | 0,23 | 0,05 | 27,83 |
| 4 | 0,05 | 0,32 | 0,10 | 19,69 |
| 5 | 0,05 | 0,32 | 0,10 | 19,69 |
| 6 | 0,05 | 0,32 | 0,10 | 19,69 |
| 7 | 8,65 | 54,32 | 2950,96 | 0,12 |
| 8 | 21,20 | 133,20 | 17741,76 | 0,05 |
| 9 | 33,63 | 211,31 | 44650,46 | 0,03 |
| 10 | 48,92 | 307,39 | 94487,12 | 0,02 |
| 11 | 52,98 | 332,87 | 110800,99 | 0,02 |
| 12 | 60,40 | 379,48 | 144005,15 | 0,02 |
| 13 | 67,73 | 425,52 | 181067,73 | 0,01 |
| 14 | 77,03 | 483,97 | 234229,72 | 0,01 |
| 15 | 86,56 | 543,85 | 295770,50 | 0,01 |
| 16 | 86,57 | 543,94 | 295869,21 | 0,01 |
| 17 | 134,72 | 846,46 | 716490,62 | 0,01 |
| 18 | 151,87 | 954,20 | 910492,86 | 0,01 |

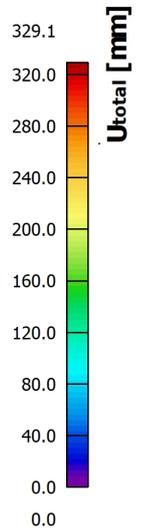
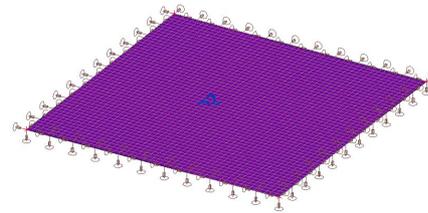
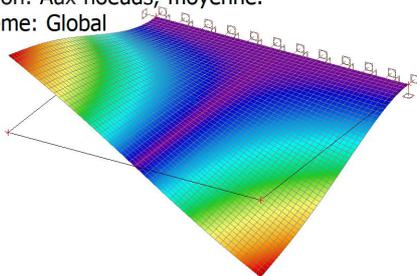
4.2. 3D displacement; Cantilever plate

Valeur: U_{total}
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/7 - 8,65
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



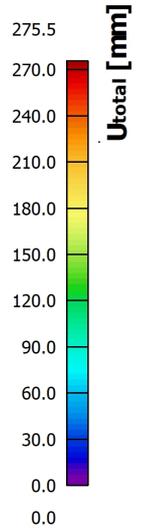
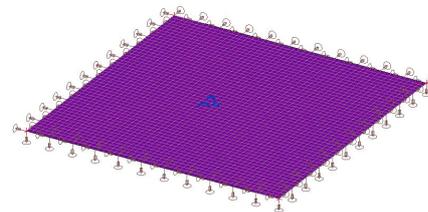
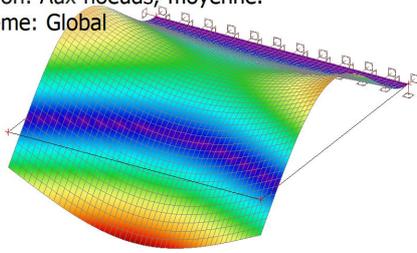
4.3. 3D displacement; Cantilever plate

Valeur: U_{total}
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/8 - 21,20
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



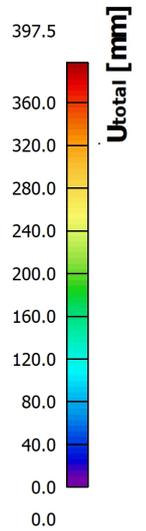
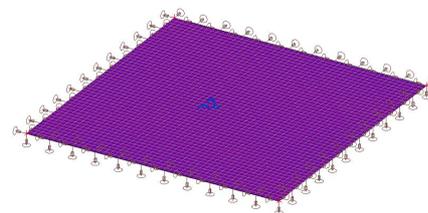
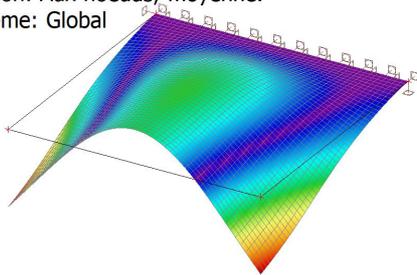
4.4. 3D displacement; Cantilever plate

Valeur: U_{total}
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/11 - 52,98
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



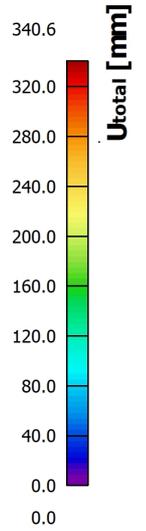
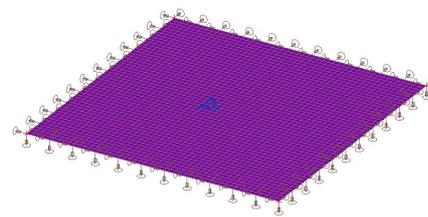
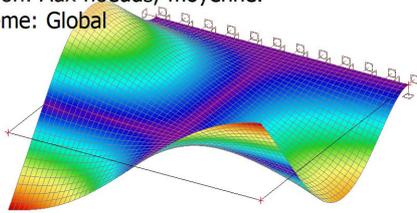
4.5. 3D displacement; Cantilever plate

Valeur: U_{total}
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/13 - 67,73
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



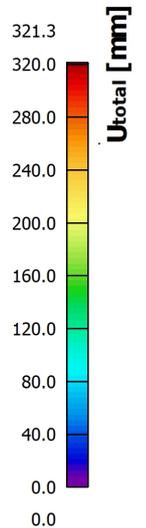
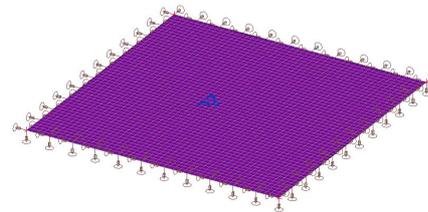
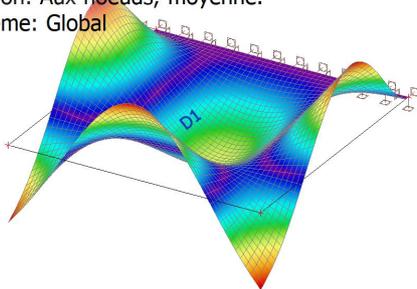
4.6. 3D displacement; Cantilever plate

Valeur: U_{total}
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/14 - 77,03
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



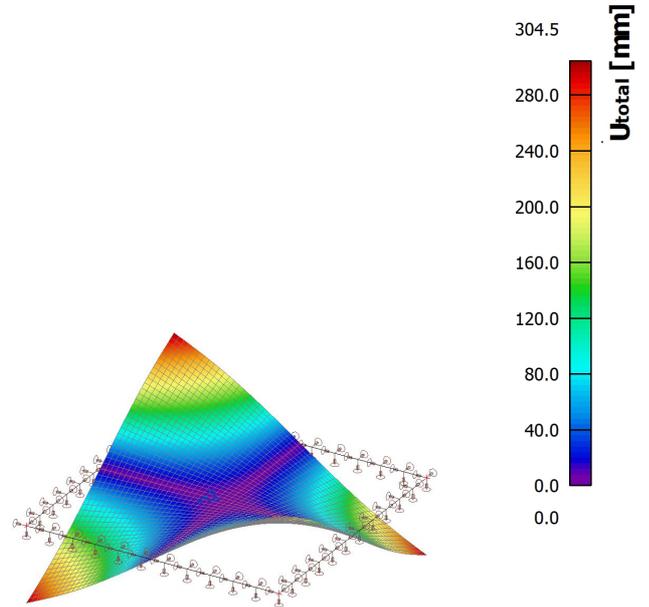
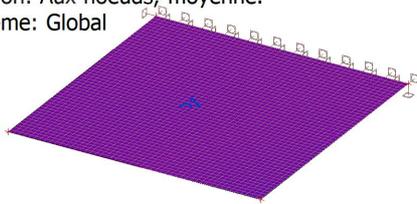
4.7. 3D displacement; Cantilever plate

Valeur: U_{total}
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/17 - 134,72
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



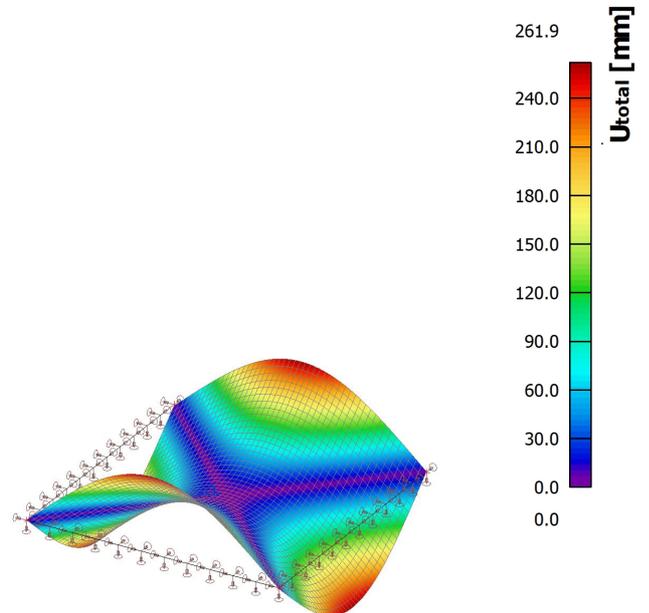
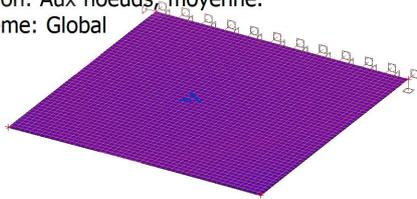
4.8. 3D displacement; Free plate

Valeur: U_{total}
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/9 - 33,63
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



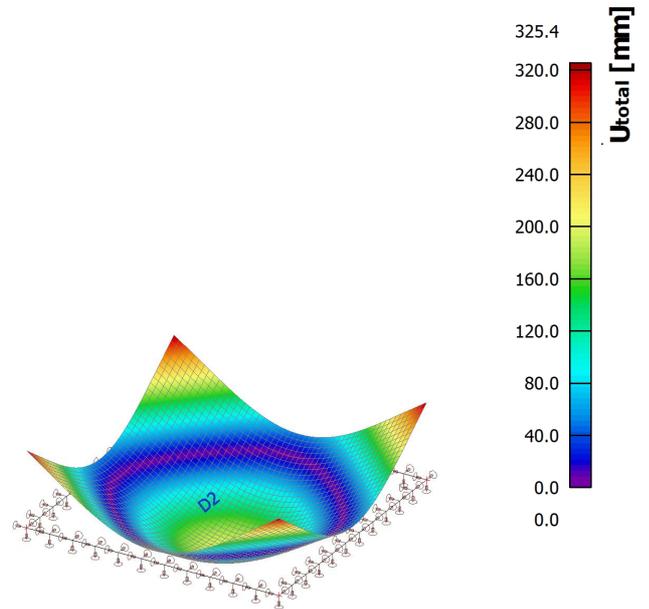
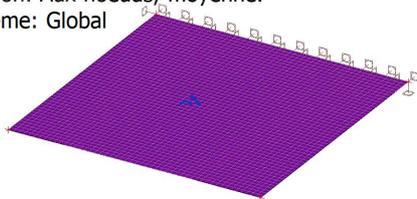
4.9. 3D displacement; Free plate

Valeur: U_{total}
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/10 - 48,92
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



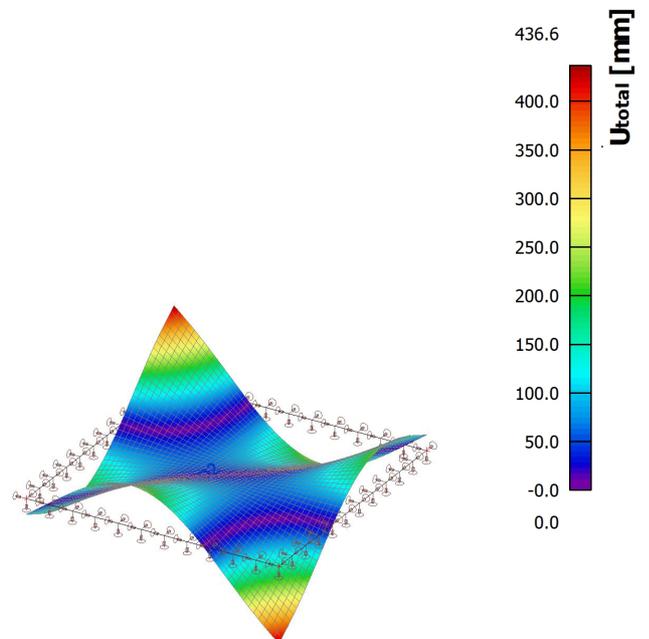
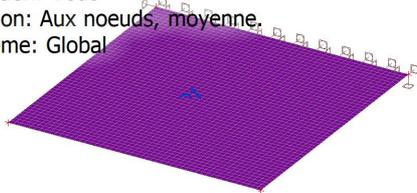
4.10. 3D displacement; Free plate

Valeur: U_{total}
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/12 - 60,40
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



4.11. 3D displacement; Free plate

Valeur: U_{total}
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/15 - 86,56
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



4.12. 3D displacement; Free plate

Valeur: U_{total}

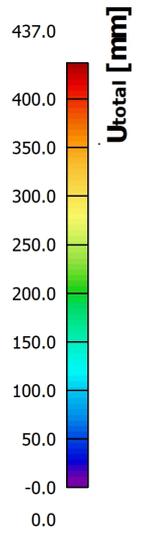
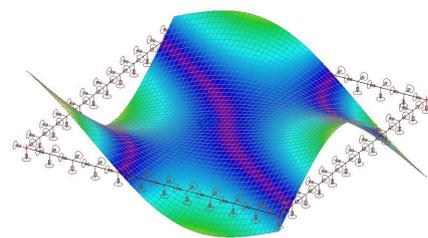
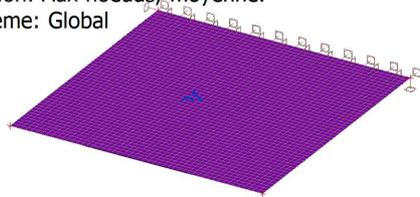
Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.

Combinaison masse: CM1/16 - 86,57

Sélection: Tout

Position: Aux noeuds, moyenne.

Système: Global



5. EXPECTED AFNOR RESULTS

Cantilever plate (D1) eigenfrequencies:

f1 = 8.7266 Hz

f2 = 21.3042 Hz

f3 = 53.5542 Hz

f4 = 68.2984 Hz

f5 = 77.7448 Hz

f5 = 136.0471 Hz

Free plate (D2) eigenfrequencies:

f1 = 33.7119 Hz

f2 = 49.4558 Hz

f3 = 61.0513 Hz

f4 = 87.5160 Hz

f5 = 87.5160 Hz

NOTE : First six eigenfrequencies are nul and correspond to rigid body motion.

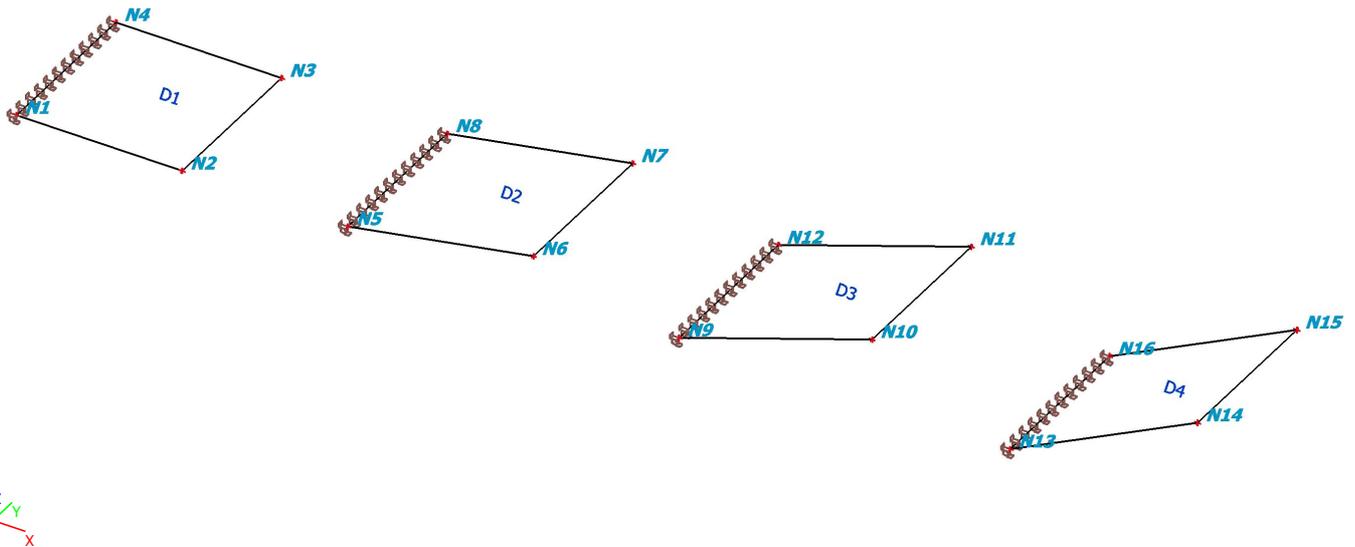
REFERENCE : "Guide de validation des progiciels de calcul de structures" AFNOR, 1990

1. TESTCASE DESCRIPTION

Modal analysis of a diamond plate with different angles

2. MODEL

2.1. Analysis model



2.2. Nodes

| Name | Coord X | Coord Y | Coord Z |
|------|---------|---------|---------|
| N1 | 0,000 | 0,000 | 0,000 |
| N2 | 1,000 | 0,000 | 0,000 |
| N3 | 1,000 | 1,000 | 0,000 |
| N4 | 0,000 | 1,000 | 0,000 |
| N5 | 2,000 | 0,000 | 0,000 |
| N6 | 2,966 | 0,259 | 0,000 |

| Name | Coord X | Coord Y | Coord Z |
|------|---------|---------|---------|
| N7 | 2,966 | 1,259 | 0,000 |
| N8 | 2,000 | 1,000 | 0,000 |
| N9 | 4,000 | 0,000 | 0,000 |
| N10 | 4,866 | 0,500 | 0,000 |
| N11 | 4,866 | 1,500 | 0,000 |
| N12 | 4,000 | 1,000 | 0,000 |

| Name | Coord X | Coord Y | Coord Z |
|------|---------|---------|---------|
| N13 | 6,000 | 0,000 | 0,000 |
| N14 | 6,707 | 0,707 | 0,000 |
| N15 | 6,707 | 1,707 | 0,000 |
| N16 | 6,000 | 1,000 | 0,000 |

2.3. 2D members

| Name | Layer | Type | Element type | Material | Thickness type | Th. [mm] |
|------|---------|------------|--------------|----------|----------------|----------|
| D1 | Calque1 | dalle (90) | Standard | S 235 | constant | 10,0 |
| D2 | Calque1 | dalle (90) | Standard | S 235 | constant | 10,0 |
| D3 | Calque1 | dalle (90) | Standard | S 235 | constant | 10,0 |
| D4 | Calque1 | dalle (90) | Standard | S 235 | constant | 10,0 |

2.4. Supports on 2D member edge

| Name | 2D member Edge | Orig Coor | Pos x1 Pos x2 | X | Y | Z | Rx | Ry | Rz |
|------|----------------|------------|---------------|-------|-------|-------|-------|-------|-------|
| Sle1 | D1 4 | From start | 0.000 | Rigid | Rigid | Rigid | Rigid | Rigid | Rigid |
| | | Rela | 1.000 | | | | | | |
| Sle2 | D2 4 | From start | 0.000 | Rigid | Rigid | Rigid | Rigid | Rigid | Rigid |
| | | Rela | 1.000 | | | | | | |
| Sle3 | D3 4 | From start | 0.000 | Rigid | Rigid | Rigid | Rigid | Rigid | Rigid |
| | | Rela | 1.000 | | | | | | |
| Sle4 | D4 4 | From start | 0.000 | Rigid | Rigid | Rigid | Rigid | Rigid | Rigid |
| | | Rela | 1.000 | | | | | | |

2.5. Materials

Steel EC3

| Name | ρ [kg/m ³] | E_{mod} [MPa] | μ | Limit inférieure [mm] | Limite supérieure [mm] | F_y [MPa] | F_u [MPa] | Colour |
|-------|--------------------------------|--------------------|--------------------|--------------------------|---------------------------|----------------|----------------|--------|
| | | G_{mod} [MPa] | α [m/mK] | | | | | |
| S 235 | 7850,00 | 2,1000e+05 | 0.3 | 0,0 | 40,0 | 235,0 | 360,0 | ■ |
| | | 8,0769e+04 | 0,01e-003 | 40,0 | 80,0 | 215,0 | 360,0 | |

3. LOAD and MASS

3.1. Mass groups

| Name | Load case |
|------|--------------------|
| MG1 | LC1 - Poids propre |

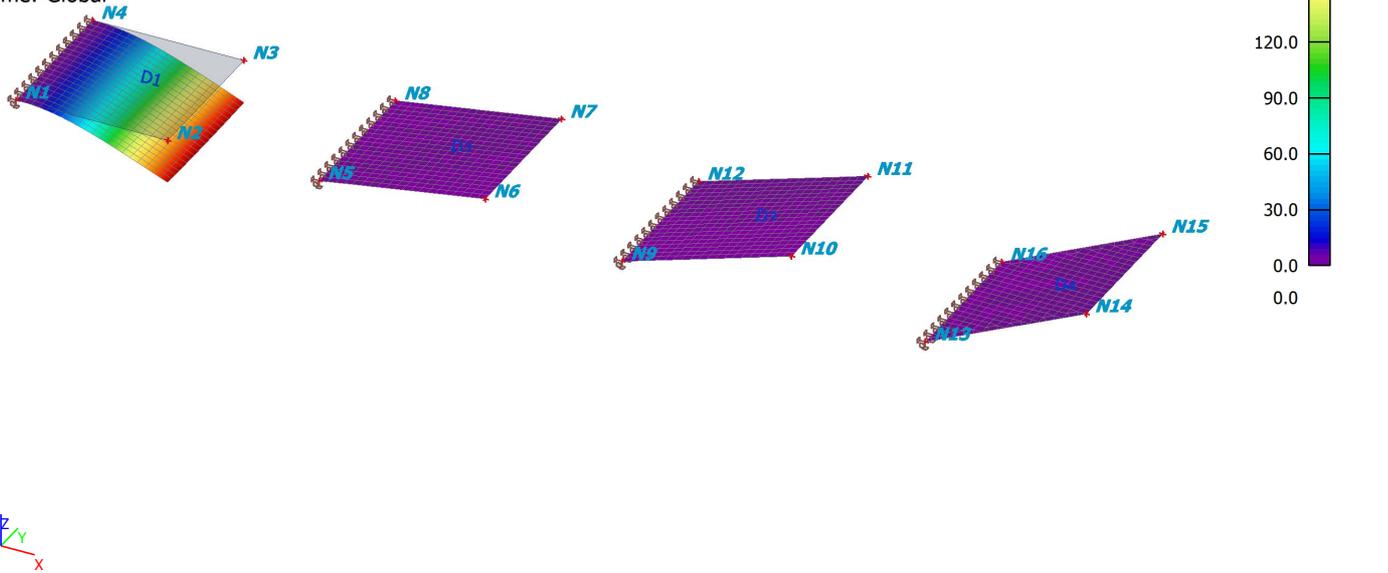
4. RESULTS

4.1. Eigen frequencies

| N | f [Hz] | ω [1/s] | ω^2 [1/s ²] | T [s] |
|-------------------------------|-----------|-------------------|-----------------------------------|----------|
| Mass combination : CM1 | | | | |
| 1 | 8,64 | 54,29 | 2947,60 | 0,12 |
| 2 | 8,92 | 56,04 | 3140,87 | 0,11 |
| 3 | 9,78 | 61,44 | 3775,33 | 0,10 |
| 4 | 11,27 | 70,81 | 5013,91 | 0,09 |
| 5 | 21,13 | 132,74 | 17620,75 | 0,05 |
| 6 | 21,60 | 135,73 | 18423,69 | 0,05 |
| 7 | 23,39 | 146,98 | 21602,45 | 0,04 |
| 8 | 27,89 | 175,21 | 30698,34 | 0,04 |

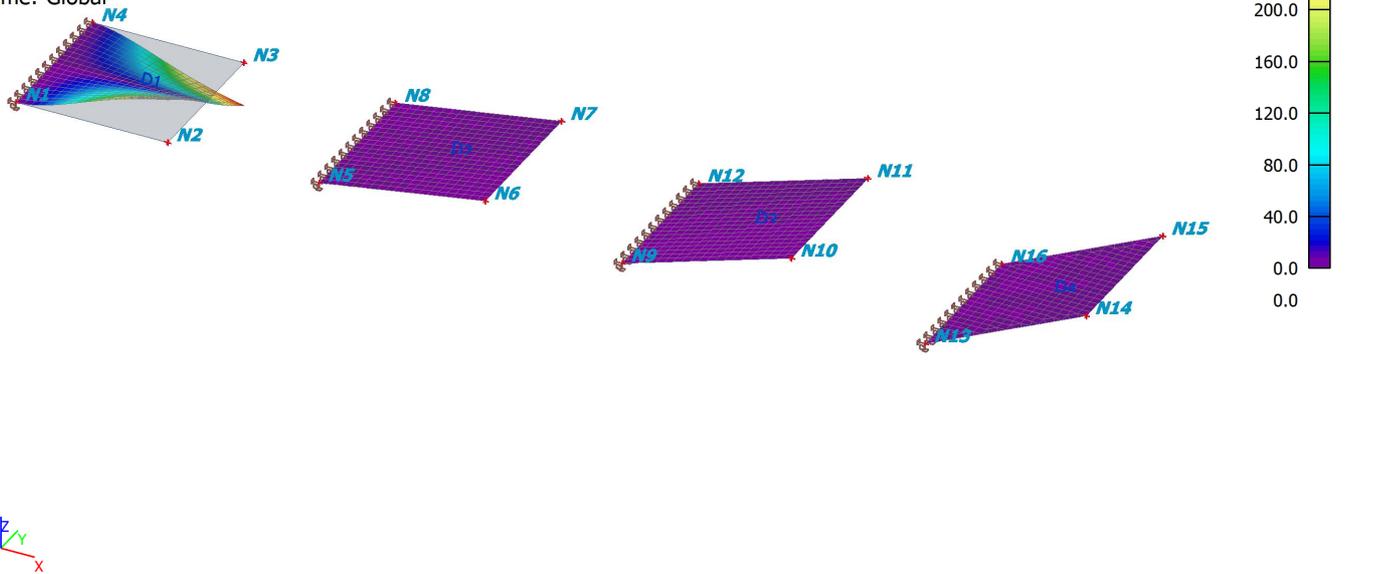
4.2. 3D displacement; Plate D1

Valeur: U_{total}
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/1 - 8,64
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



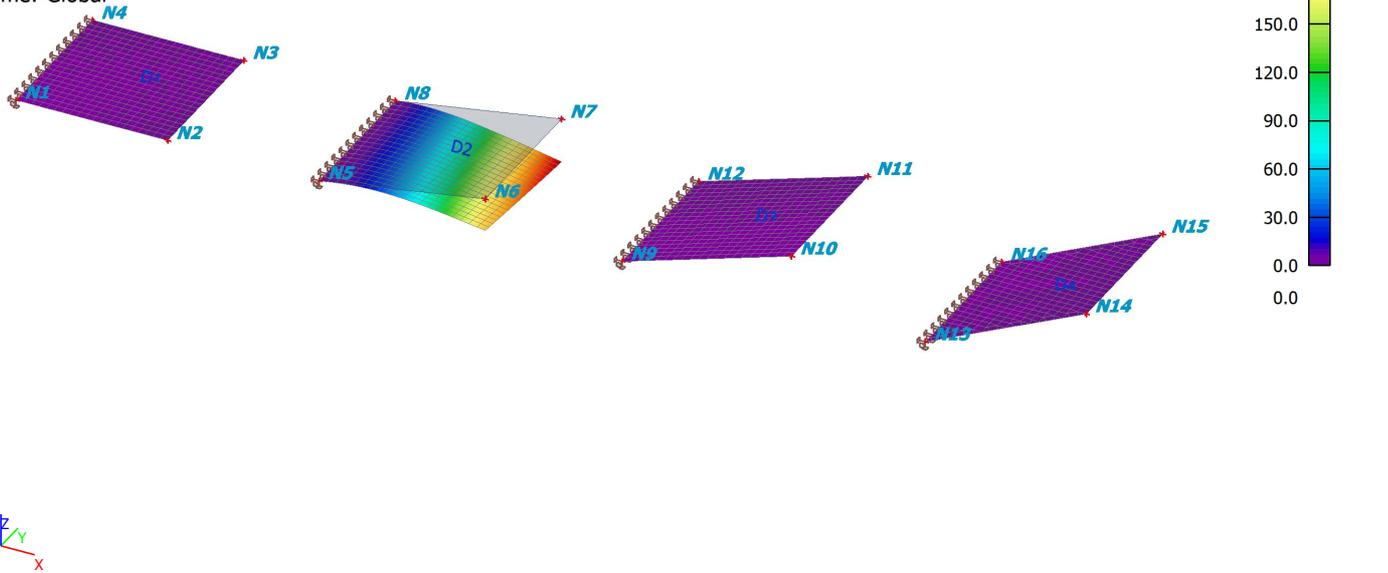
4.3. 3D displacement; Plate D1

Valeur: U_{total}
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/5 - 21,13
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



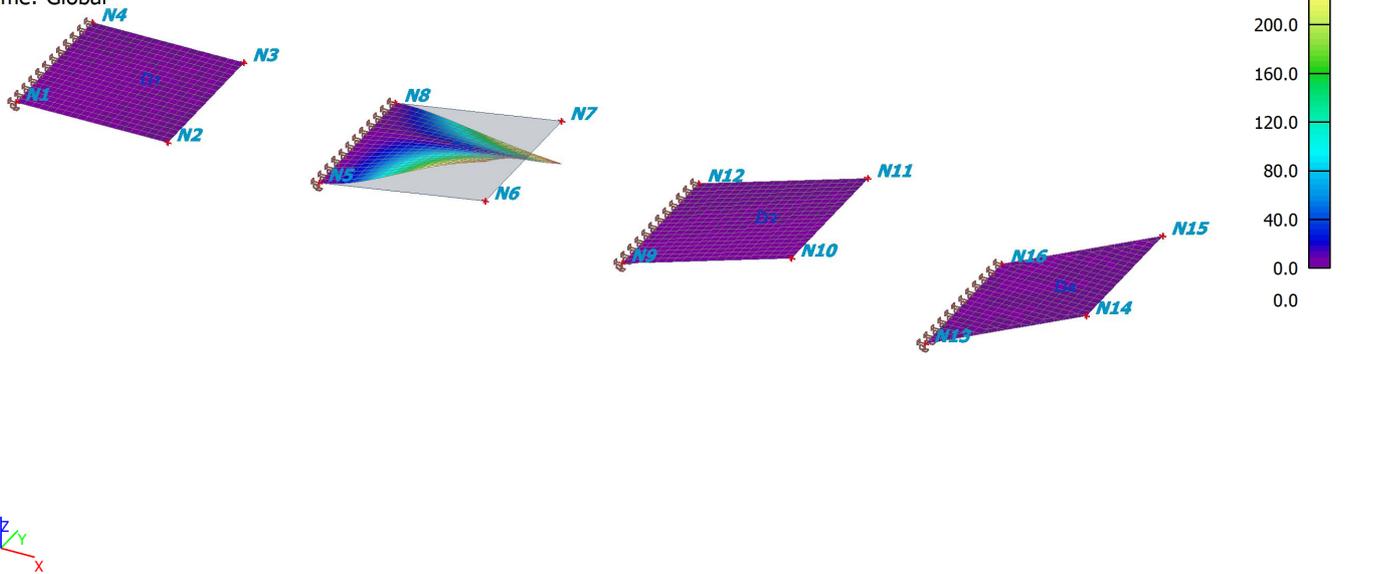
4.4. 3D displacement; Plate D2

Valeur: U_{total}
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/2 - 8,92
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



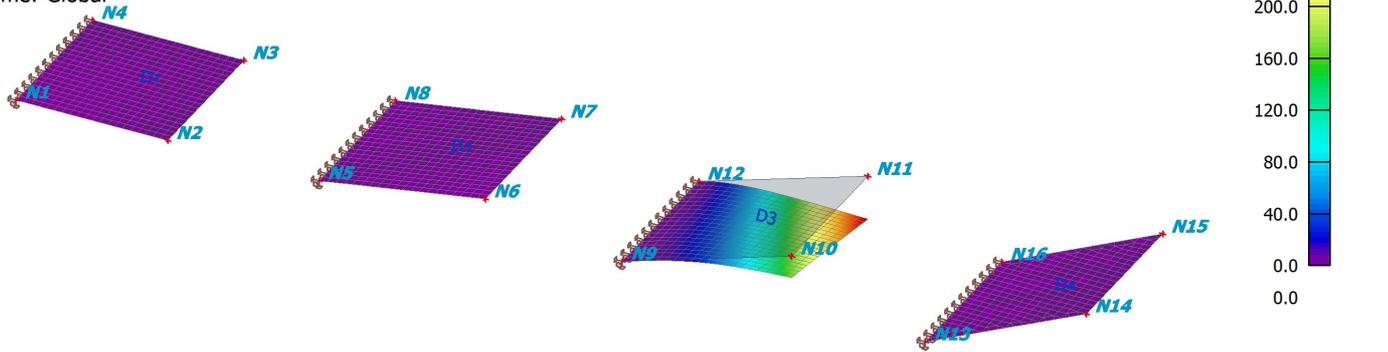
4.5. 3D displacement; Plate D2

Valeur: U_{total}
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/6 - 21,60
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



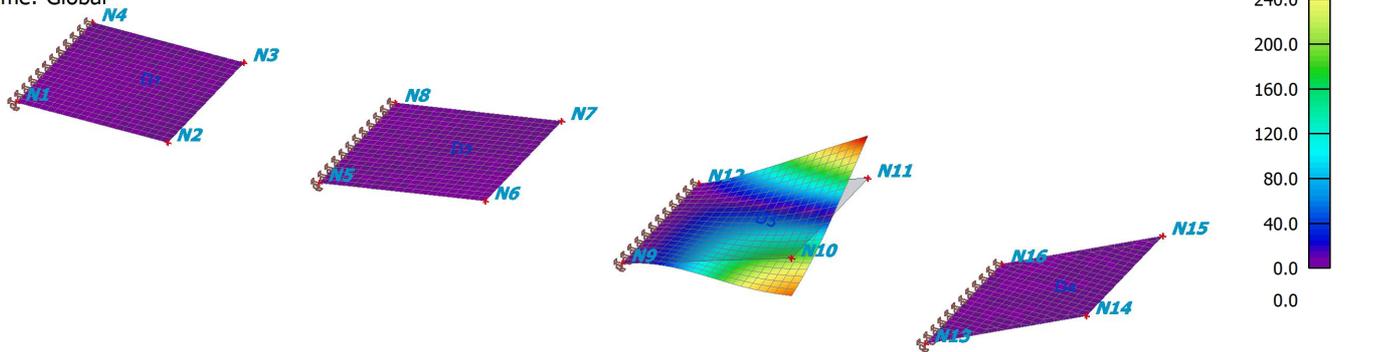
4.6. 3D displacement; Plate D3

Valeur: U_{total}
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/3 - 9,78
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



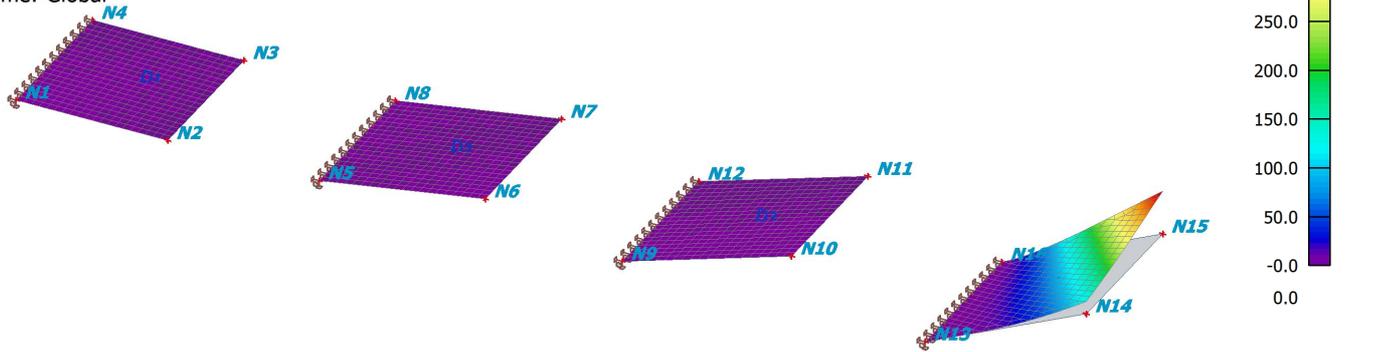
4.7. 3D displacement; Plate D3

Valeur: U_{total}
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/7 - 23,39
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



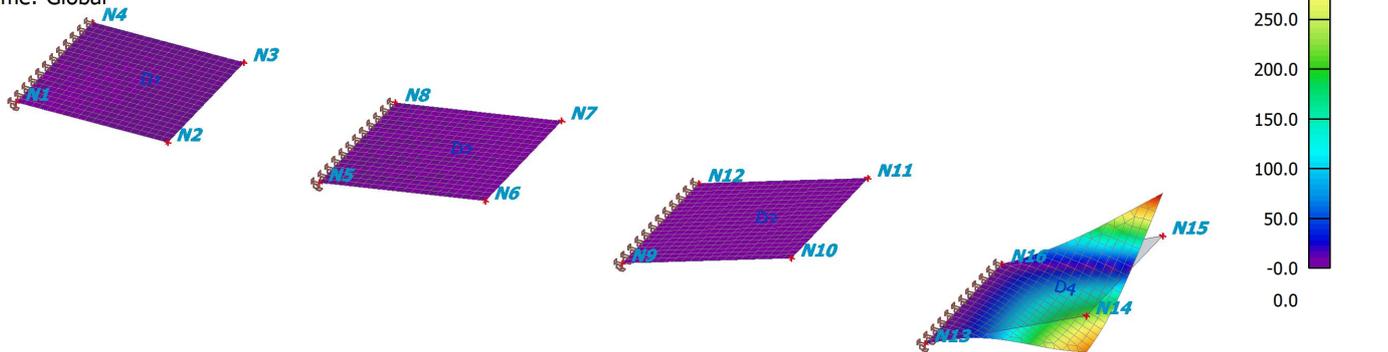
4.8. 3D displacement; Plate D4

Valeur: U_{total}
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/4 - 11,27
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



4.9. 3D displacement; Plate D4

Valeur: U_{total}
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/8 - 27,89
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



5. EXPECTED AFNOR RESULTS

PLATE D1 (0 degrees):

f1 = 8.7266 Hz

f2 = 21.3042 Hz

PLATE D2 (15 degrees):

f1 = 8.9990 Hz

f2 = 22.1714 Hz

PLATE D3 (30 degrees):

f1 = 9.8987 Hz

f2 = 25.4651 Hz

PLATE D4 (45 degrees):

f1 = 11.15 Hz

f2 = 27.0 Hz

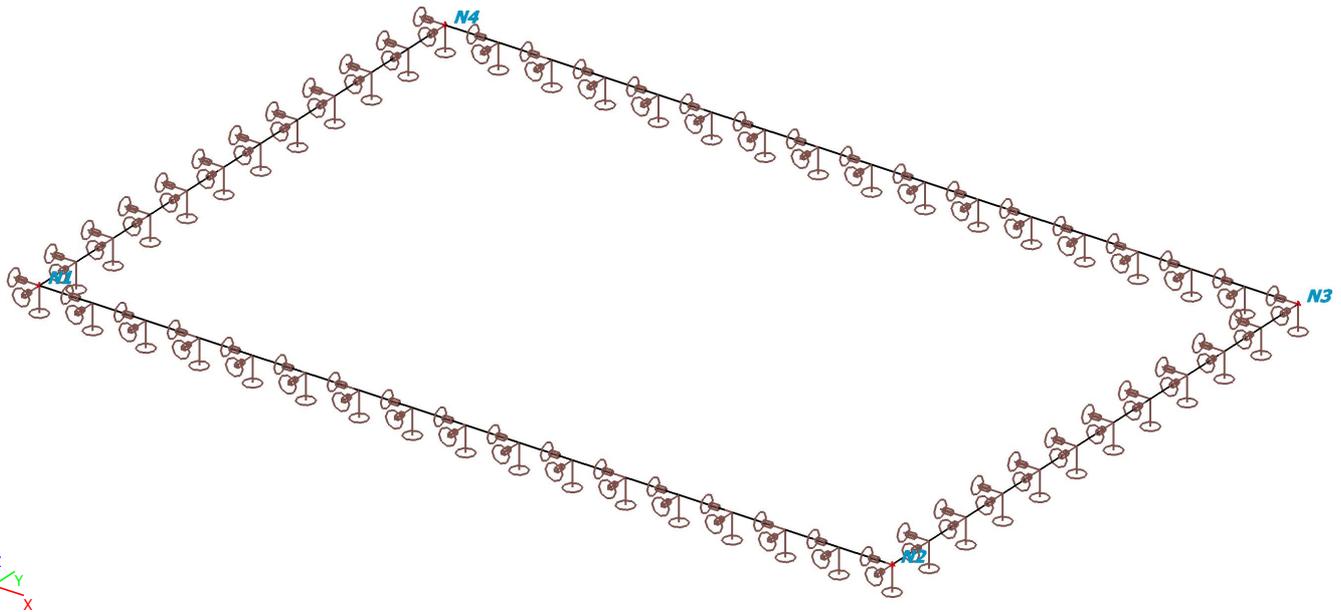
REFERENCE : "Guide de validation des progiciels de calcul de structures" AFNOR, 1990

1. TESTCASE DESCRIPTION

Modal analysis of a thin plate simply supported on the edges.

2. MODEL

2.1. Analysis model



2.2. Nodes

| Name | Coord X | Coord Y | Coord Z |
|------|---------|---------|---------|
| N1 | 0,000 | 0,000 | 0,000 |
| N2 | 1,500 | 0,000 | 0,000 |
| N3 | 1,500 | 1,000 | 0,000 |
| N4 | 0,000 | 1,000 | 0,000 |

2.3. 2D members

| Name | Layer | Type | Element type | Material | Thickness type | Th. [mm] |
|------|---------|------------|--------------|----------|----------------|----------|
| D1 | Calque1 | dalle (90) | Standard | S 235 | constant | 10,0 |

2.4. Supports on 2D member edge

| Name | 2D member Edge | Orig Coor | Pos x ₁ Pos x ₂ | X | Y | Z | Rx | Ry | Rz |
|------|----------------|------------|---------------------------------------|----------|----------|-------|------|------|------|
| Sle1 | D1 1 | From start | 0.000 | Flexible | Flexible | Rigid | Free | Free | Free |
| | | Rela | 1.000 | | | | | | |
| Sle2 | D1 2 | From start | 0.000 | Flexible | Flexible | Rigid | Free | Free | Free |
| | | Rela | 1.000 | | | | | | |
| Sle3 | D1 3 | From start | 0.000 | Flexible | Flexible | Rigid | Free | Free | Free |
| | | Rela | 1.000 | | | | | | |
| Sle4 | D1 4 | From start | 0.000 | Flexible | Flexible | Rigid | Free | Free | Free |
| | | Rela | 1.000 | | | | | | |

2.5. Materials

Steel EC3

| Name | ρ [kg/m ³] | E_{mod} [MPa] | μ | Limit inférieure [mm] | Limite supérieure [mm] | F_y [MPa] | F_u [MPa] | Colour |
|-------|--------------------------------|--------------------|--------------------|--------------------------|---------------------------|----------------|----------------|--------|
| | | G_{mod} [MPa] | α [m/mK] | | | | | |
| S 235 | 7850,00 | 2,1000e+05 | 0.3 | 0,0 | 40,0 | 235,0 | 360,0 | ■ |
| | | 8,0769e+04 | 0,01e-003 | 40,0 | 80,0 | 215,0 | 360,0 | |

3. LOAD and MASS

3.1. Mass groups

| Name | Load case |
|------|--------------------|
| MG1 | LC1 - Poids propre |

4. RESULTS

4.1. Eigen frequencies

| N | f [Hz] | ω [1/s] | ω^2 [1/s ²] | T [s] |
|-------------------------------|-----------|-------------------|-----------------------------------|----------|
| Mass combination : CM1 | | | | |
| 1 | 0,33 | 2,06 | 4,25 | 3,05 |
| 2 | 0,33 | 2,06 | 4,25 | 3,05 |
| 3 | 0,45 | 2,85 | 8,15 | 2,20 |
| 4 | 35,46 | 222,79 | 49635,97 | 0,03 |
| 5 | 68,11 | 427,95 | 183145,07 | 0,01 |
| 6 | 109,37 | 687,20 | 472239,19 | 0,01 |
| 7 | 122,74 | 771,19 | 594731,96 | 0,01 |
| 8 | 141,49 | 888,98 | 790293,04 | 0,01 |
| 9 | 195,24 | 1226,70 | 1504788,49 | 0,01 |

4.2. 3D displacement; U_{total}

Valeur: **U_{total}**

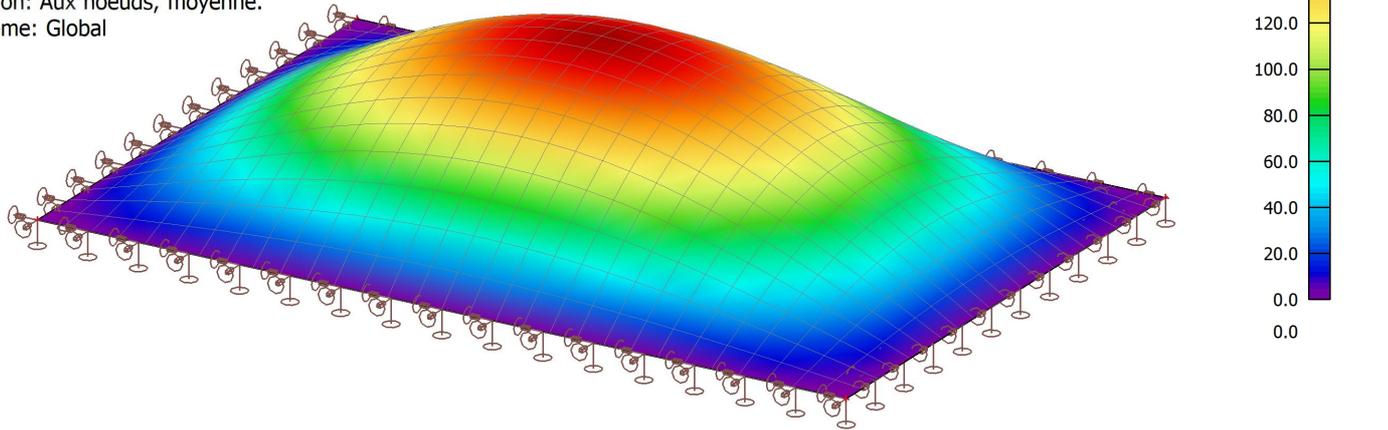
Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.

Combinaison masse: CM1/4 - 35,46

Sélection: Tout

Position: Aux noeuds, moyenne.

Système: Global



4.3. 3D displacement; U_{total}

Valeur: **U_{total}**

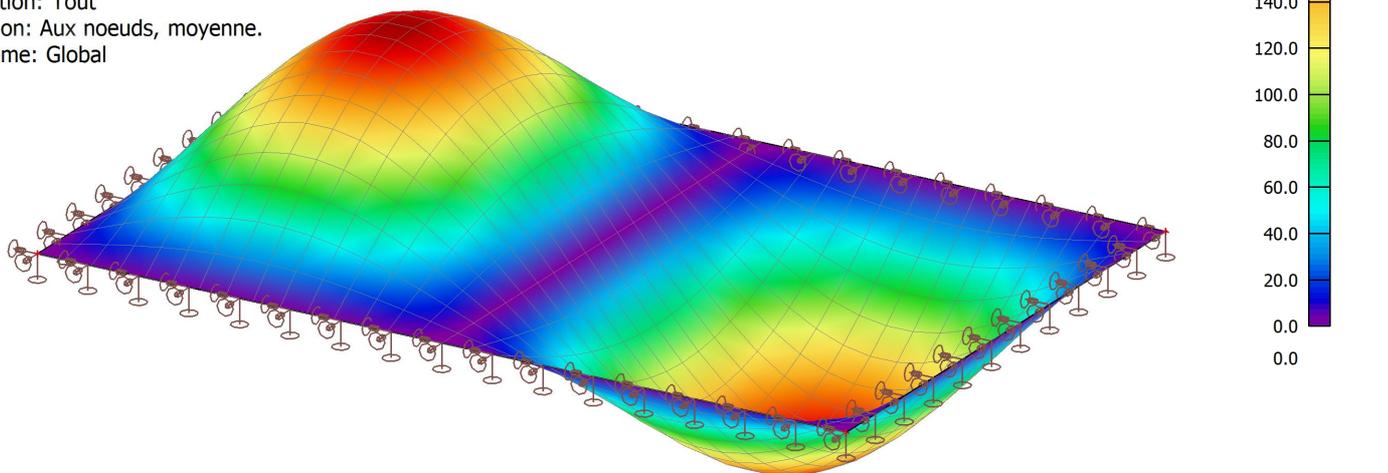
Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.

Combinaison masse: CM1/5 - 68,11

Sélection: Tout

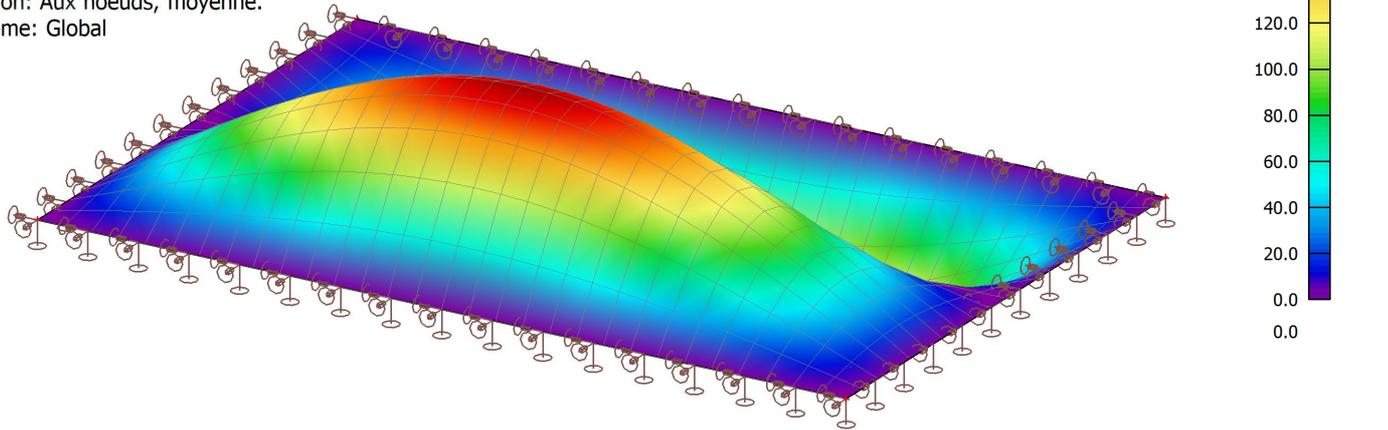
Position: Aux noeuds, moyenne.

Système: Global



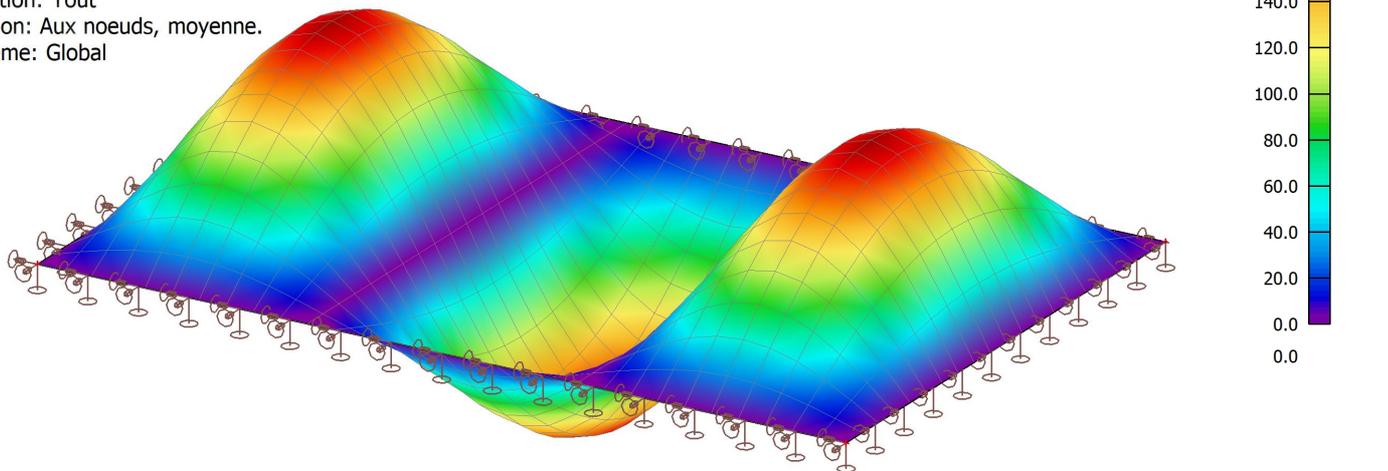
4.4. 3D displacement; U_{total}

Valeur: U_{total}
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/6 - 109,37
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



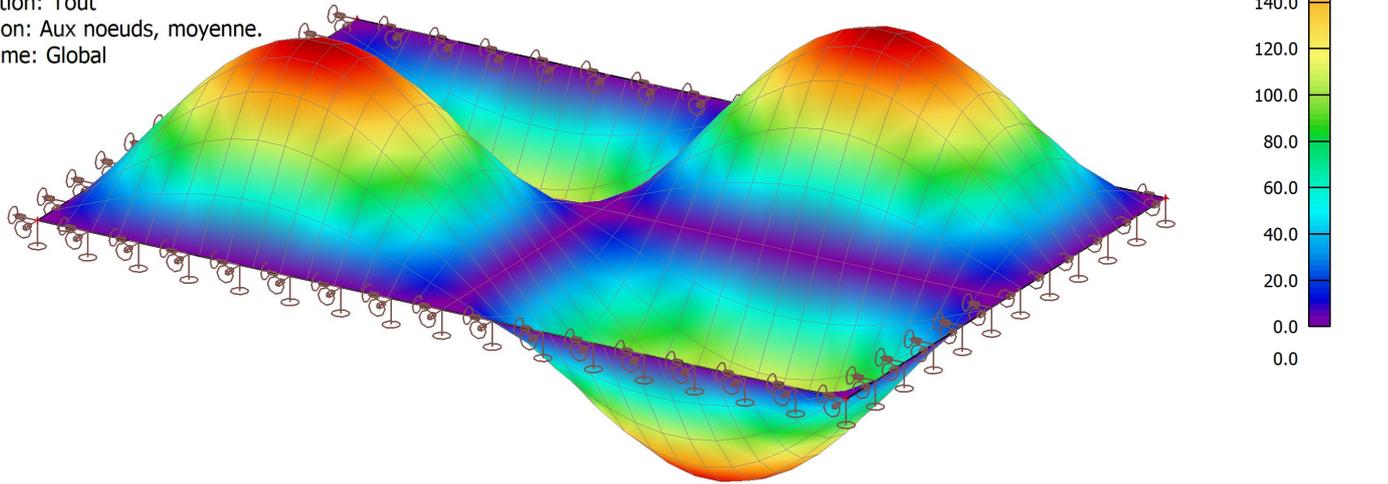
4.5. 3D displacement; U_{total}

Valeur: U_{total}
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/7 - 122,74
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



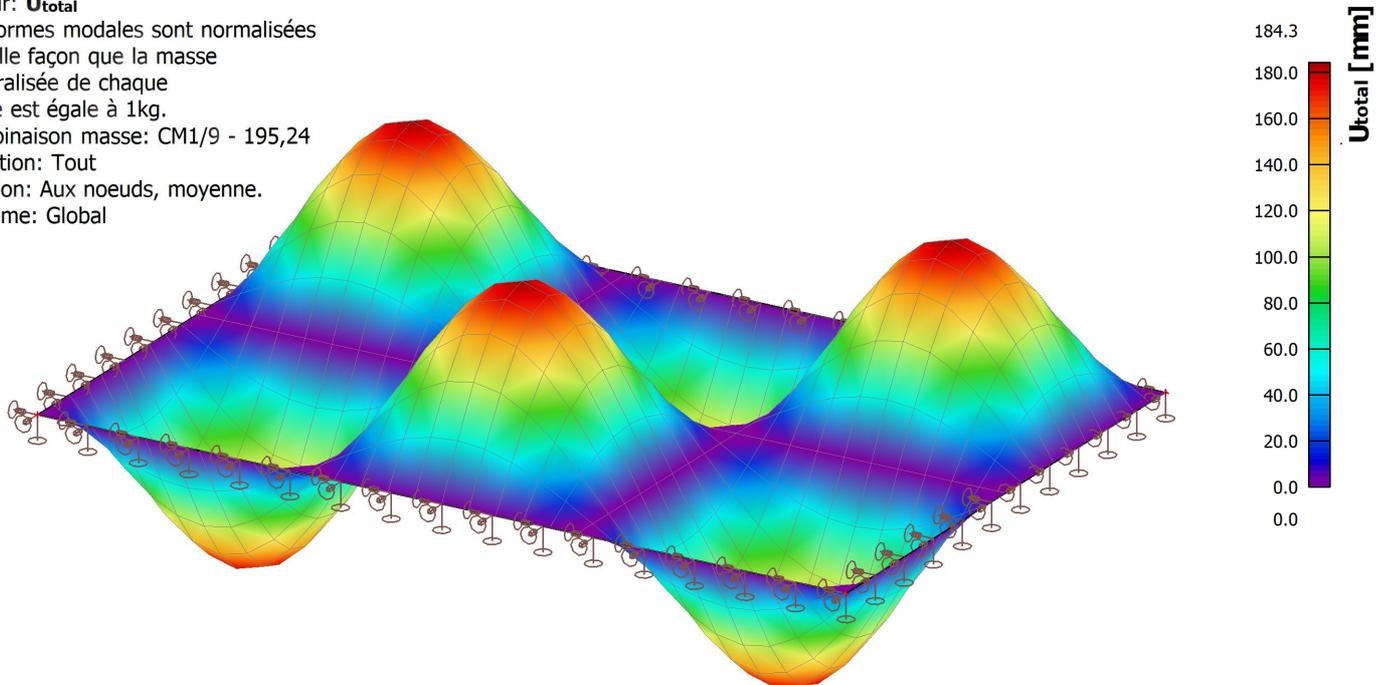
4.6. 3D displacement; U_{total}

Valeur: U_{total}
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/8 - 141,49
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



4.7. 3D displacement; U_{total}

Valeur: U_{total}
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/9 - 195,24
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



5. EXPECTED AFNOR RESULTS

Eigenfrequencies:

f1 = 35.63 Hz

f2 = 68.51 Hz

f3 = 109.62 Hz

f4 = 123.32 Hz

f5 = 142.51 Hz

f6 = 197.32 Hz

NOTE: The first three Eigenfrequencies are nul and correspond to rigid body motion.

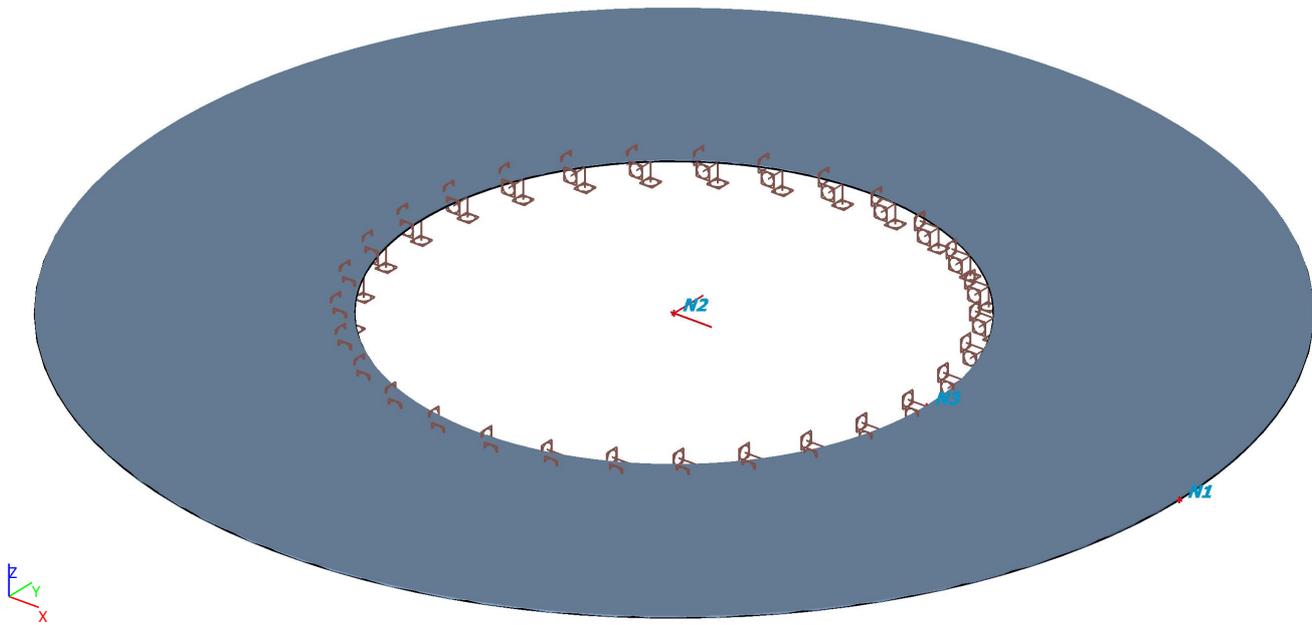
REFERENCE : "Guide de validation des progiciels de calcul de structures" AFNOR, 1990

1. TESTCASE DESCRIPTION

Modal analysis of a circular ring plate fixed on the internal circumference.

2. MODEL

2.1. Analysis model



2.2. Nodes

| Name | Coord X | Coord Y | Coord Z |
|------|---------|---------|---------|
| N1 | 0,200 | 0,000 | 0,000 |
| N2 | 0,000 | 0,000 | 0,000 |
| N3 | 0,100 | 0,000 | 0,000 |

2.3. 2D members

| Name | Layer | Type | Element type | Material | Thickness type | Th. [mm] |
|------|---------|------------|--------------|----------|----------------|----------|
| D1 | Calque1 | dalle (90) | Standard | S 235 | constant | 1,0 |

2.4. 2D member openings

| Name | 2D member |
|------|-----------|
| O1 | D1 |

2.5. Supports on 2D member edge

| Name | Edge | Orig Coord | Pos x ₁ Pos x ₂ | X | Y | Z | Rx | Ry | Rz |
|------|------|--------------------|--|-------|-------|-------|-------|-------|-------|
| Sle1 | 1 | From start Rela | 0.000 1.000 | Rigid | Rigid | Rigid | Rigid | Rigid | Rigid |

2.6. Materials

Steel EC3

| Name | ρ [kg/m ³] | E_{mod} [MPa] | μ | Limit inférieure [mm] | Limite supérieure [mm] | F_y [MPa] | F_u [MPa] | Colour |
|-------|--------------------------------|--------------------|--------------------|--------------------------|---------------------------|----------------|----------------|--------|
| | | G_{mod} [MPa] | α [m/mK] | | | | | |
| S 235 | 7850,00 | 2,1000e+05 | 0.3 | 0,0 | 40,0 | 235,0 | 360,0 | ■ |
| | | 8,0769e+04 | 0,01e-003 | 40,0 | 80,0 | 215,0 | 360,0 | |

3. LOAD and MASS

3.1. Mass groups

| Name | Load case |
|------|--------------------|
| MG1 | LC1 - Poids propre |

4. RESULTS

4.1. Eigen frequencies

| N | f [Hz] | ω [1/s] | ω^2 [1/s ²] | T [s] |
|-------------------------------|-----------|-------------------|-----------------------------------|----------|
| Mass combination : CM1 | | | | |
| 1 | 81,09 | 509,50 | 259593,39 | 0,01 |
| 2 | 82,73 | 519,82 | 270212,61 | 0,01 |
| 3 | 82,73 | 519,82 | 270212,61 | 0,01 |
| 4 | 91,49 | 574,85 | 330455,21 | 0,01 |
| 5 | 91,49 | 574,85 | 330457,35 | 0,01 |
| 6 | 115,43 | 725,24 | 525970,02 | 0,01 |
| 7 | 115,43 | 725,24 | 525970,02 | 0,01 |
| 8 | 159,11 | 999,72 | 999430,67 | 0,01 |
| 9 | 159,11 | 999,72 | 999434,13 | 0,01 |
| 10 | 222,10 | 1395,48 | 1947354,44 | 0,00 |
| 11 | 222,10 | 1395,48 | 1947354,44 | 0,00 |
| 12 | 302,58 | 1901,13 | 3614291,33 | 0,00 |
| 13 | 302,59 | 1901,15 | 3614372,29 | 0,00 |
| 14 | 399,08 | 2507,41 | 6287129,70 | 0,00 |
| 15 | 399,08 | 2507,41 | 6287129,70 | 0,00 |
| 16 | 510,57 | 3207,91 | 10290667,03 | 0,00 |
| 17 | 510,57 | 3207,93 | 10290802,62 | 0,00 |
| 18 | 529,08 | 3324,18 | 11050178,70 | 0,00 |
| 19 | 539,34 | 3388,67 | 11483054,73 | 0,00 |
| 20 | 539,34 | 3388,67 | 11483054,73 | 0,00 |
| 21 | 570,21 | 3582,61 | 12835083,18 | 0,00 |
| 22 | 570,23 | 3582,73 | 12835923,92 | 0,00 |
| 23 | 621,96 | 3907,75 | 15270479,98 | 0,00 |
| 24 | 621,96 | 3907,75 | 15270479,98 | 0,00 |

4.2. 3D displacement; U_{total}

Valeur: U_{total}

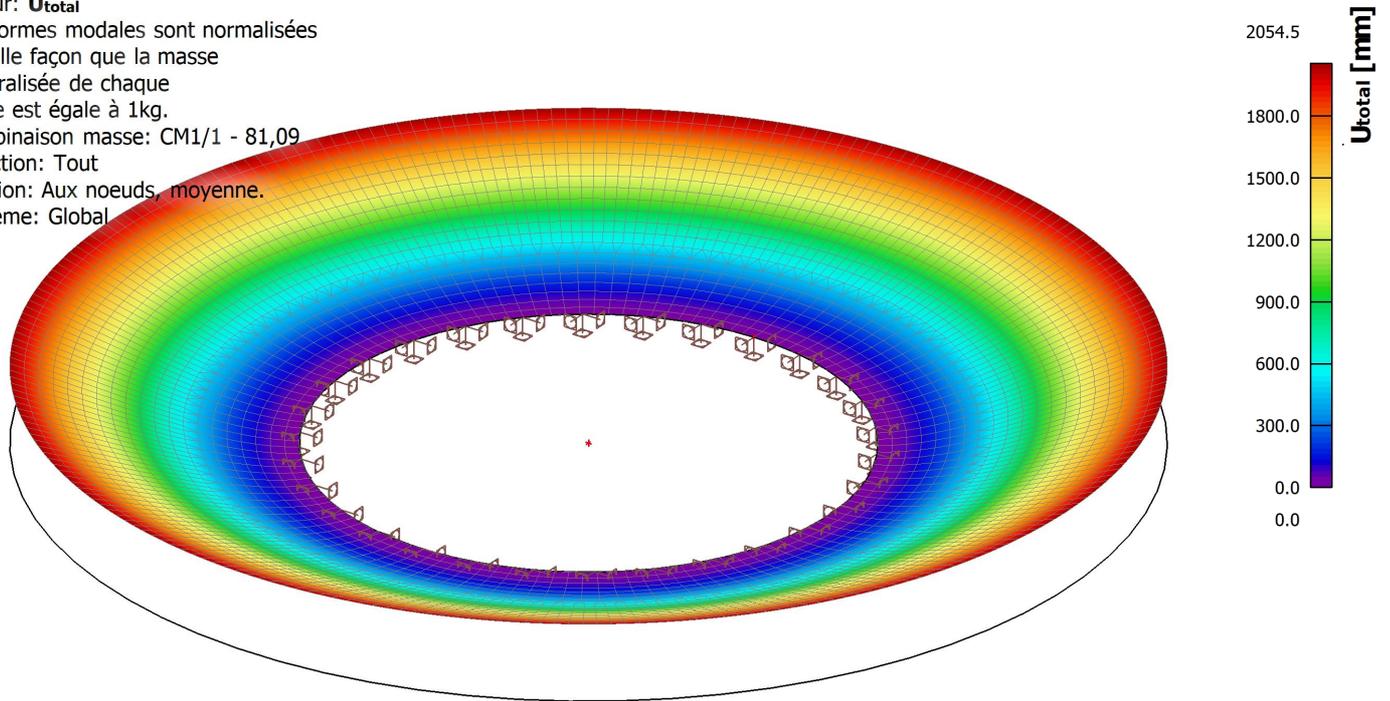
Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.

Combinaison masse: CM1/1 - 81,09

Sélection: Tout

Position: Aux noeuds, moyenne.

Système: Global



4.3. 3D displacement; U_{total}

Valeur: U_{total}

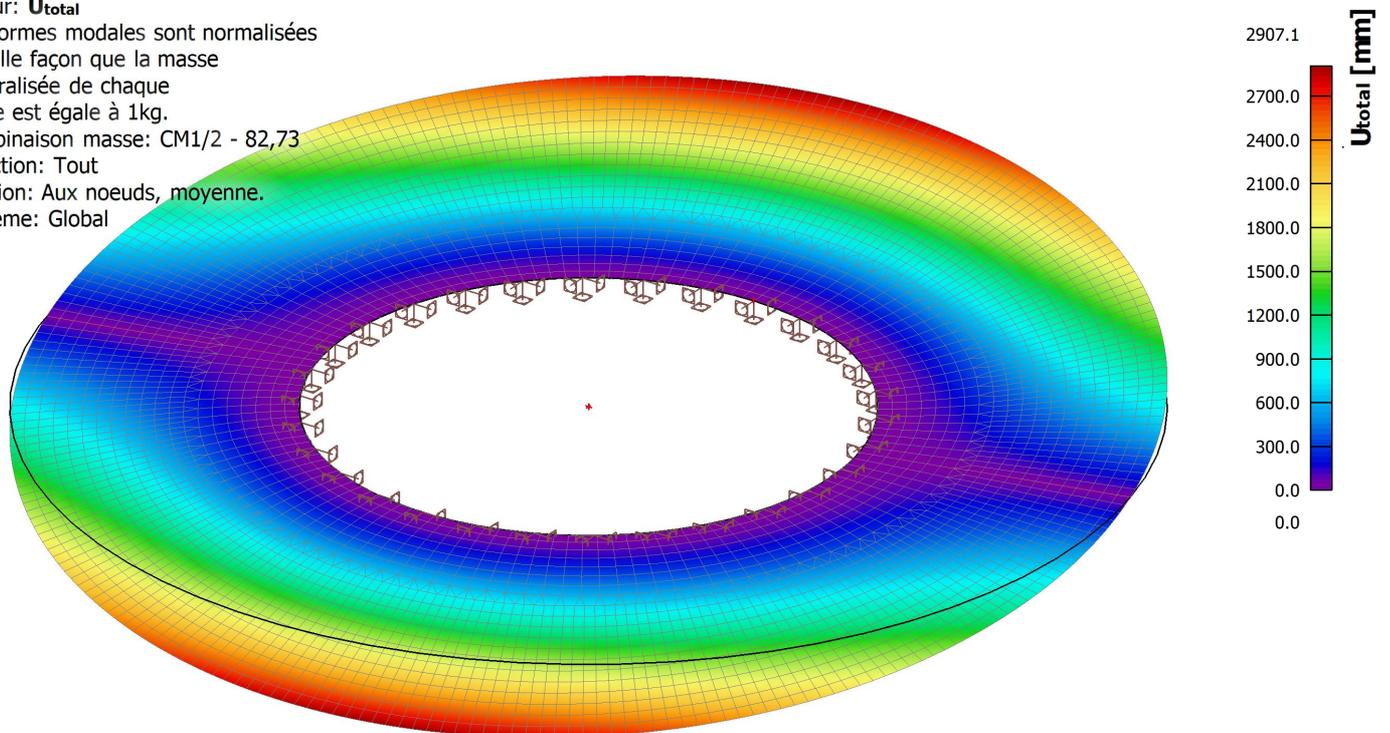
Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.

Combinaison masse: CM1/2 - 82,73

Sélection: Tout

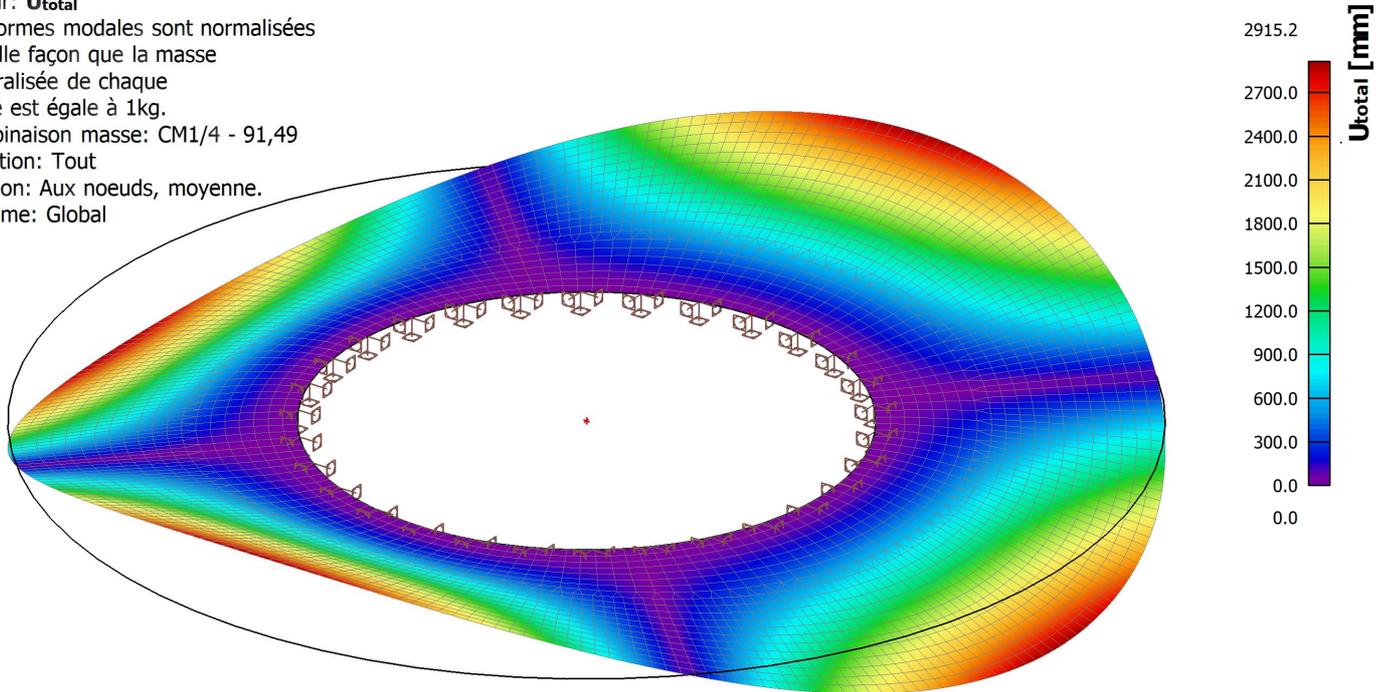
Position: Aux noeuds, moyenne.

Système: Global



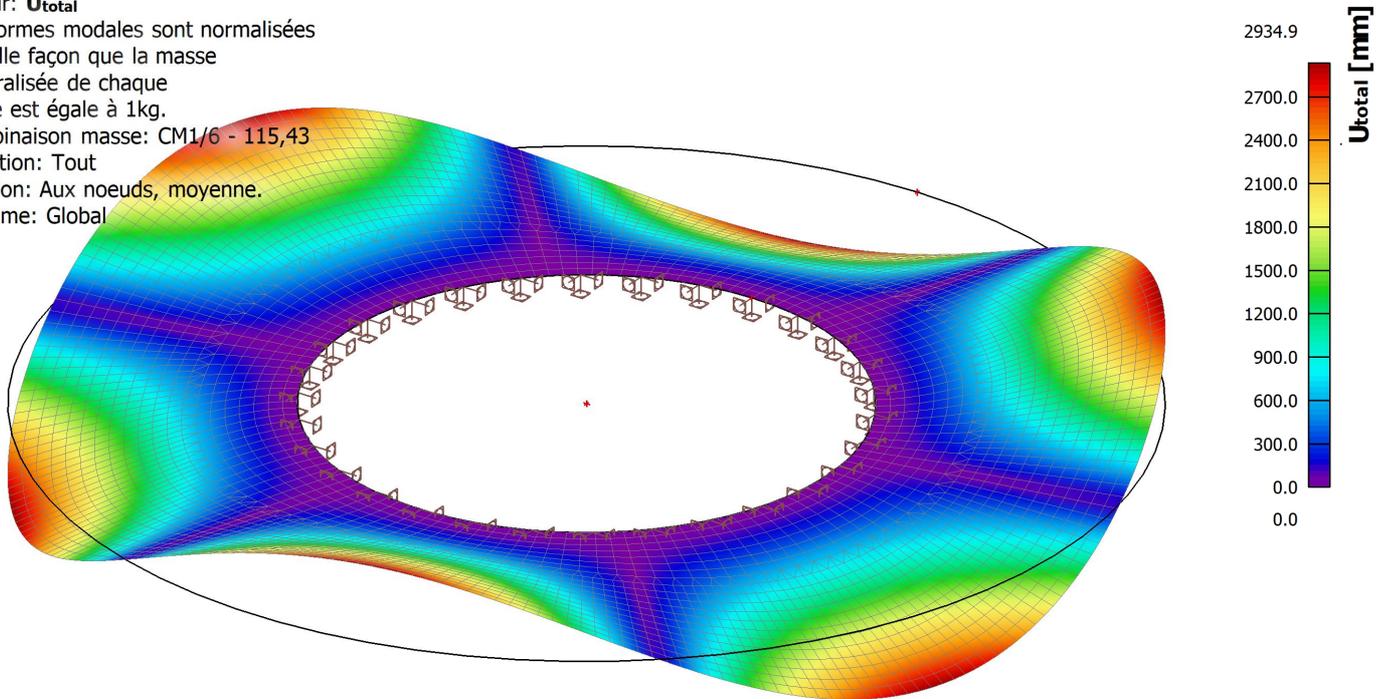
4.4. 3D displacement; U_total

Valeur: U_{total}
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/4 - 91,49
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



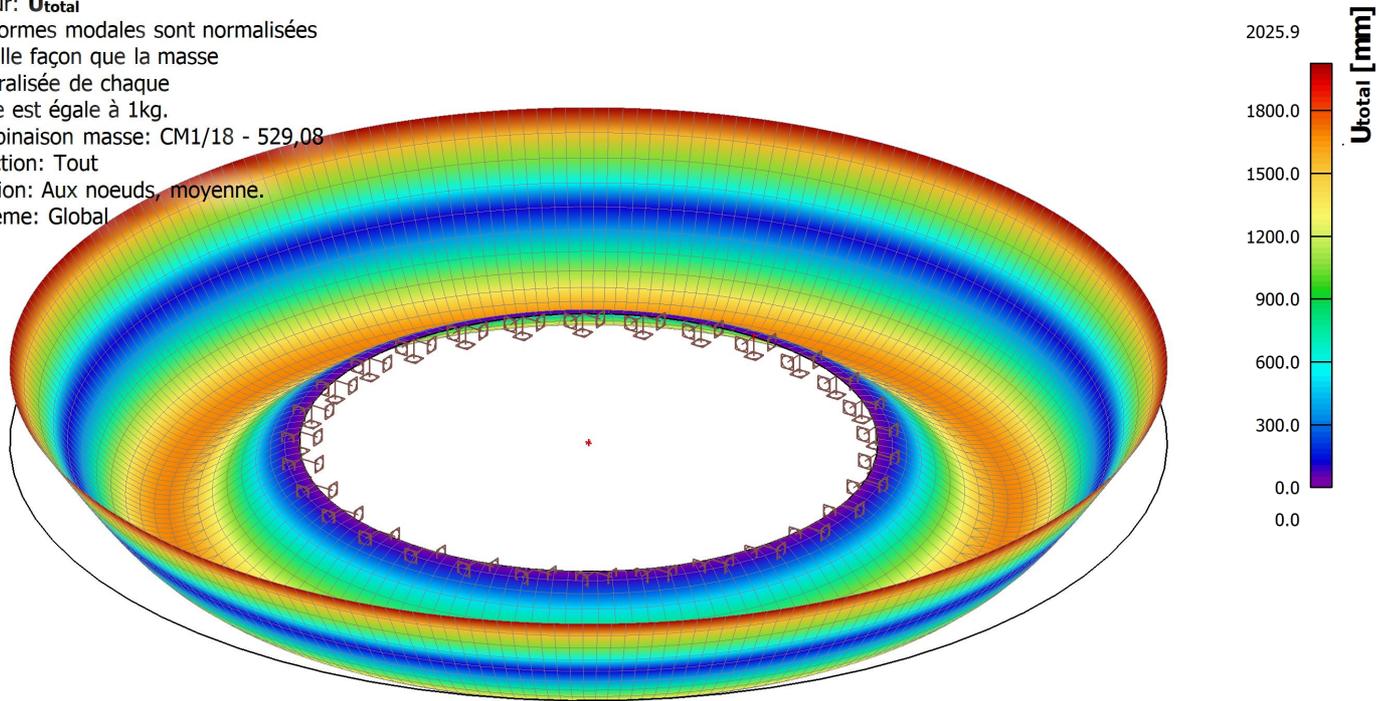
4.5. 3D displacement; U_total

Valeur: U_{total}
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/6 - 115,43
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



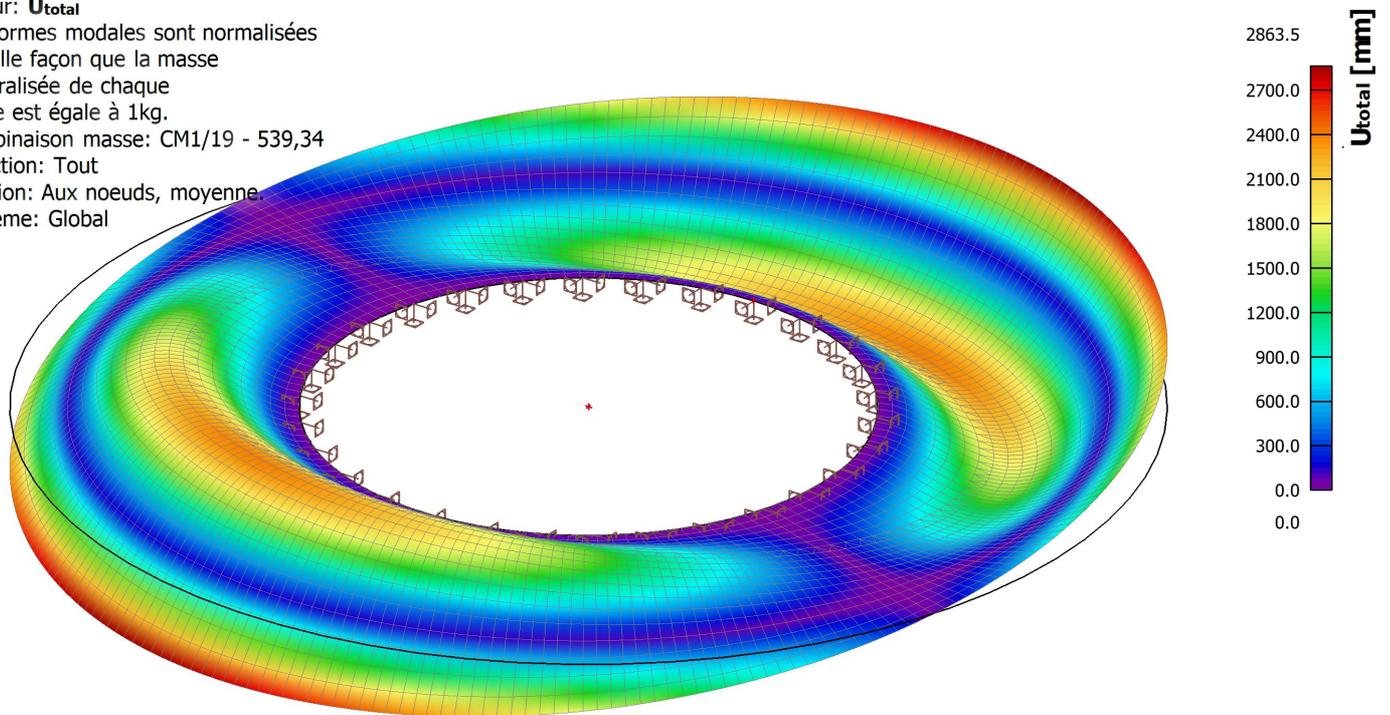
4.6. 3D displacement; U_total

Valeur: U_{total}
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/18 - 529,08
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



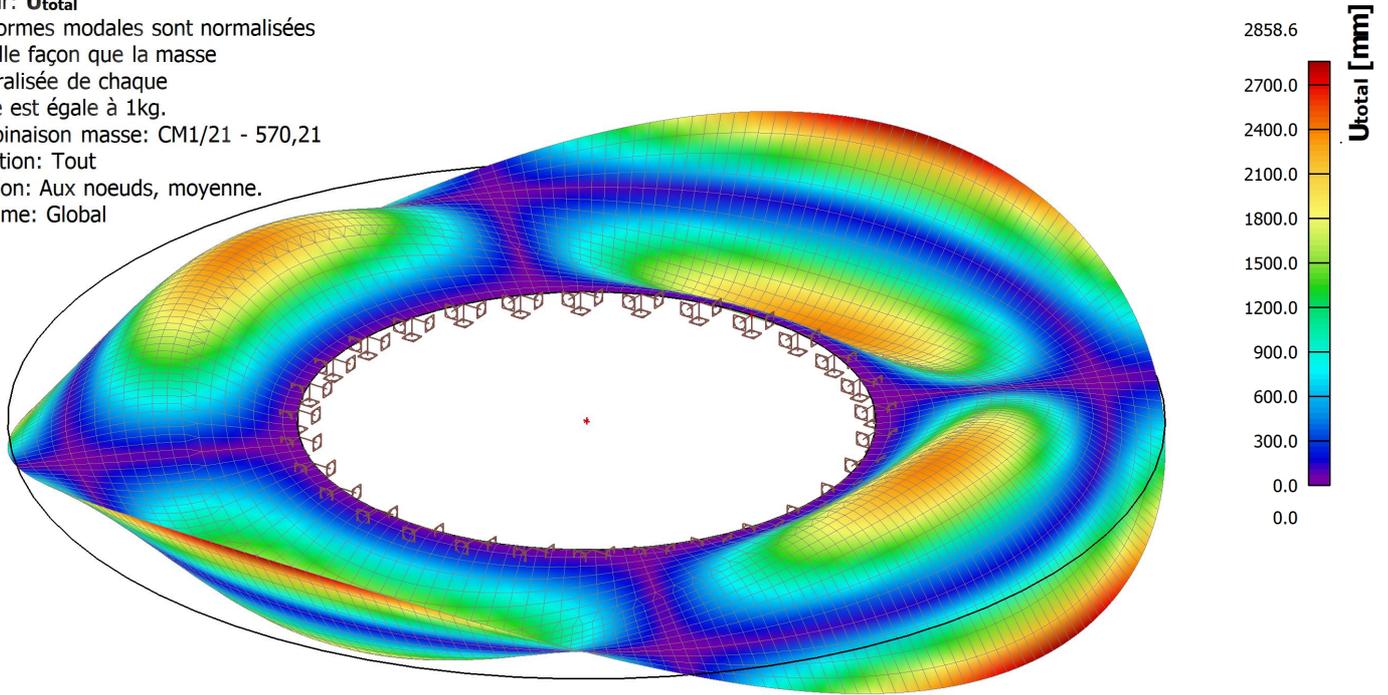
4.7. 3D displacement; U_total

Valeur: U_{total}
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/19 - 539,34
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



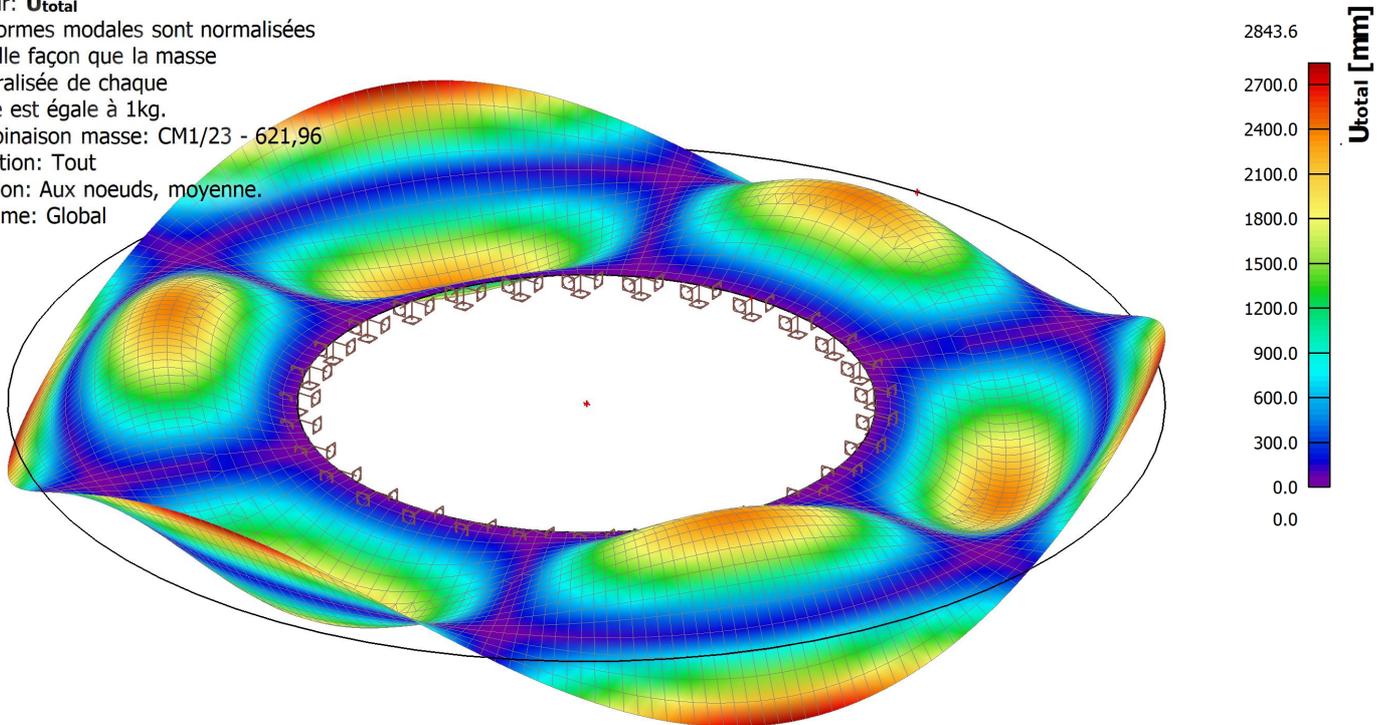
4.8. 3D displacement; U_{total}

Valeur: U_{total}
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/21 - 570,21
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



4.9. 3D displacement; U_{total}

Valeur: U_{total}
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/23 - 621,96
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



5. EXPECTED AFNOR RESULTS

Eigenfrequencies:

f1 = 79.26 Hz

f2 = 81.09 Hz

f4 = 89.63 Hz

f6 = 112.79 Hz

f18 = 518.85 Hz

f19 = 528.61 Hz

f21 = 559.09 Hz

f23 = 609.70 Hz

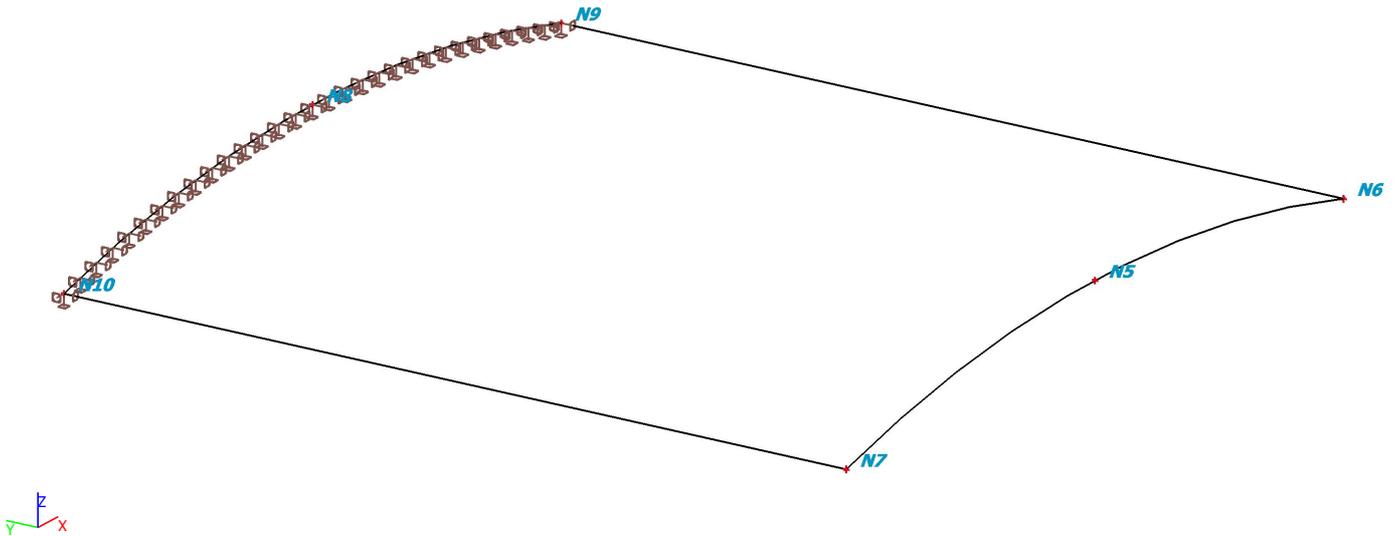
REFERENCE : "Guide de validation des progiciels de calcul de structures" AFNOR, 1990

1. TESTCASE DESCRIPTION

Modal analysis of a cantilever curve shell.

2. MODEL

2.1. Analysis model



2.2. Nodes

| Name | Coord X | Coord Y | Coord Z |
|------|---------|---------|---------|
| N5 | 0,000 | 0,000 | 0,610 |
| N6 | 0,151 | 0,000 | 0,591 |

| Name | Coord X | Coord Y | Coord Z |
|------|---------|---------|---------|
| N7 | -0,151 | 0,000 | 0,591 |
| N8 | 0,000 | 0,305 | 0,610 |

| Name | Coord X | Coord Y | Coord Z |
|------|---------|---------|---------|
| N9 | 0,151 | 0,305 | 0,591 |
| N10 | -0,151 | 0,305 | 0,591 |

2.3. 2D members

| Name | Layer | Type | Element type | Material | Thickness type | Th. [mm] |
|------|---------|------------|--------------|----------|----------------|----------|
| D3 | Calque1 | coque (98) | Standard | Material | constant | 3,0 |

2.4. Supports on 2D member edge

| Name | 2D member | Orig | Pos x ₁ | X | Y | Z | Rx | Ry | Rz |
|------|-----------|------------|--------------------|-------|-------|-------|-------|-------|-------|
| | Edge | Coor | Pos x ₂ | | | | | | |
| Sle1 | D3 | From start | 0.000 | Rigid | Rigid | Rigid | Rigid | Rigid | Rigid |
| | 2 | Rela | 1.000 | | | | | | |

2.5. Materials

Steel EC3

| Name | ρ [kg/m ³] | E_{mod} [MPa] | μ | Limit inférieure [mm] | Limite supérieure [mm] | F_y [MPa] | F_u [MPa] | Colour |
|----------|-----------------------------|-----------------|-----------------|-----------------------|------------------------|-------------|-------------|--------|
| | | G_{mod} [MPa] | α [m/mK] | | | | | |
| Material | 7857,20 | 2,0685e+05 | 0.3 | 0,0 | 40,0 | 235,0 | 360,0 | ■ |
| | | 7,9558e+04 | 0,01e-003 | 40,0 | 80,0 | 215,0 | 360,0 | |

3. LOAD and MASS

3.1. Mass groups

| Name | Load case |
|------|--------------------|
| MG1 | LC1 - Poids propre |

4. RESULTS

4.1. Eigen frequencies

| N | f [Hz] | ω [1/s] | ω^2 [1/s ²] | T [s] |
|-------------------------------|-----------|-------------------|-----------------------------------|----------|
| Mass combination : CM1 | | | | |
| 1 | 85,78 | 538,96 | 290473,04 | 0,01 |
| 2 | 138,32 | 869,07 | 755290,44 | 0,01 |
| 3 | 246,33 | 1547,71 | 2395393,73 | 0,00 |
| 4 | 341,59 | 2146,22 | 4606279,85 | 0,00 |
| 5 | 384,96 | 2418,71 | 5850163,98 | 0,00 |
| 6 | 526,42 | 3307,52 | 10939663,66 | 0,00 |

4.2. 3D displacement; U_{total}

Valeur: **U_{total}**

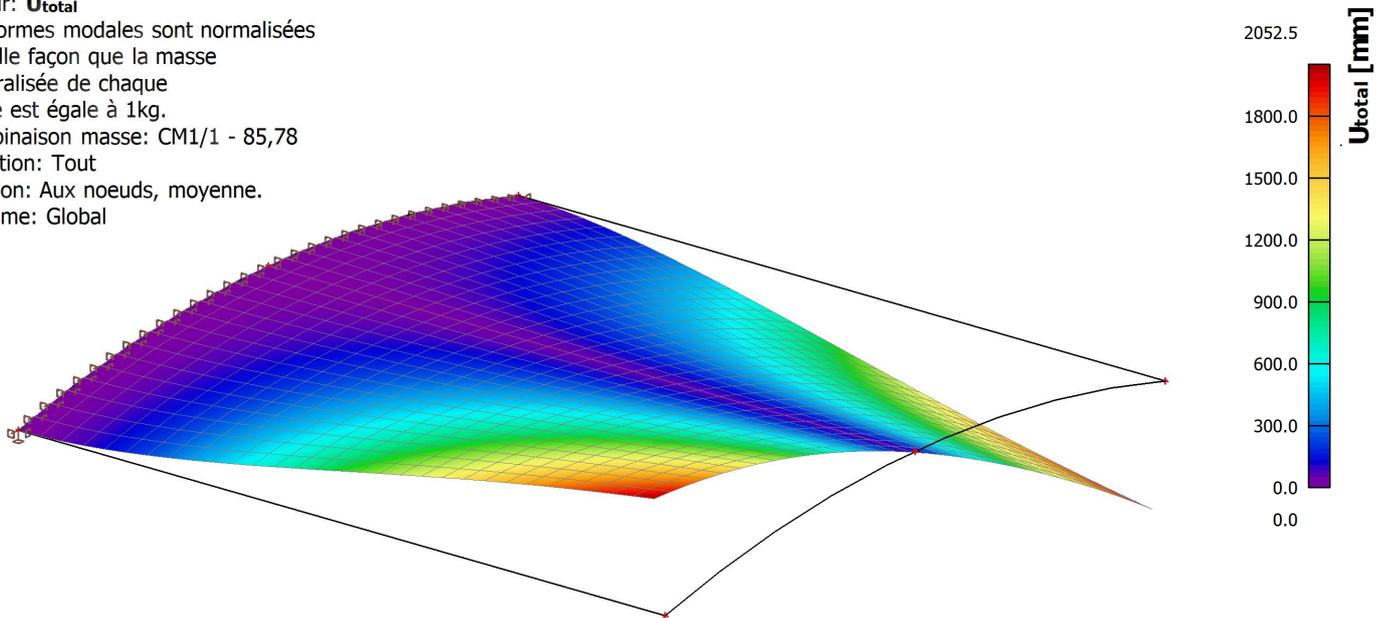
Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.

Combinaison masse: CM1/1 - 85,78

Sélection: Tout

Position: Aux noeuds, moyenne.

Système: Global



4.3. 3D displacement; U_{total}

Valeur: **U_{total}**

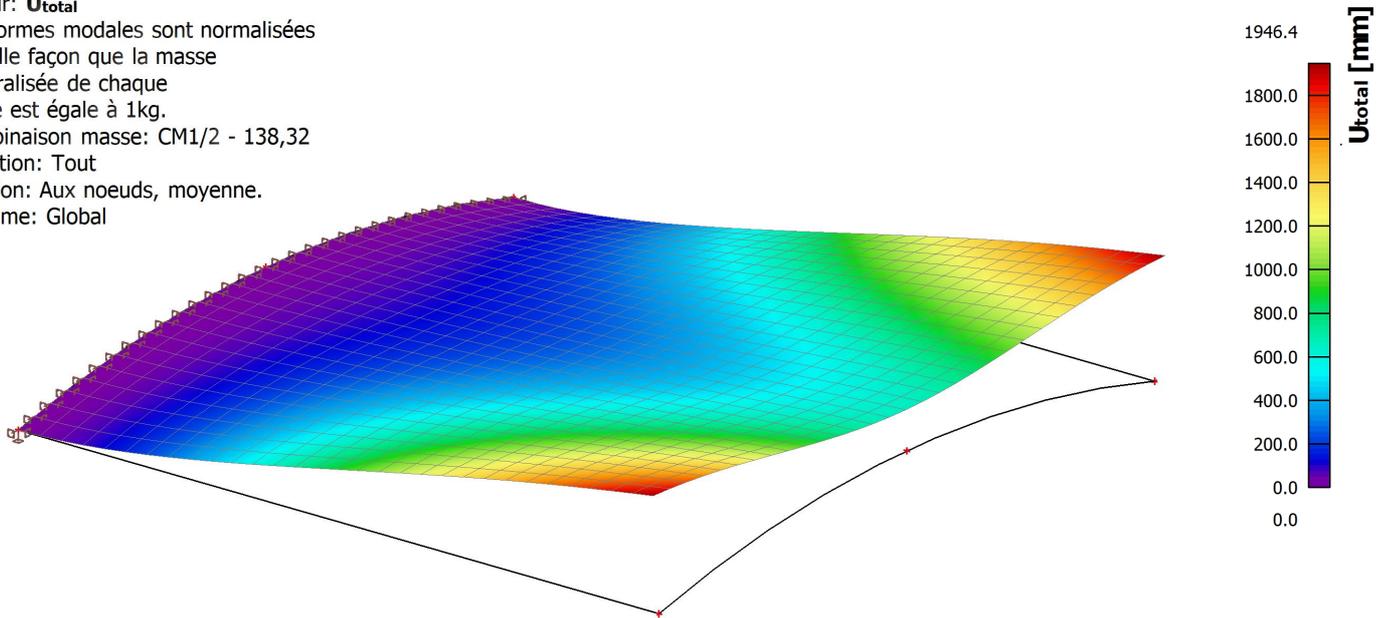
Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.

Combinaison masse: CM1/2 - 138,32

Sélection: Tout

Position: Aux noeuds, moyenne.

Système: Global



4.4. 3D displacement; U_{total}

Valeur: **U_{total}**

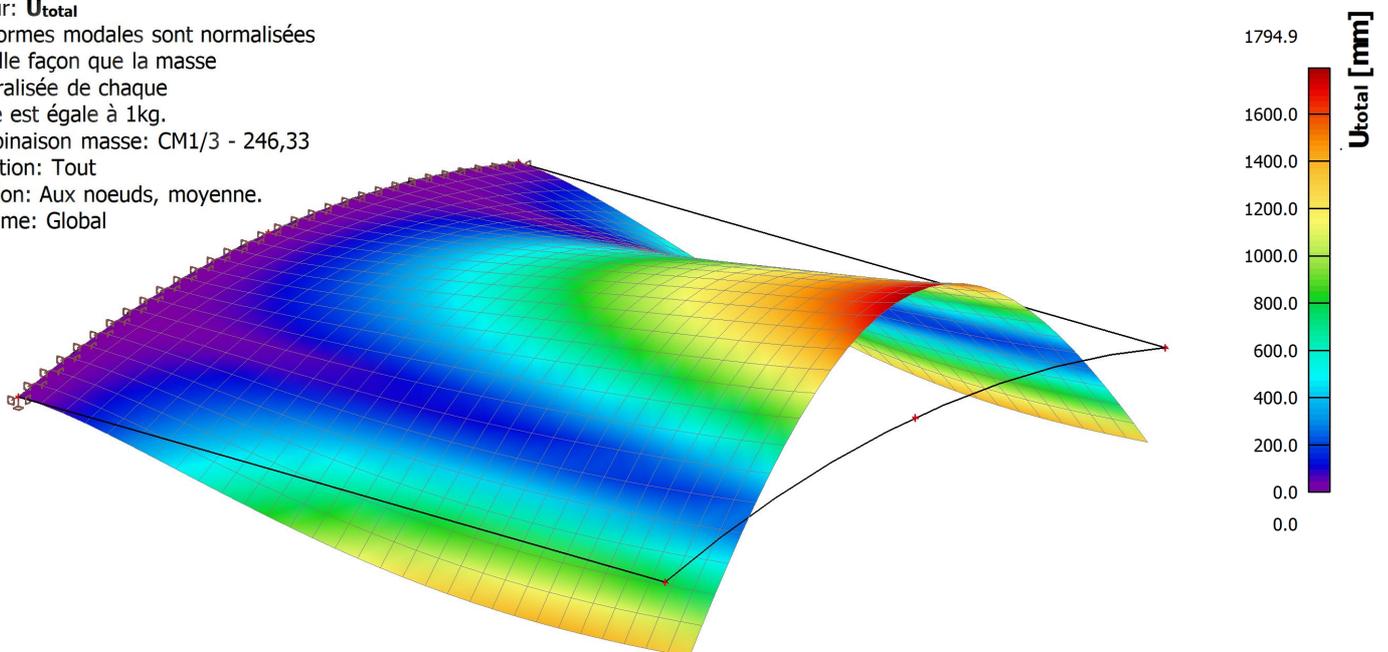
Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.

Combinaison masse: CM1/3 - 246,33

Sélection: Tout

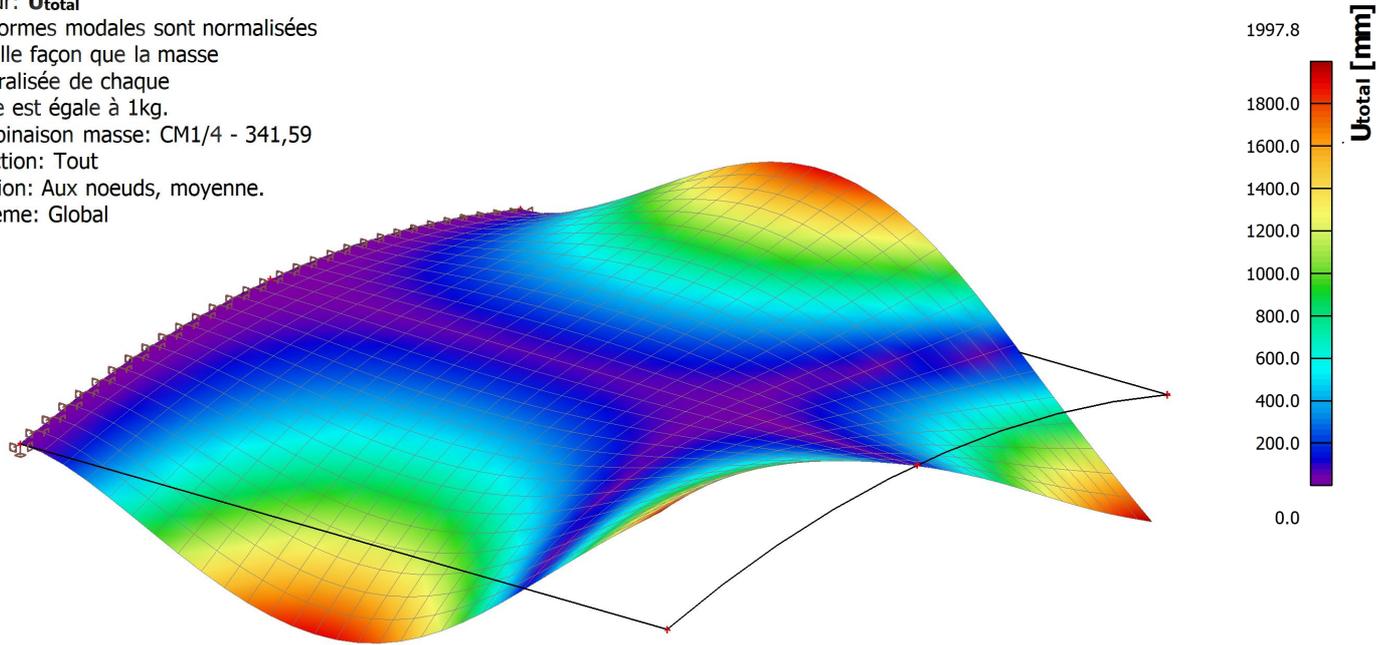
Position: Aux noeuds, moyenne.

Système: Global



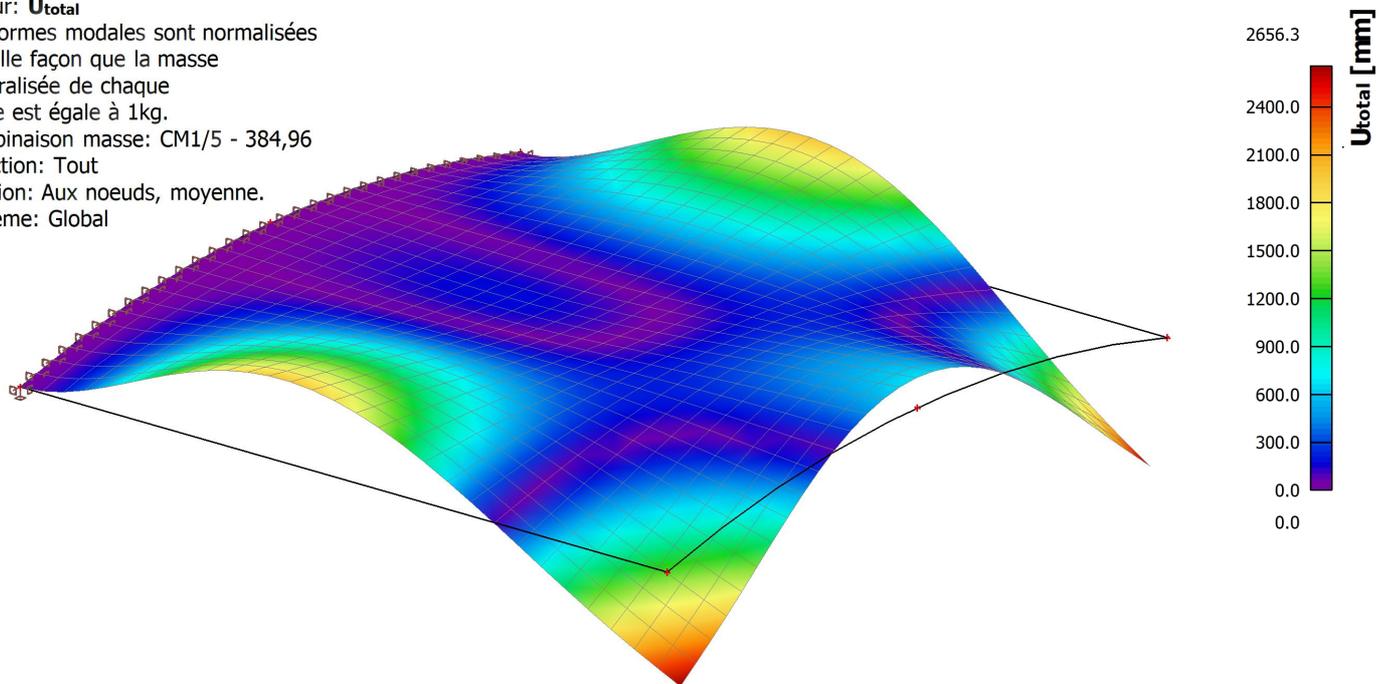
4.5. 3D displacement; U_total

Valeur: U_{total}
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/4 - 341,59
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



4.6. 3D displacement; U_total

Valeur: U_{total}
 Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
 Combinaison masse: CM1/5 - 384,96
 Sélection: Tout
 Position: Aux noeuds, moyenne.
 Système: Global



4.7. 3D displacement; U_{total}

Valeur: U_{total}

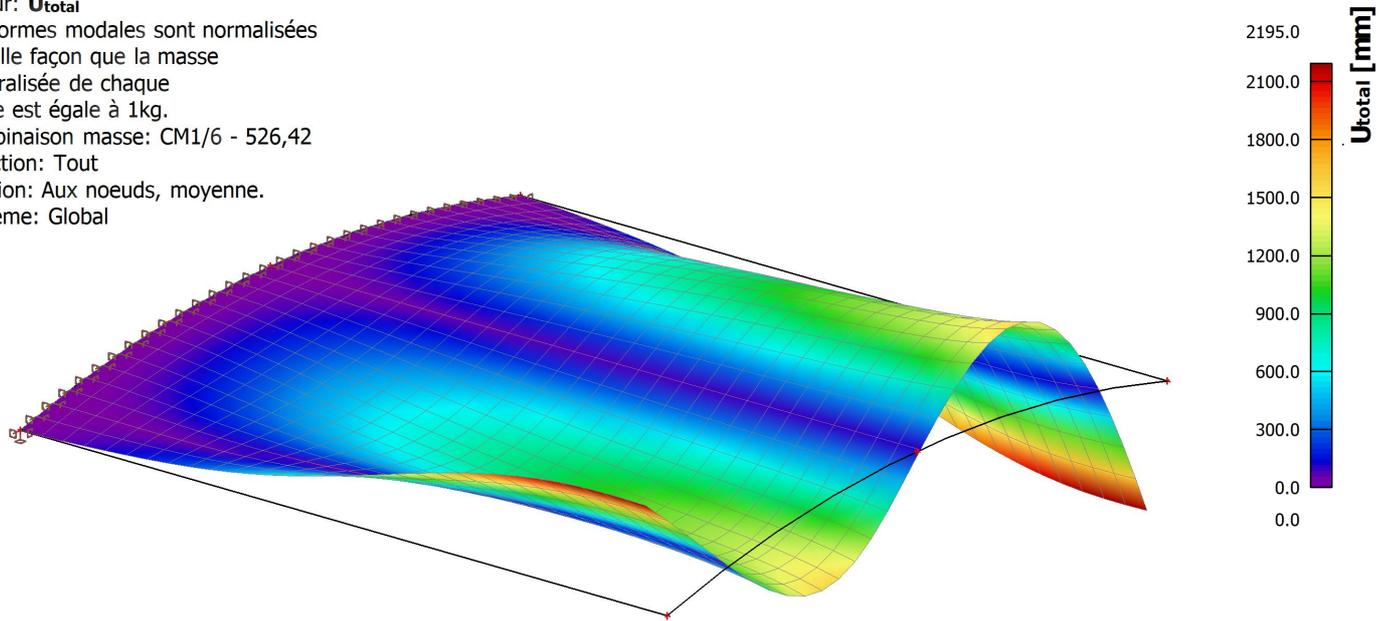
Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.

Combinaison masse: CM1/6 - 526,42

Sélection: Tout

Position: Aux noeuds, moyenne.

Système: Global



5. EXPECTED AFNOR RESULTS

Eigenfrequencies:

f1 = 85.6 Hz

f2 = 134.5 Hz

f3 = 259.0 Hz

f4 = 351.0 Hz

f5 = 395.0 Hz

f6 = 531.0 Hz

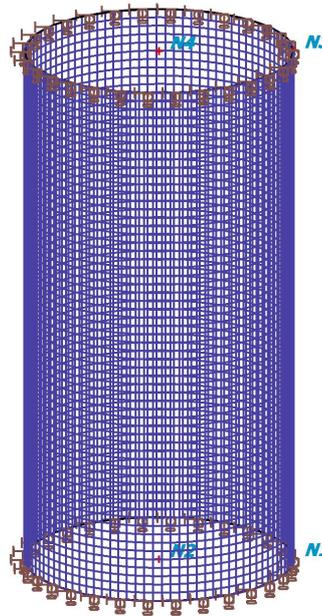
REFERENCE : "Guide de validation des progiciels de calcul de structures" AFNOR, 1990

1. TESTCASE DESCRIPTION

Modal analysis of a thin cylinder fixed at both ends.

2. MODEL

2.1. Analysis model



2.2. Nodes

| Name | Coord X [m] | Coord Y [m] | Coord Z [m] |
|------|-------------|-------------|-------------|
| N1 | 0,076 | 0,000 | 0,000 |
| N2 | 0,000 | 0,000 | 0,000 |
| N3 | 0,076 | 0,000 | 0,305 |
| N4 | 0,000 | 0,000 | 0,305 |

2.3. 2D members

| Name | Layer | Type | Element type | Material | Thickness type | Th. [mm] |
|------|--------|------------|--------------|----------|----------------|----------|
| S1 | Layer1 | voile (80) | Standard | Material | constant | 0 |

2.4. Supports on 2D member edge

| Name | 2D member Edge | Orig Coor | Pos x ₁ Pos x ₂ | X | Y | Z | Rx | Ry | Rz |
|------|----------------|--------------------|---------------------------------------|-------|-------|-------|-------|-------|-------|
| Sle1 | S1 3 | From start Rela | 0,000 1,000 | Rigid | Rigid | Rigid | Rigid | Rigid | Rigid |
| Sle2 | S1 1 | From start Rela | 0,000 1,000 | Rigid | Rigid | Rigid | Rigid | Rigid | Rigid |

2.5. Materials

Steel EC3

| Name | ρ [kg/m ³] | E_{mod} [MPa] | μ | Limit inférieure [mm] | Limite supérieure [mm] | F_y [MPa] | F_u [MPa] | Colour |
|----------|--------------------------------|--------------------|--------------------|--------------------------|---------------------------|----------------|----------------|--------|
| | | G_{mod} [MPa] | α [m/mK] | | | | | |
| Material | 7850,00 | 2,0600e+05 | 0,3 | 0 | 40 | 235,0 | 360,0 | ■ |
| | | 7,9231e+04 | 0,01e-003 | 40 | 80 | 215,0 | 360,0 | |

3. LOAD and MASS

3.1. Mass groups

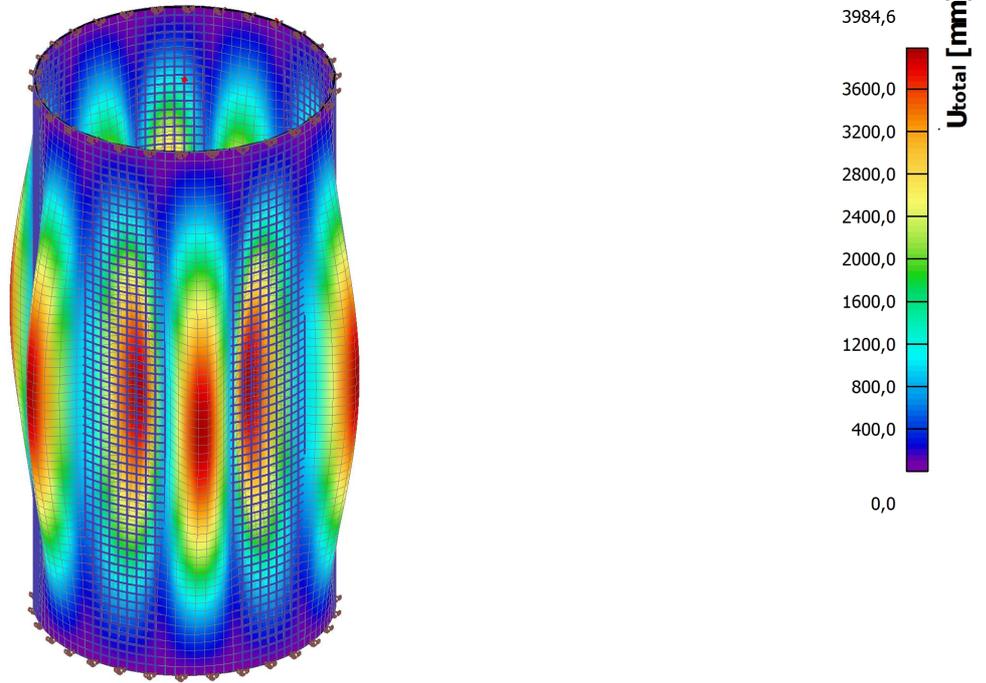
| Name | Load case |
|------|-------------------|
| MG1 | LC1 - Self weight |

4. RESULTS

4.1. 3D displacement; m=1, n=6

Valeur: U_{total}

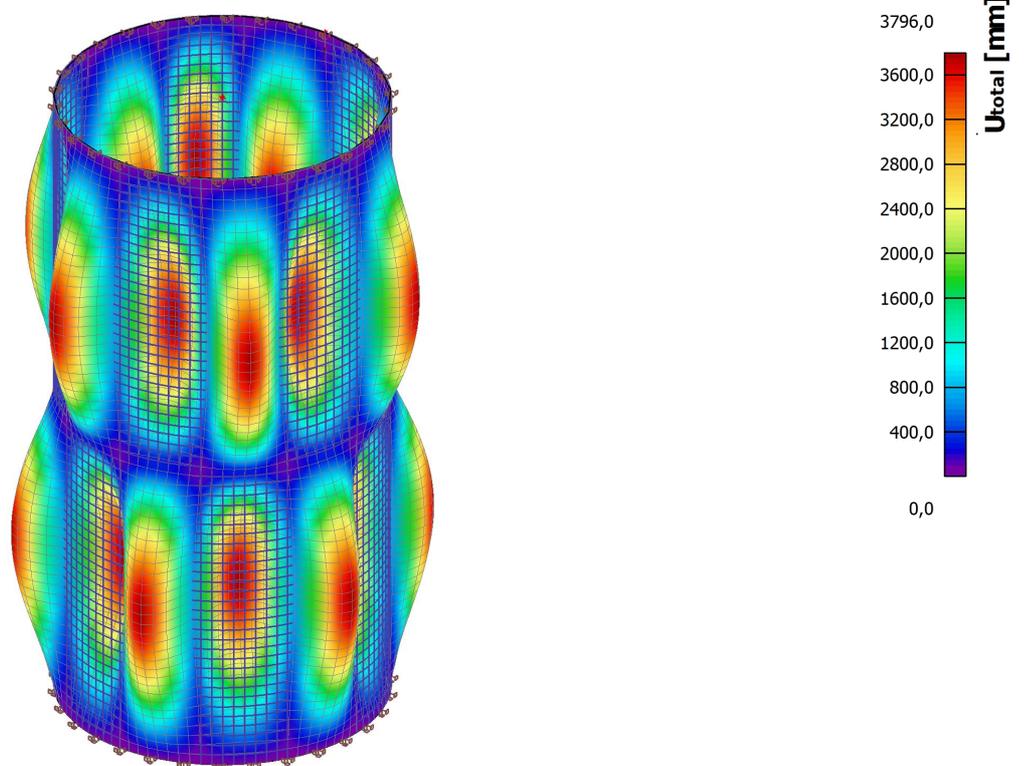
Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
Combinaison masse: CM1/1 - 535,48
Sélection: Tout
Position: Aux noeuds, moyenne.
Système: Global



4.2. 3D displacement; m=2, n=6

Valeur: U_{total}

Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.
Combinaison masse: CM1/19 - 1024,62
Sélection: Tout
Position: Aux noeuds, moyenne.
Système: Global



4.3. 3D displacement; m=3, n=6

Valeur: U_{total}

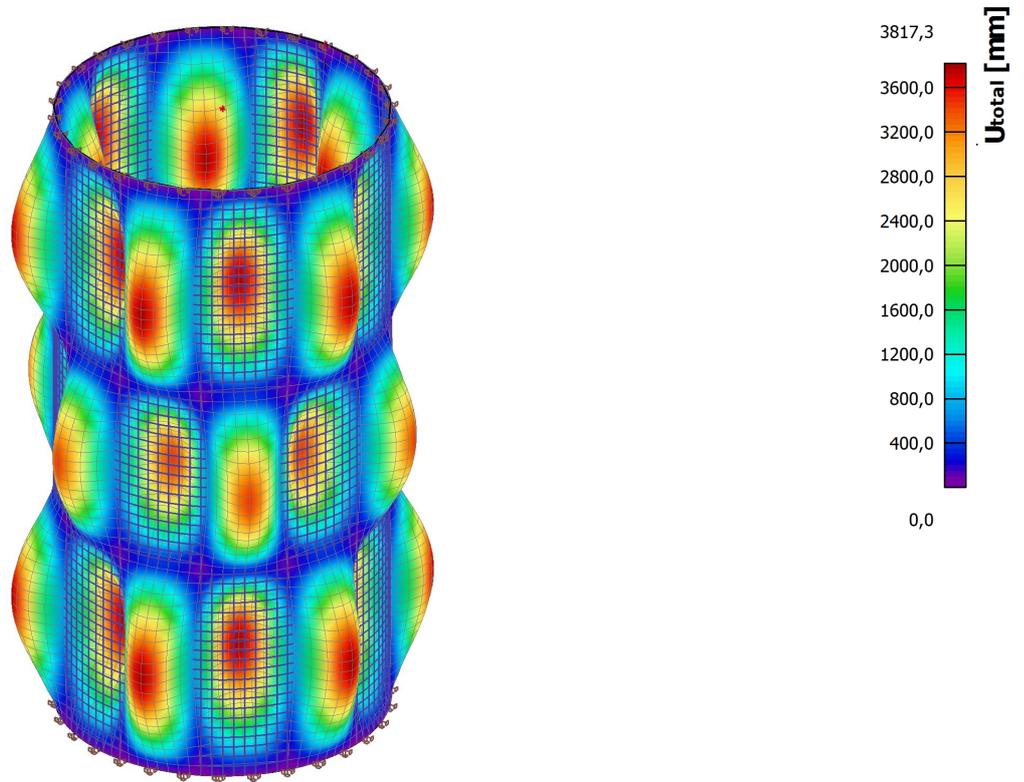
Les formes modales sont normalisées de telle façon que la masse généralisée de chaque mode est égale à 1kg.

Combinaison masse: CM1/55 - 1727,51

Sélection: Tout

Position: Aux noeuds, moyenne.

Système: Global



5. EXPECTED AFNOR RESULTS

Eigenfrequencies (m=1, n=6)

f = 538.5 Hz

Eigenfrequencies (m=2, n=6)

f = 1041.5 Hz

Eigenfrequencies (m=3, n=6)

f = 1764.9 Hz

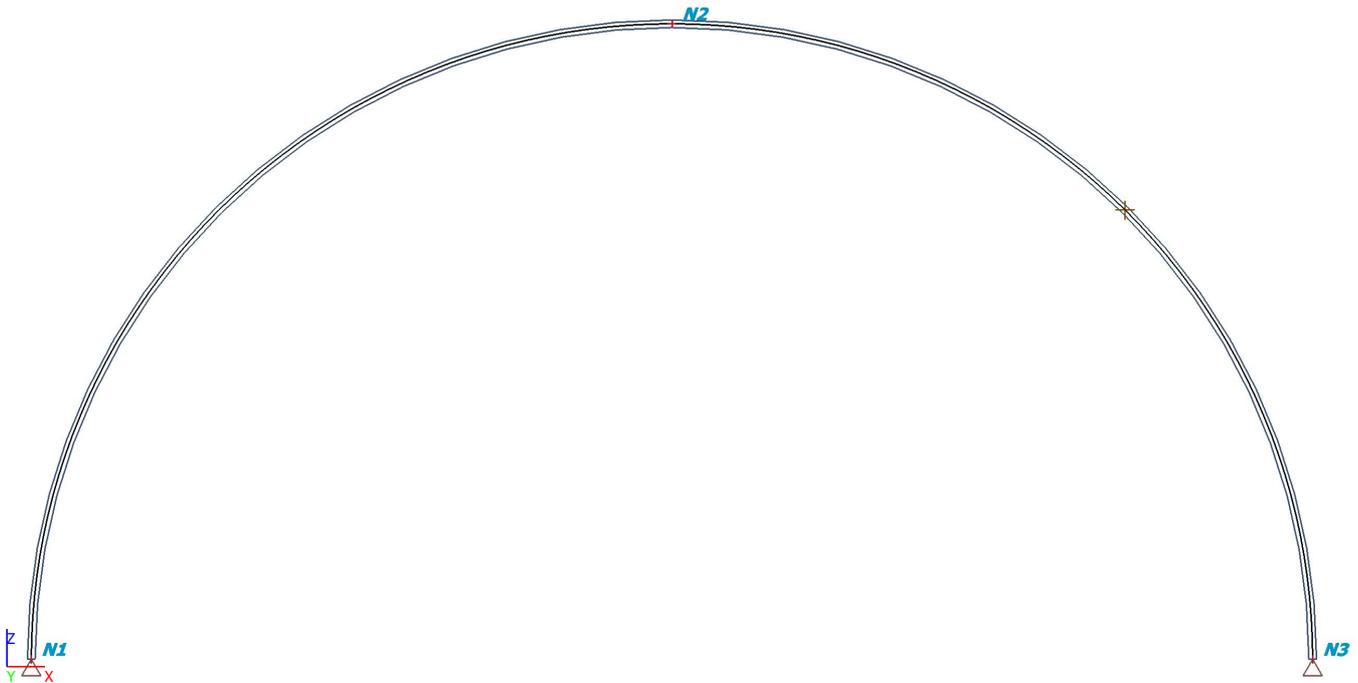
REFERENCE : "Guide de validation des progiciels de calcul de structures" AFNOR, 1990

1. TESTCASE DESCRIPTION

Arch with 2 pinned supports
Specification: Thin-walled arch - Thermal gradient - Pinned supports

2. MODEL

2.1. Analysis model



2.2. Nodes

| Name | Coord X [m] | Coord Z [m] |
|------|-------------|-------------|
| N1 | 0,000 | 0,000 |
| N2 | 10,000 | 10,000 |
| N3 | 20,000 | 0,000 |

2.3. Members

| Name | Cross-section | Material | Length [m] | Beg. node | End node | Type |
|------|--|----------|------------|-----------|----------|-------------|
| B1 | CS1 - Rectangulaire plein (120,0; 120,0) | S 355 | 31,416 | N1 | N3 | general (0) |

2.4. Nodal supports

| Name | Node | System | Type | X | Z | Ry |
|------|------|--------|----------|-------|-------|------|
| Sn1 | N1 | GCS | Standard | Rigid | Rigid | Free |
| Sn2 | N3 | GCS | Standard | Rigid | Rigid | Free |

2.5. Materials

Steel EC3

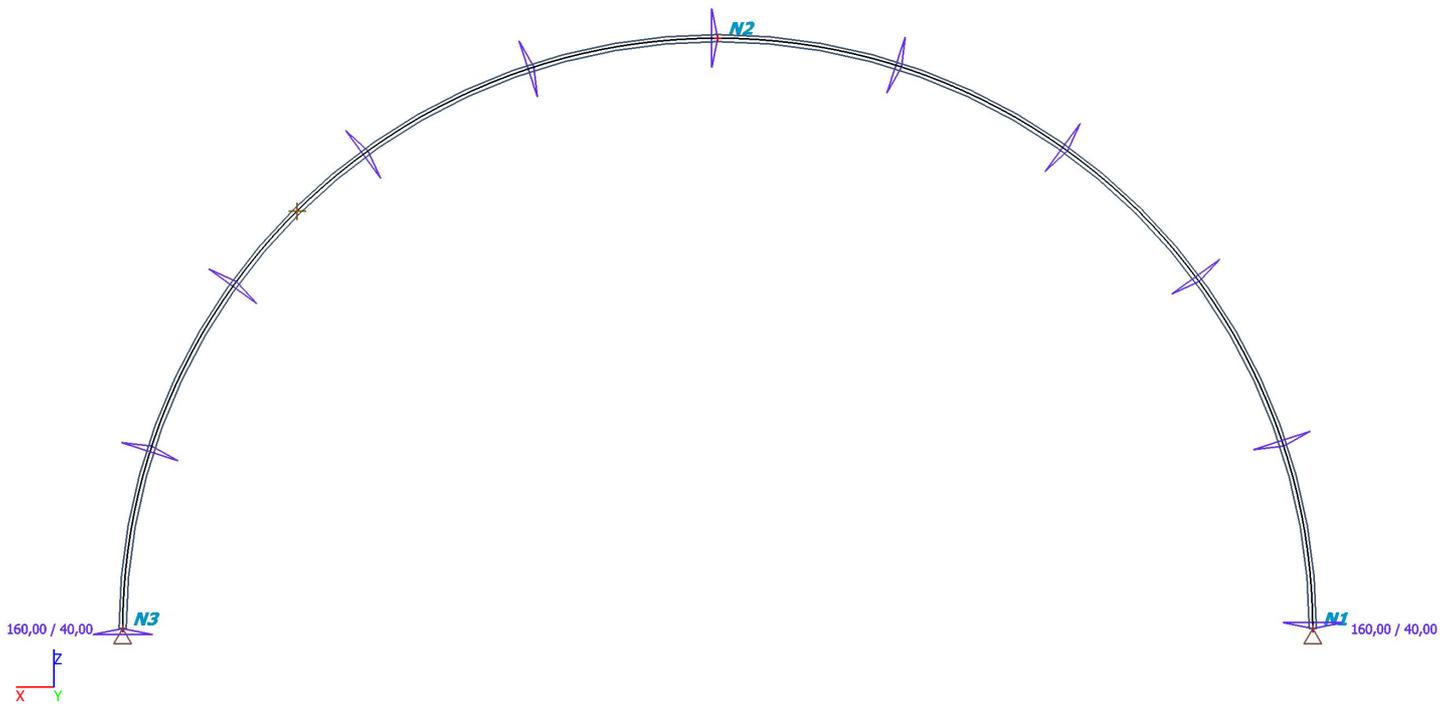
| Name | ρ [kg/m ³] | E_{mod} [MPa] | μ | Limit inférieure [mm] | Limite supérieure [mm] | F_y [MPa] | F_u [MPa] | Colour |
|-------|-----------------------------|-----------------|-----------------|-----------------------|------------------------|-------------|-------------|--------|
| | | G_{mod} [MPa] | α [m/mK] | | | | | |
| S 355 | 7850,00 | 2,0000e+05 | 0.3 | 0,0 | 40,0 | 355,0 | 490,0 | ■ |
| | | 7,6923e+04 | 0,01e-003 | 40,0 | 80,0 | 335,0 | 470,0 | |

3. LOAD

4. Thermal load

| Name | Member | Load case | Pos x ₁ | Coor | Orig | Distribution | +z - Top delta [K] |
|------|--------|-----------|--------------------|------|------------|--------------|-----------------------|
| | | | Pos x ₂ | | | | -z - Bottom delta [K] |
| LT1 | B1 | LC2 | 0.000 | Rela | From start | Linear | 160,00 |
| | | | 1.000 | | | | 40,00 |

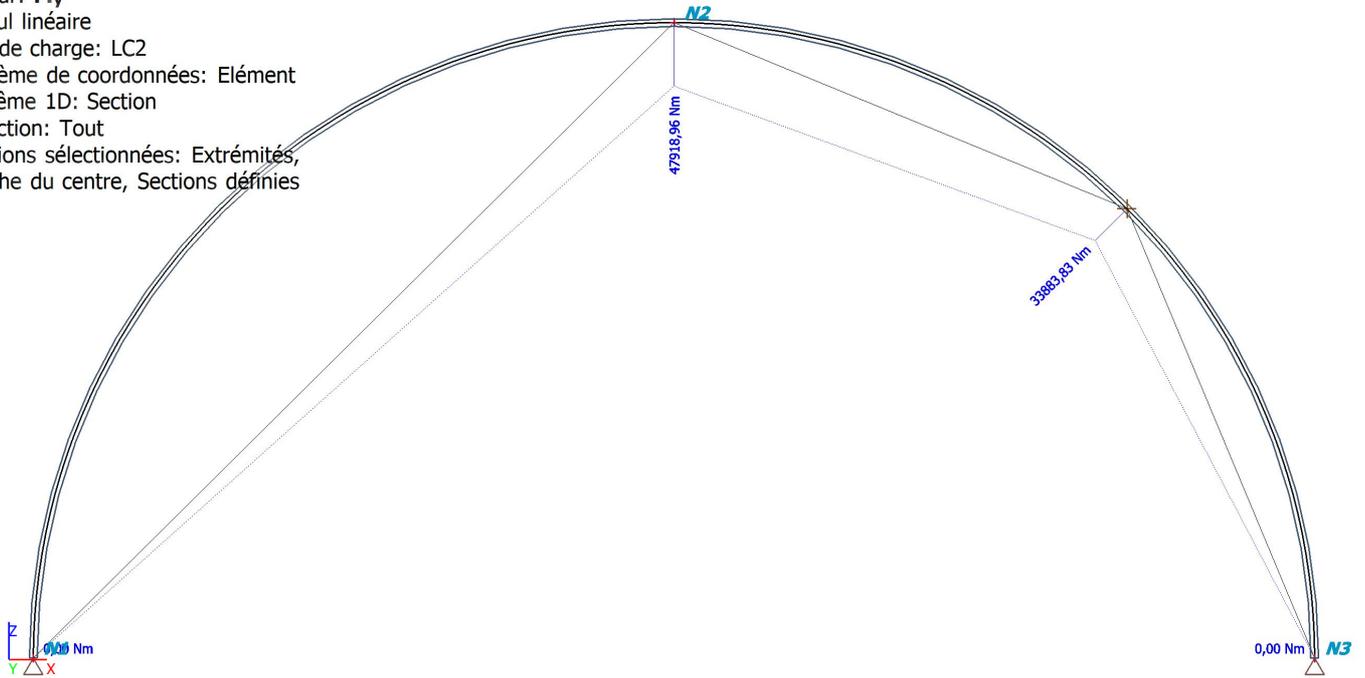
5. LC2



6. RESULTS

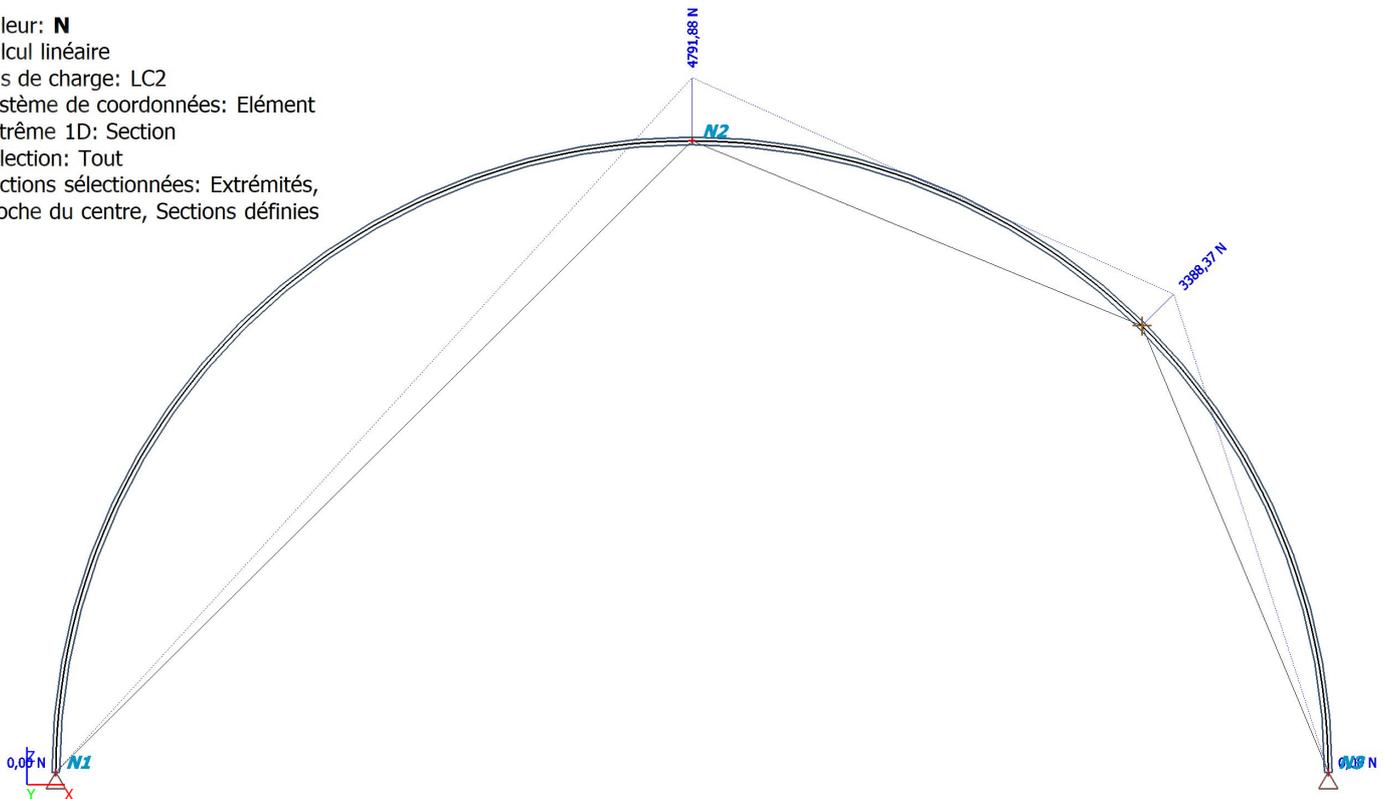
7. 1D internal forces; M_y

Valeur: M_y
 Calcul linéaire
 Cas de charge: LC2
 Système de coordonnées: Elément
 Extrême 1D: Section
 Sélection: Tout
 Sections sélectionnées: Extrémités,
 Proche du centre, Sections définies



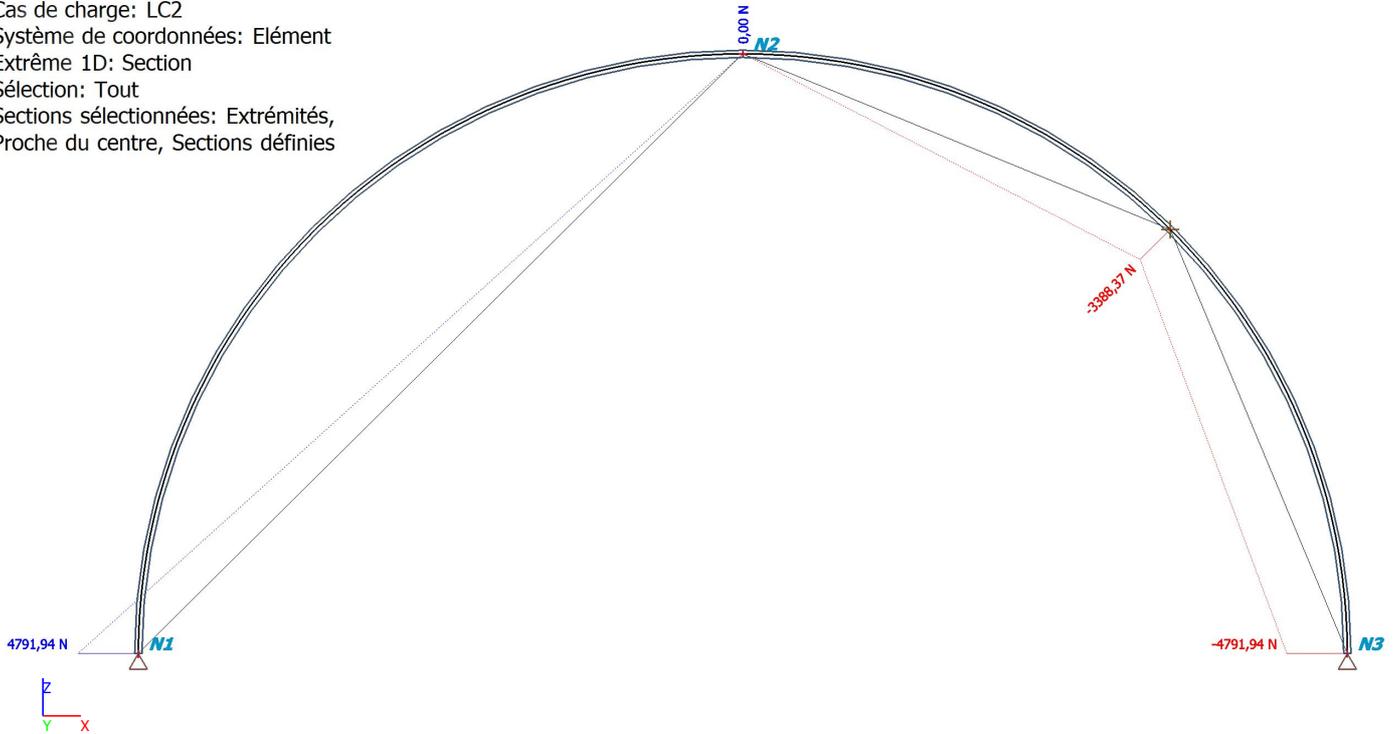
8. 1D internal forces; N

Valeur: N
 Calcul linéaire
 Cas de charge: LC2
 Système de coordonnées: Elément
 Extrême 1D: Section
 Sélection: Tout
 Sections sélectionnées: Extrémités,
 Proche du centre, Sections définies



9. 1D internal forces; V_z

Valeur: V_z
 Calcul linéaire
 Cas de charge: LC2
 Système de coordonnées: Elément
 Extrême 1D: Section
 Sélection: Tout
 Sections sélectionnées: Extrémités,
 Proche du centre, Sections définies



10. 1D internal forces

Linear calculation
 Load case: LC2
 Coordinate system: Member
 Extreme 1D: No
 Selection: All
 Selected sections: Ends, Close to middle, Inputted

| Name | dx [m] | Case | N [N] | V _z [N] | M _y [Nm] |
|------|---------|------|---------|--------------------|---------------------|
| B1 | 0,000 | LC2 | 0,00 | 4791,94 | 0,00 |
| B1 | 15,708- | LC2 | 4791,88 | 0,00 | 47918,96 |
| B1 | 15,708+ | LC2 | 4791,88 | 0,00 | 47918,96 |
| B1 | 23,562- | LC2 | 3388,37 | -3388,37 | 33883,83 |
| B1 | 23,562+ | LC2 | 3388,37 | -3388,37 | 33883,83 |
| B1 | 31,416 | LC2 | 0,00 | -4791,94 | 0,00 |

11. EXPECTED AFNOR RESULTS

For THETA= $\pi/2$ (dx=31,416) :

M = 0 Nm

N = 0 N

V = -4792 N

For THETA= $\pi/4$ (dx=23,562) :

M = 33883 Nm

N = -3388 N

V = -3388 N

For THETA= 0 (dx=15,708):

M = 47918 Nm

N = -4792 N

V = 0N

REFERENCE : "Guide de validation des progiciels de calcul de structures" AFNOR, 1990

1. TESTCASE DESCRIPTION

Thin plate deformed according to spherical curve under thermal gradient

2. MODEL

2.1. Analysis model



2.2. 2D members

| Name | Layer | Type | Element type | Material | Thickness type | Th. [mm] |
|------|---------|------------|--------------|----------|----------------|----------|
| D1 | Calque1 | dalle (90) | Standard | Material | constant | 10,0 |

2.3. Supports on 2D member edge

| Name | 2D member Edge | Orig Coor | Pos x ₁ Pos x ₂ | X | Y | Z | Rx | Ry | Rz |
|------|----------------|------------|---------------------------------------|-------|-------|-------|-------|------|------|
| Sle1 | D1 1 | From start | 0.000 1.000 | Rigid | Rigid | Rigid | Rigid | Free | Free |
| Sle2 | D1 2 | From start | 0.000 1.000 | Rigid | Rigid | Rigid | Rigid | Free | Free |
| Sle3 | D1 3 | From start | 0.000 1.000 | Rigid | Rigid | Rigid | Rigid | Free | Free |
| Sle4 | D1 4 | From start | 0.000 1.000 | Rigid | Rigid | Rigid | Rigid | Free | Free |

2.4. Materials

Steel EC3

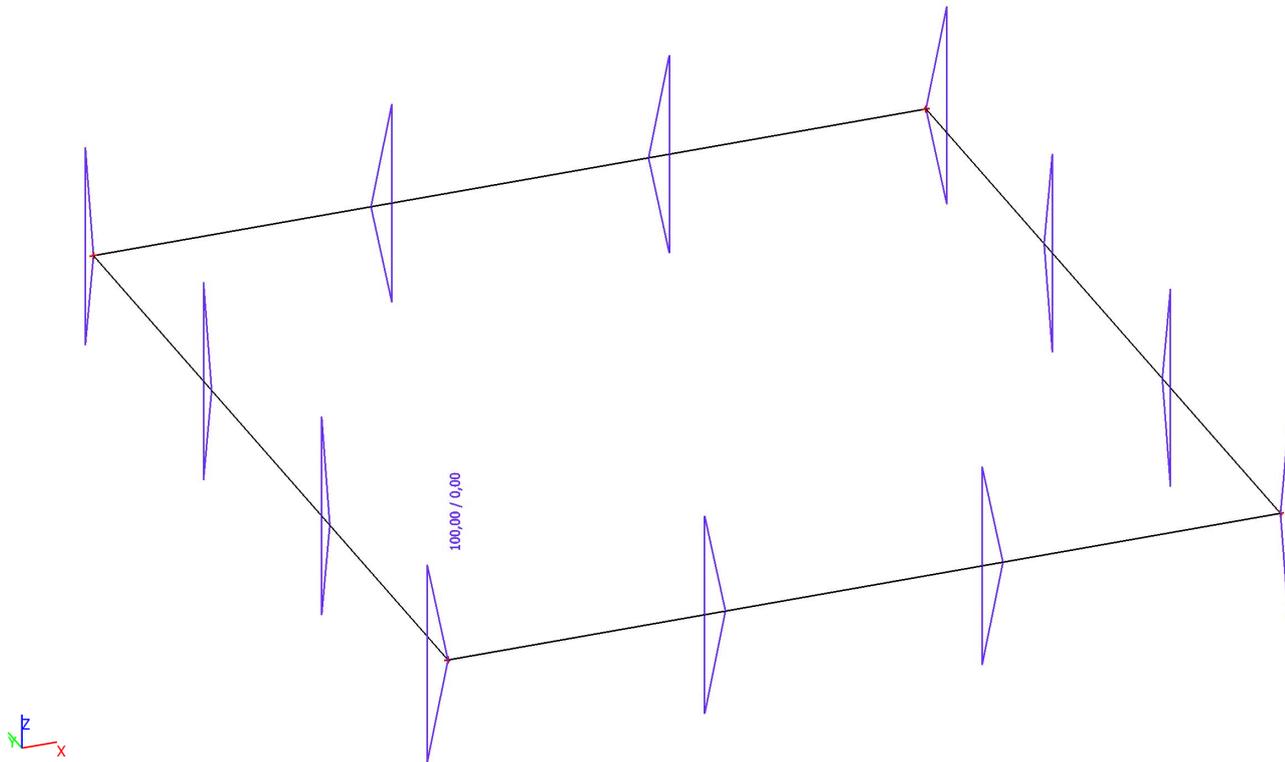
| Name | ρ [kg/m ³] | E_{mod} [MPa] G_{mod} [MPa] | μ α [m/mK] | Limit inférieure [mm] | Limite supérieure [mm] | F_y [MPa] | F_u [MPa] | Colour |
|----------|-----------------------------|------------------------------------|--------------------------|-----------------------|------------------------|------------------|------------------|--------|
| Material | 7850,00 | 2,0000e+05 7,6923e+04 | 0.3 0,01e-003 | 0,0 40,0 | 40,0 80,0 | 235,00 215,00 | 360,00 360,00 | ■ |

3. LOAD

3.1. Thermal load on 2D member

| Name | 2D member | Load case | Distribution | +z - Top delta [K] | -z - Bottom delta [K] |
|------|-----------|-----------|--------------|--------------------|-----------------------|
| ST1 | D1 | LC2 | Linear | 100,00 | 0,00 |

3.2. LC2



4. RESULTS

4.1. 2D internal forces

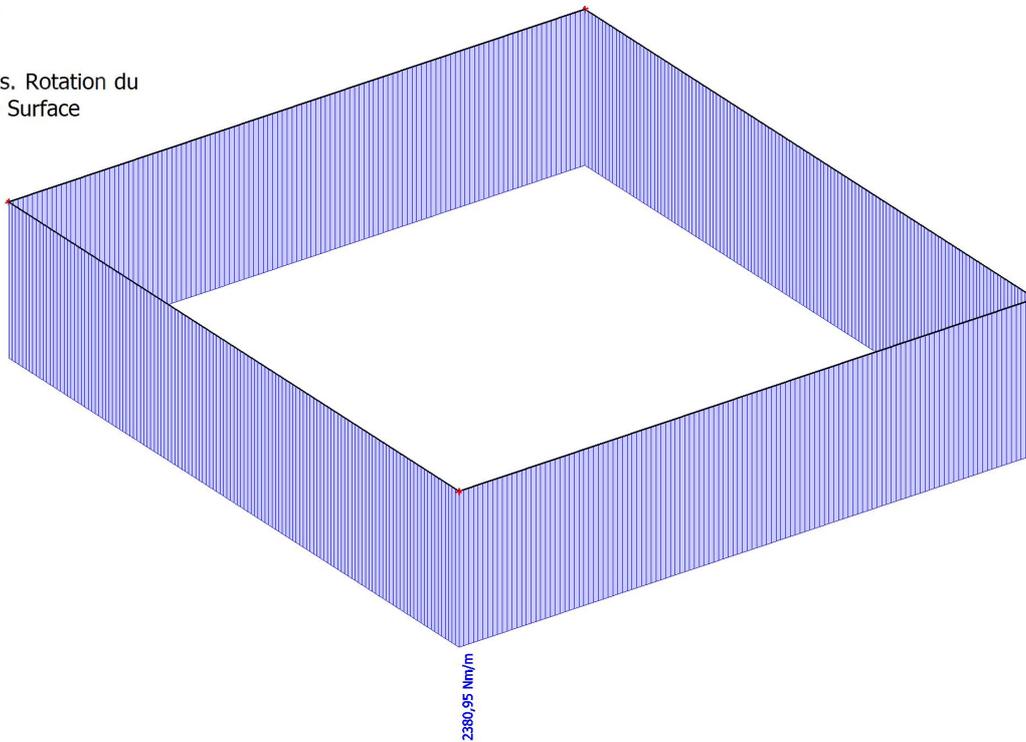
Linear calculation
 Load case: LC2
 Extreme: Global
 Selection: All
 Location: In nodes avg. on macro. System: LCS mesh element

Basic magnitudes

| Name | Mesh | Position [m] | Case | m_x [Nm/m] |
|------|-----------------------|-------------------------|------|----------------|
| D1 | Element: 1 Node: 1 | 0,000 0,000 0,000 | LC2 | 2380,95 |

4.2. 2D internal forces; m_y

Valeur: m_y
 Calcul linéaire
 Cas de charge: LC2
 Extrême: Global
 Sélection: Tout
 Position: Aux centres. Rotation du système plan: SCL - Surface



4.3. 2D stress/strain

Linear calculation

Load case: LC2

Extreme: Global

Selection: All

Location: In nodes avg. on macro. System: LCS mesh element

Membrane stress

| Name | Mesh | Position [m] | Case | σ_{mE} [MPa] | σ_{m1} [MPa] | σ_{m2} [MPa] |
|------|-----------------------|-------------------------|------|---------------------|---------------------|---------------------|
| D1 | Element: 1 Node: 1 | 0,000 0,000 0,000 | LC2 | 142,86 | -142,86 | -142,86 |

4.4. 2D stress/strain; σ_{m1}

Valeur: σ_{m1}

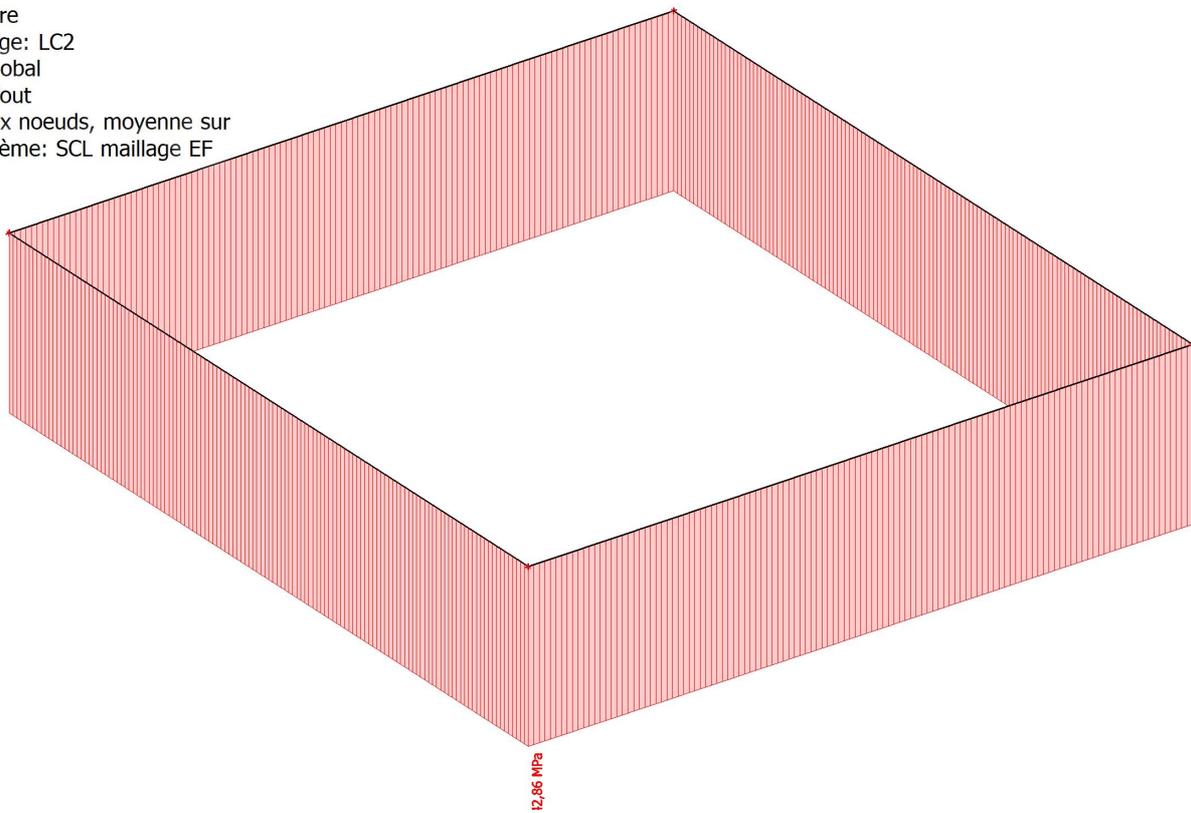
Calcul linéaire

Cas de charge: LC2

Extrême: Global

Sélection: Tout

Position: Aux noeuds, moyenne sur macro. Système: SCL maillage EF



5. EXPECTED AFNOR RESULTS

Bending moment =2380,95Nm/m

Maximum stress= 142,857 MPa

REFERENCE : "Guide de validation des progiciels de calcul de structures" AFNOR, 1990